

**July 10, Week 6**

Today: Finish Chapter 10, Begin Chapter 7, Rotational Motion

Homework #6 due tomorrow

# General Energy Conservation III

$$\frac{1}{2}mv_i^2 + mgy_i + \frac{1}{2}ks_i^2 + W_{other} = \frac{1}{2}mv_f^2 + mgy_f + \frac{1}{2}ks_f^2$$

Example: An  $80\text{ kg}$  man jumps onto a spring platform ( $k = 18000\text{ N/m}$ ) going  $9\text{ m/s}$ . How far does he compress the spring?

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Example: An  $80\text{ kg}$  man jumps onto a spring platform ( $k = 18000\text{ N/m}$ ) going  $9\text{ m/s}$ . How far does he compress the spring?

Example: An  $80\text{ kg}$  man skydives from a plane  $1600\text{ m}$  above the ground. If he lands with a speed of  $10\text{ m/s}$  (and was essentially at rest when he jumped), how much work did his parachute do?

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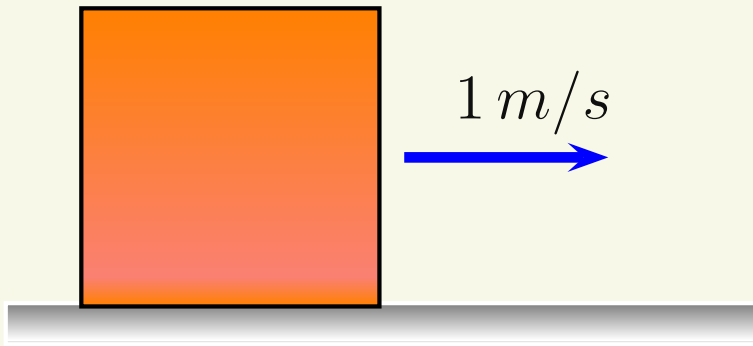
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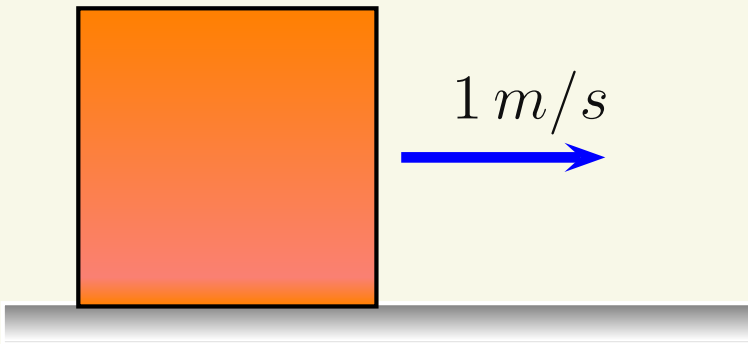
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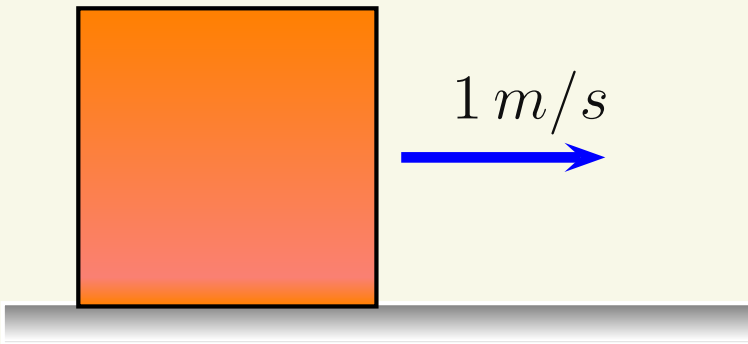


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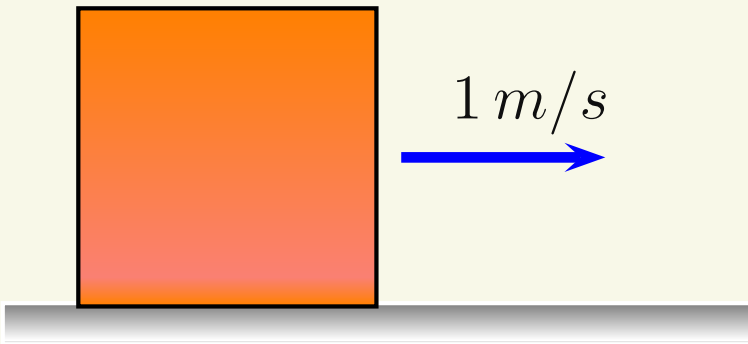
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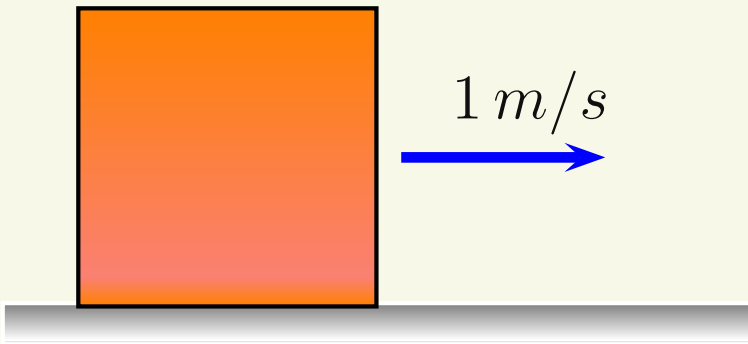
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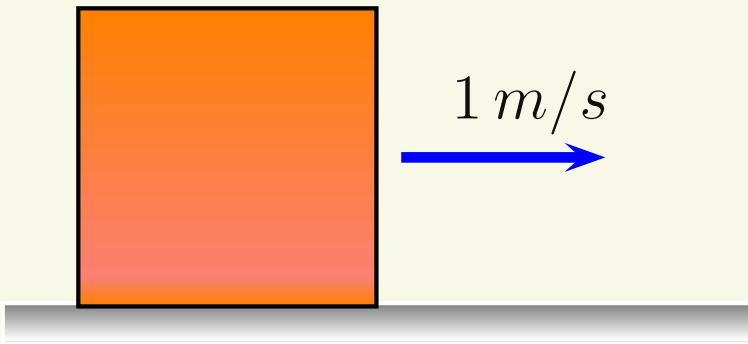
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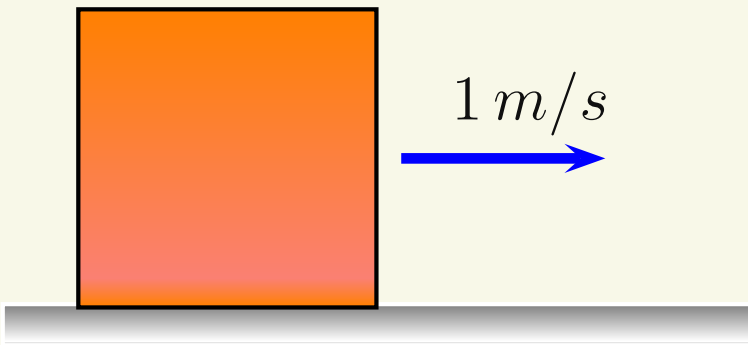
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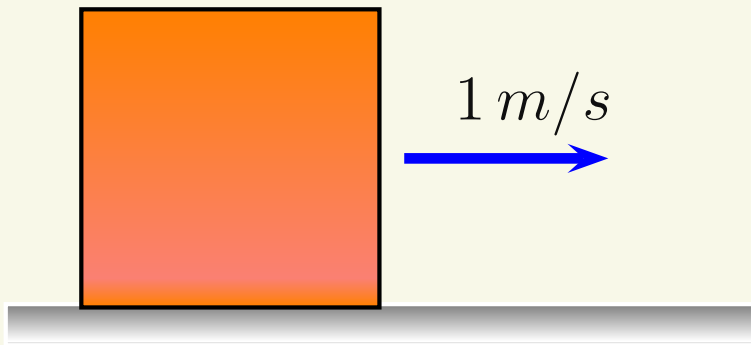
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$$\text{No springs or gravity} \Rightarrow \frac{1}{2}mv_i^2 = \frac{1}{2}mv_f^2 + \Delta E_{th}$$

$$v_i = 3\text{ m/s}, v_f = 0 \Rightarrow 45\text{ J} = 0 + \Delta E_{th}$$



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$$1 \, hp = 550 \, lb \cdot ft/s = 746 \, Watt$$

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 Non-negligible size, *i.e.*, can't be treated as a particle

# Rotational Axis

All rotation occurs about an axis.



# Rotational Axis

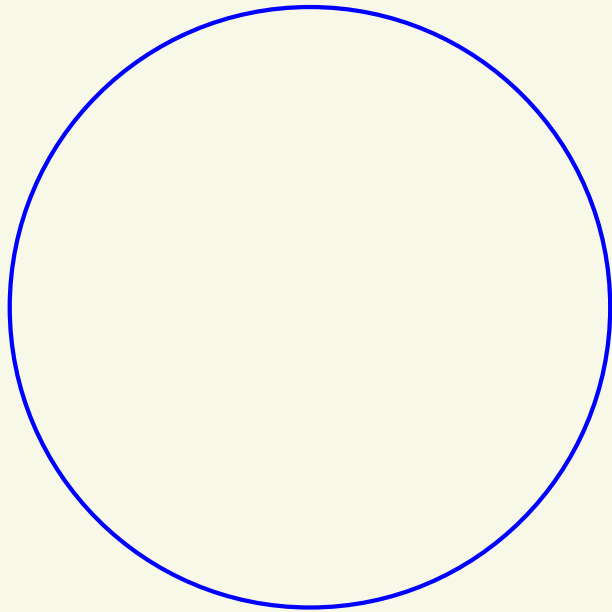
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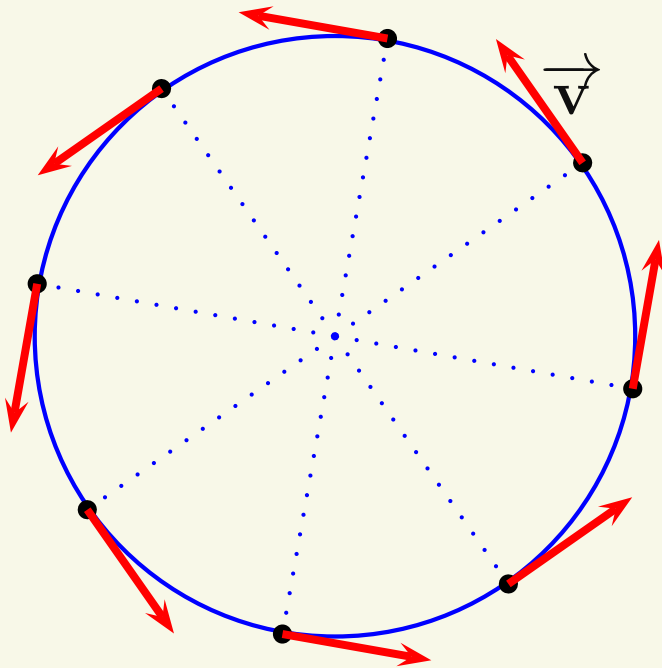


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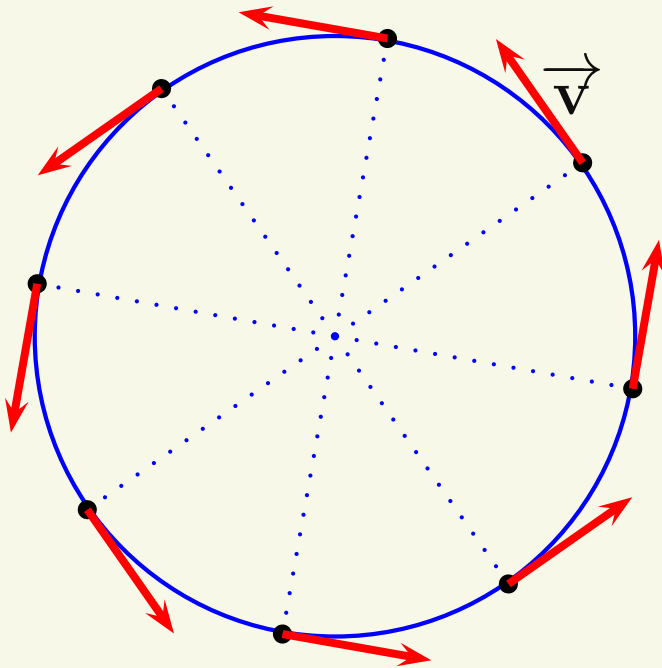


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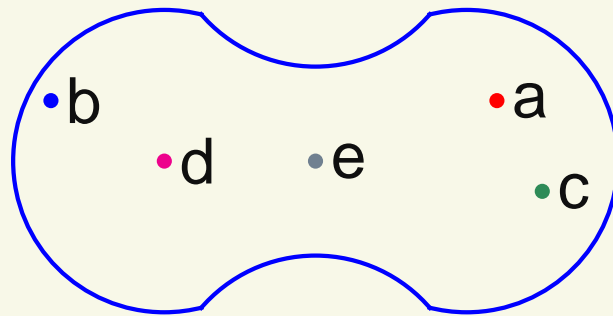


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The rotational axis is along the  $z$ -axis,  
*i.e.*, into and out of the page

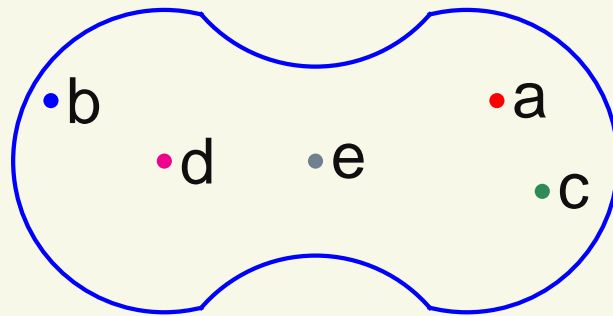
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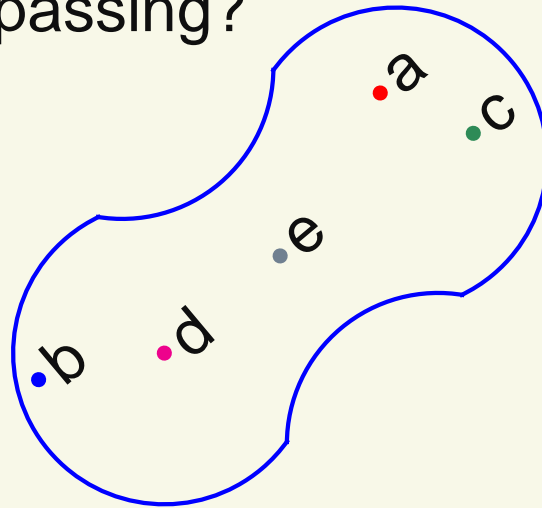
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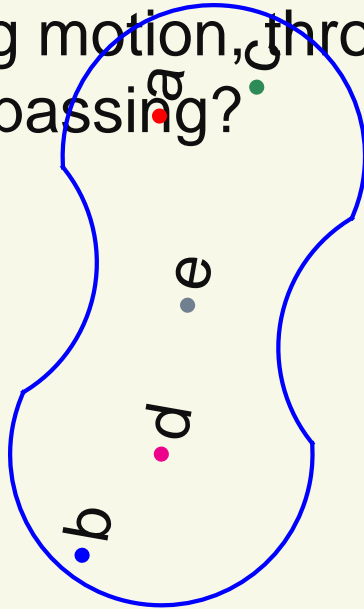
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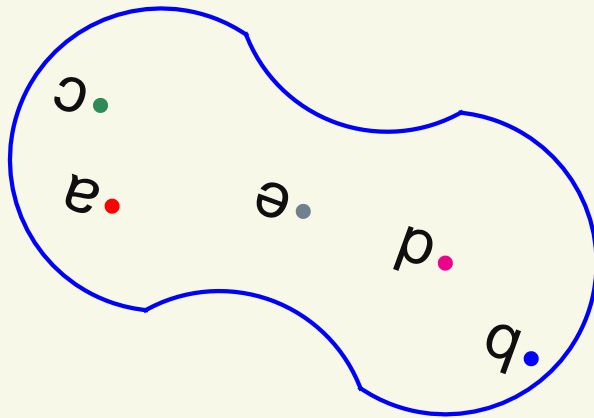
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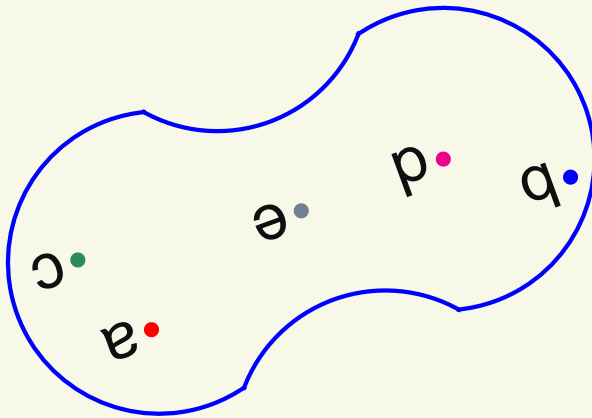
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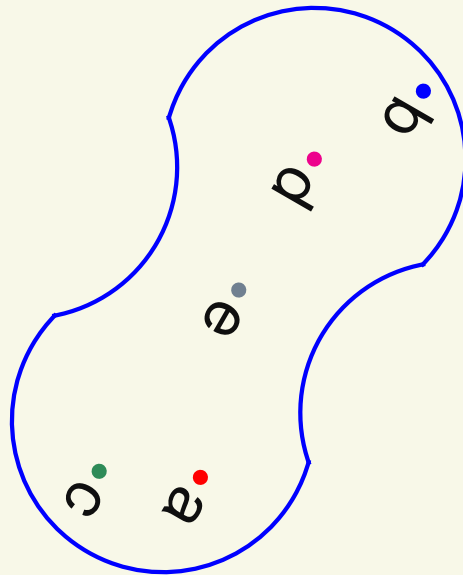
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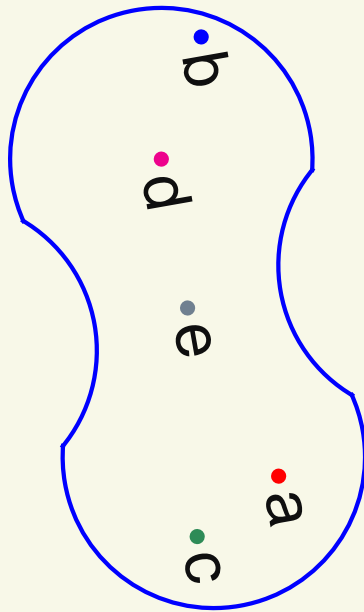
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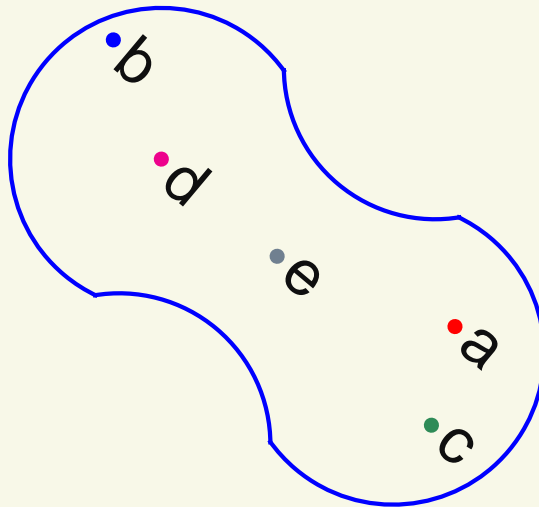
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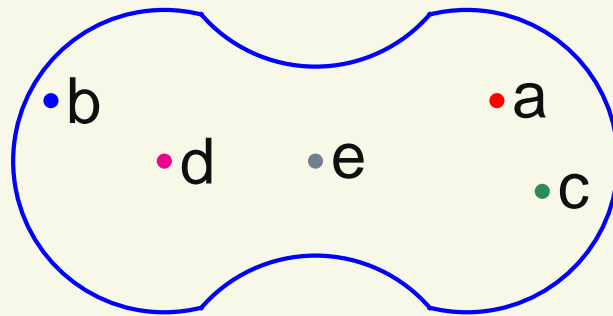
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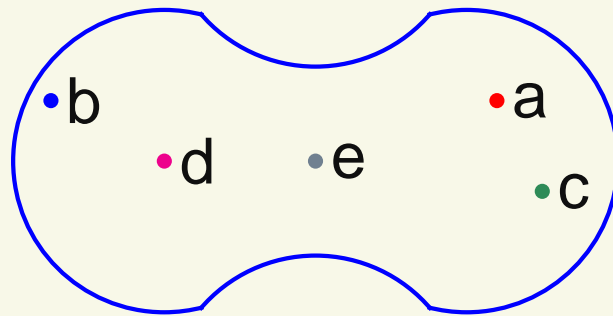
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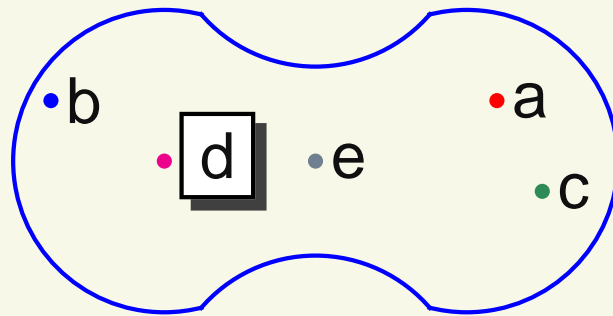
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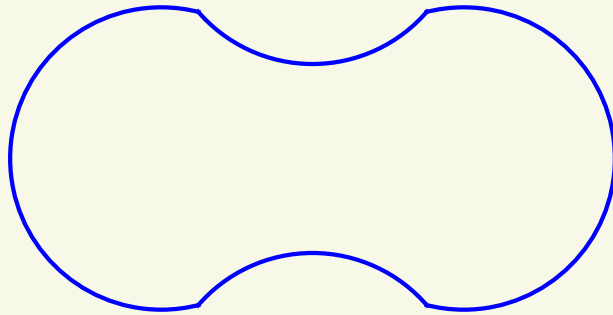
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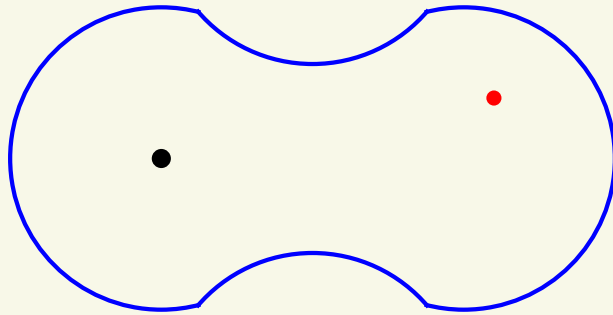
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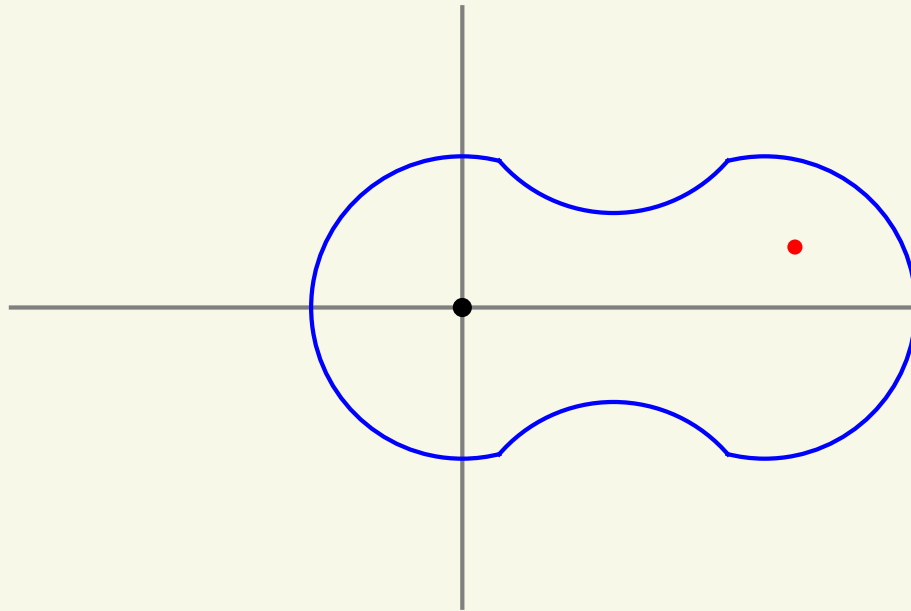
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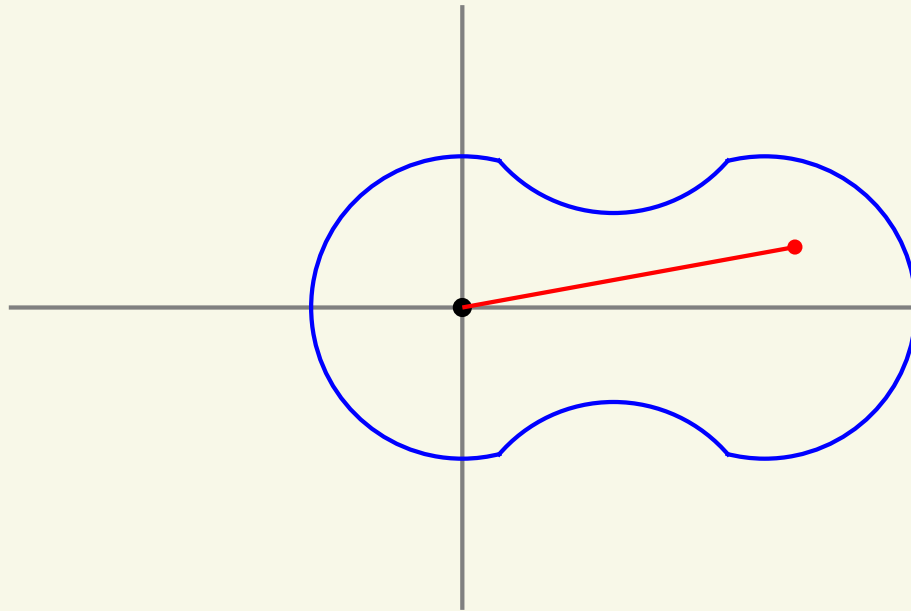
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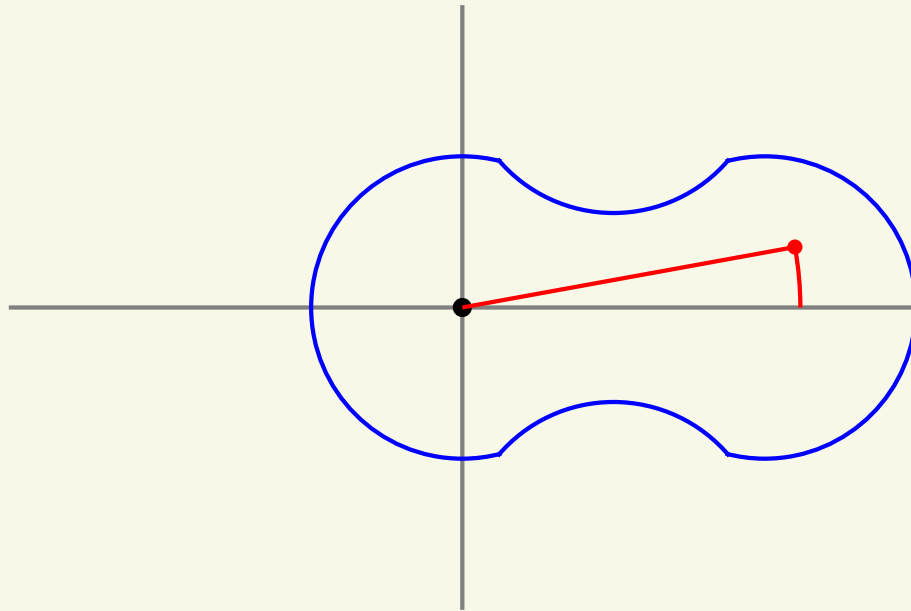
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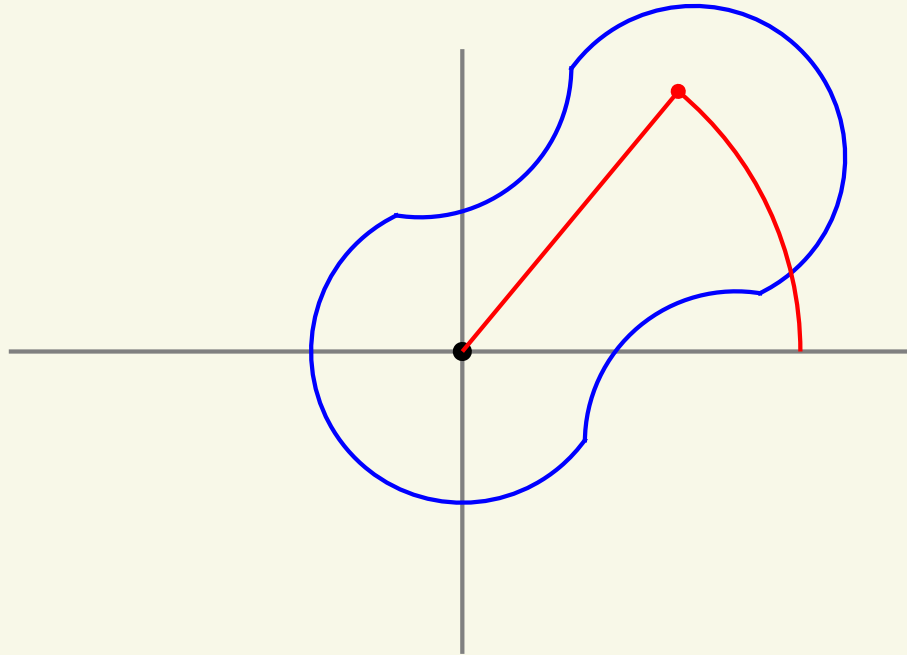
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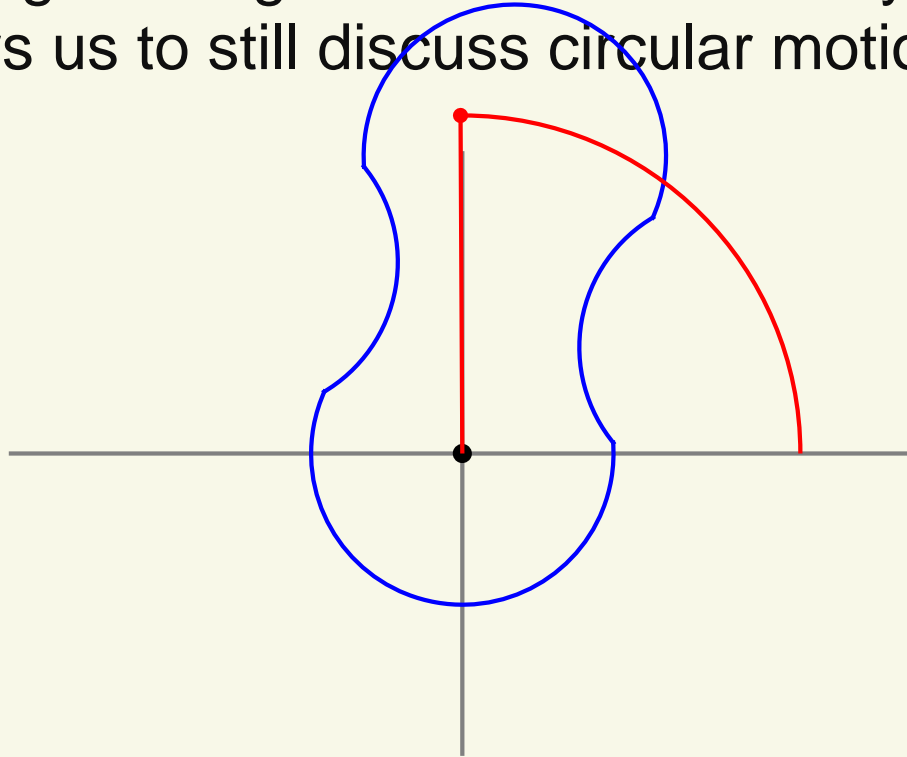
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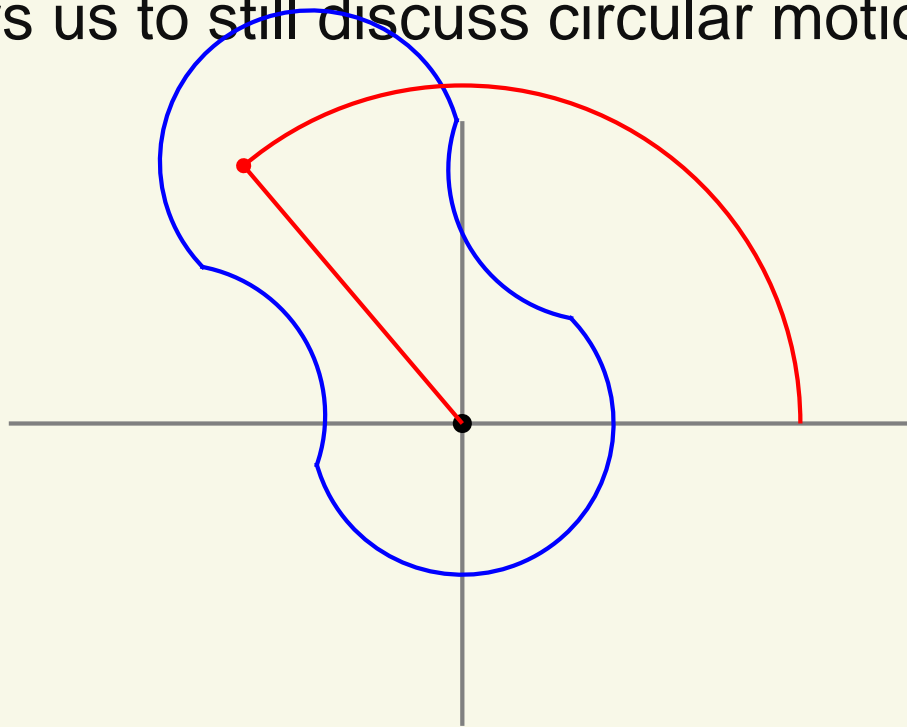


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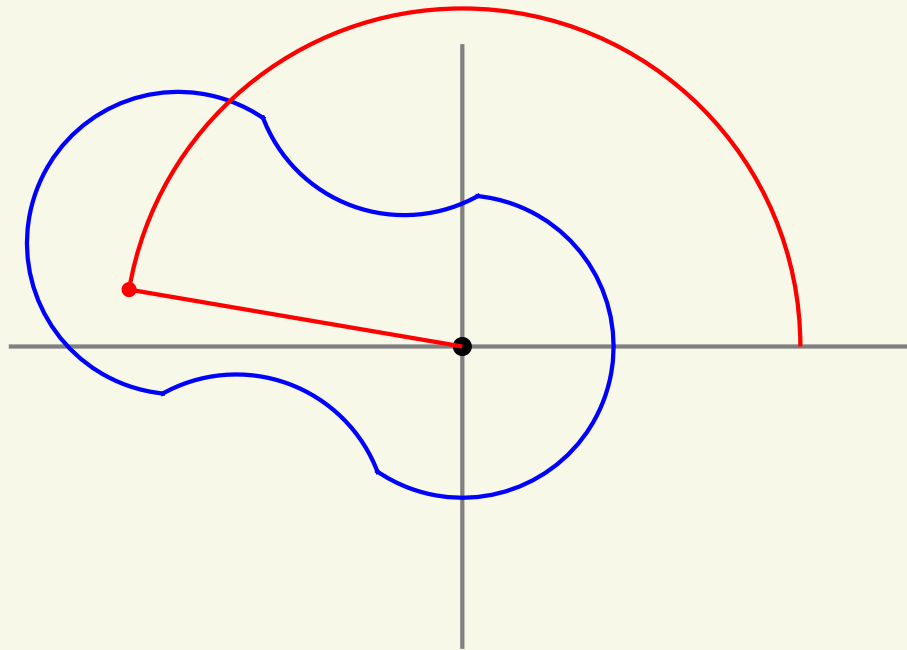
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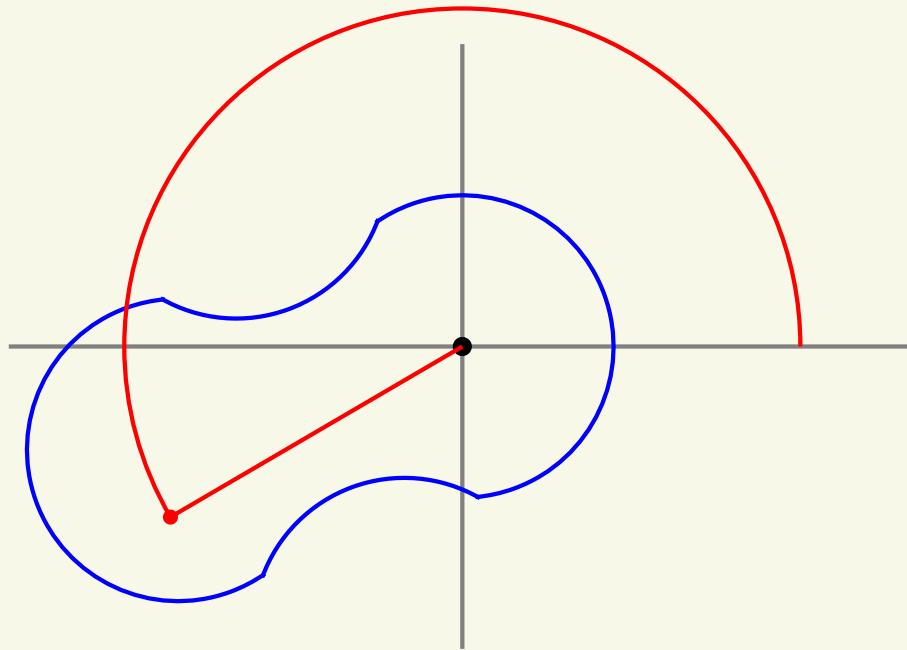
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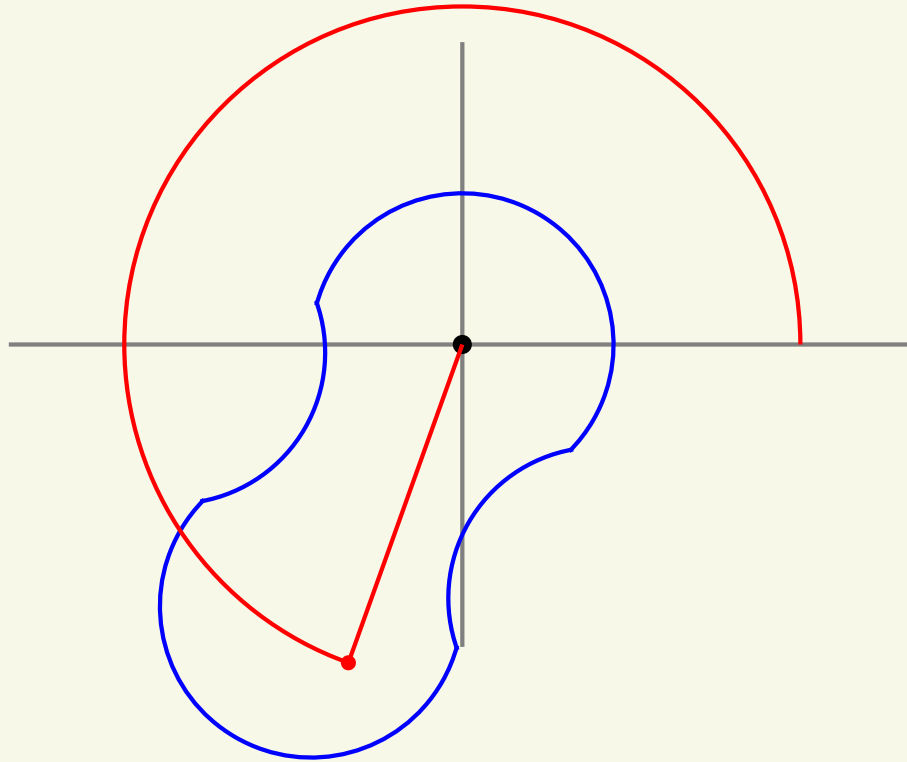
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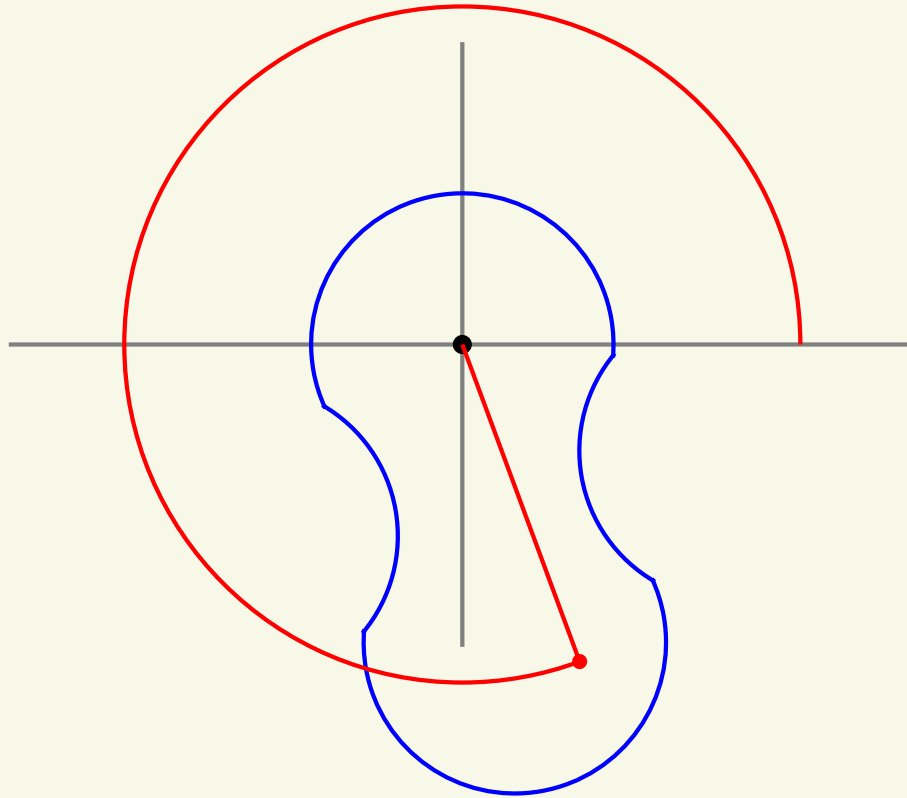
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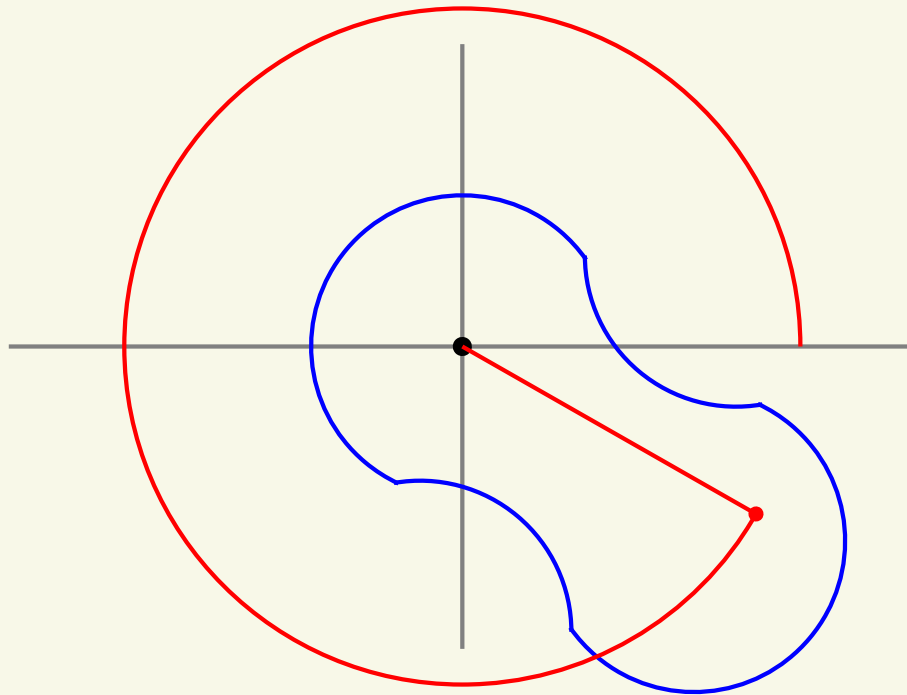
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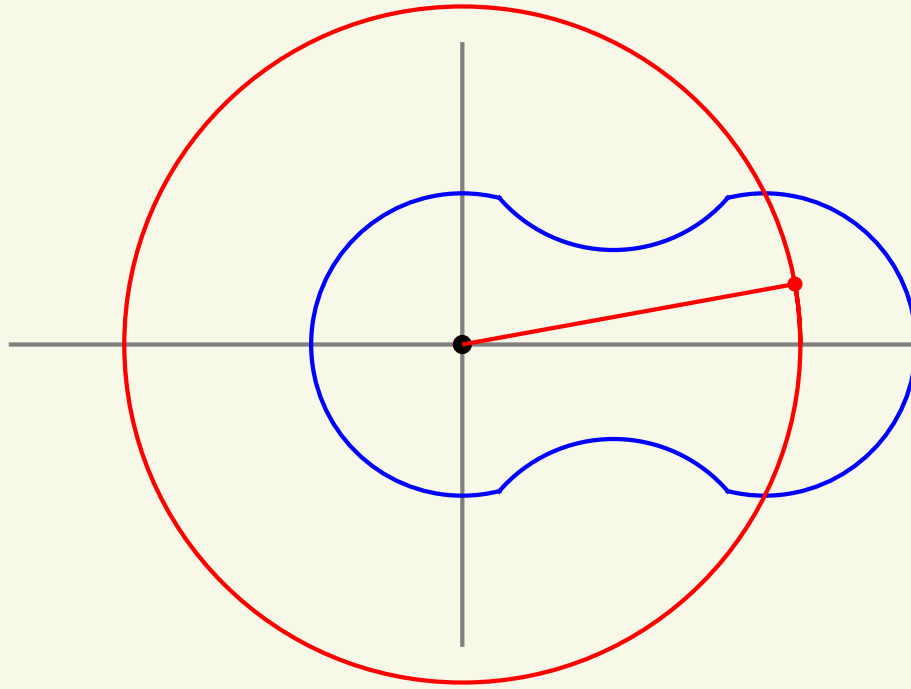
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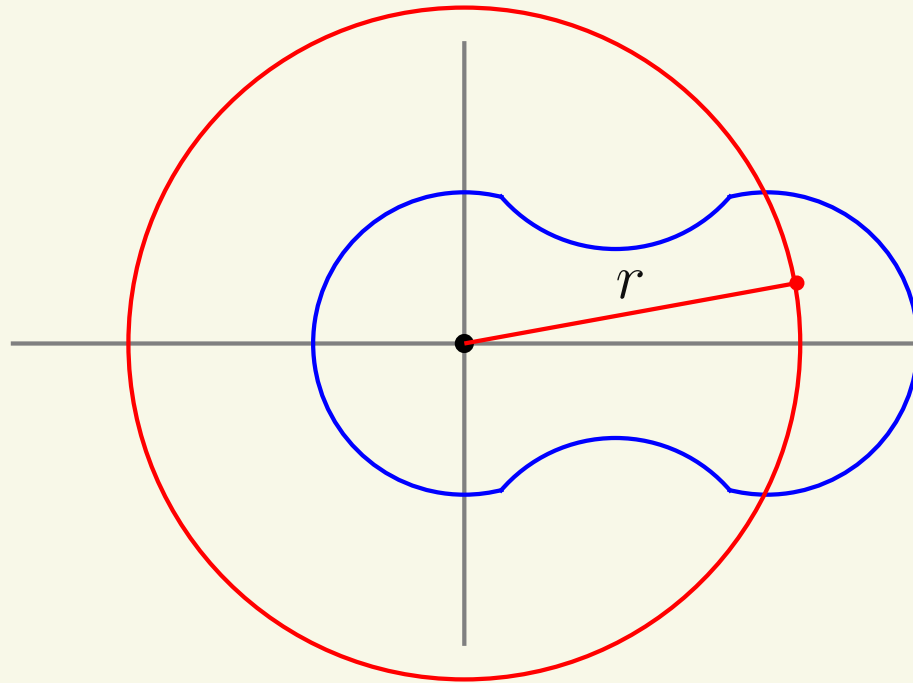
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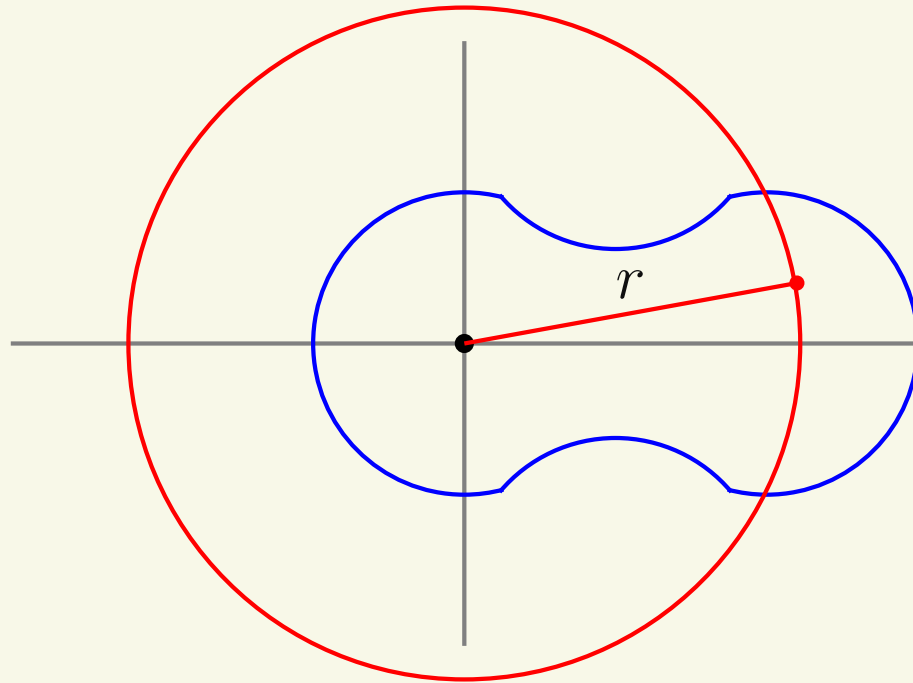


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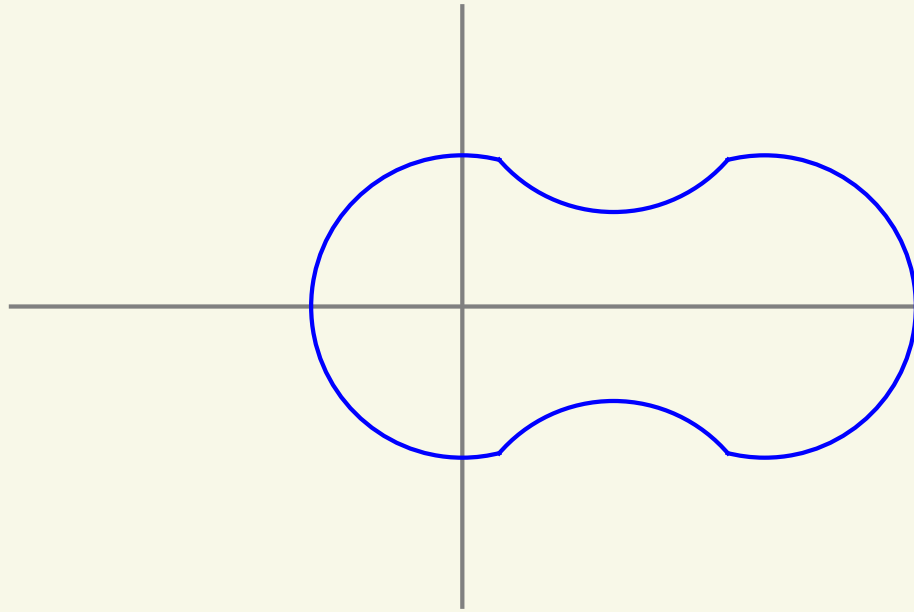


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$r$  = distance from axis of rotation

# Why Rotational Motion

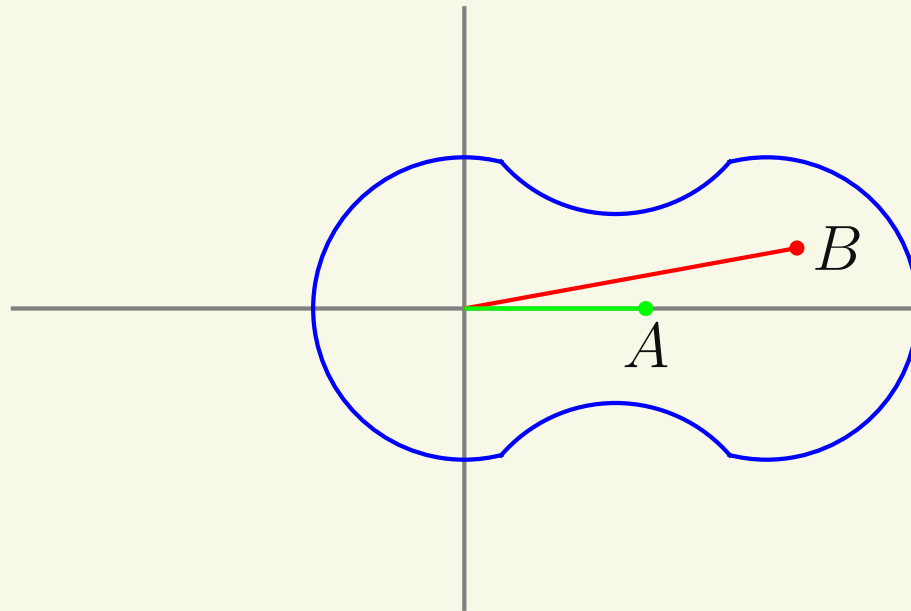
The motion of a rigid body is very different than a particle



Pick two points

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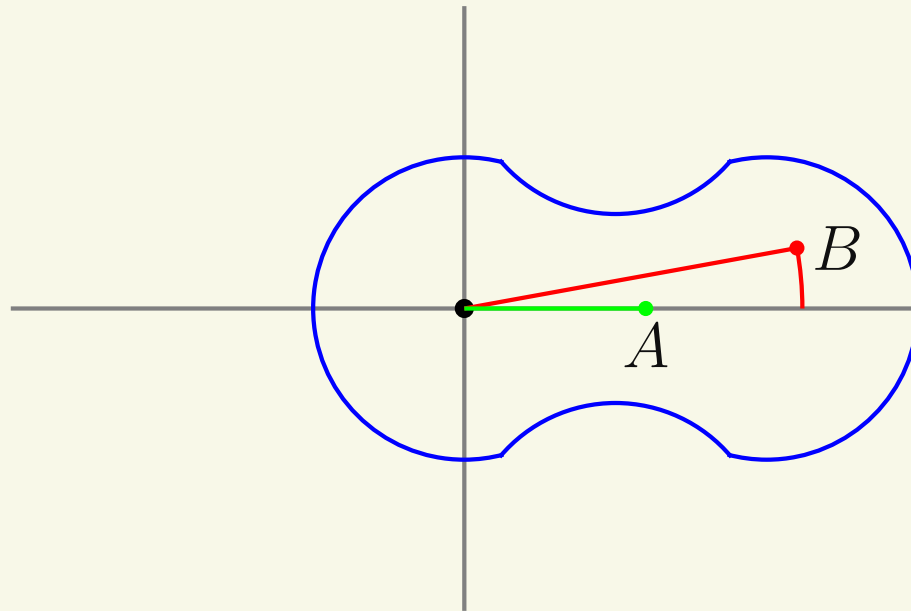
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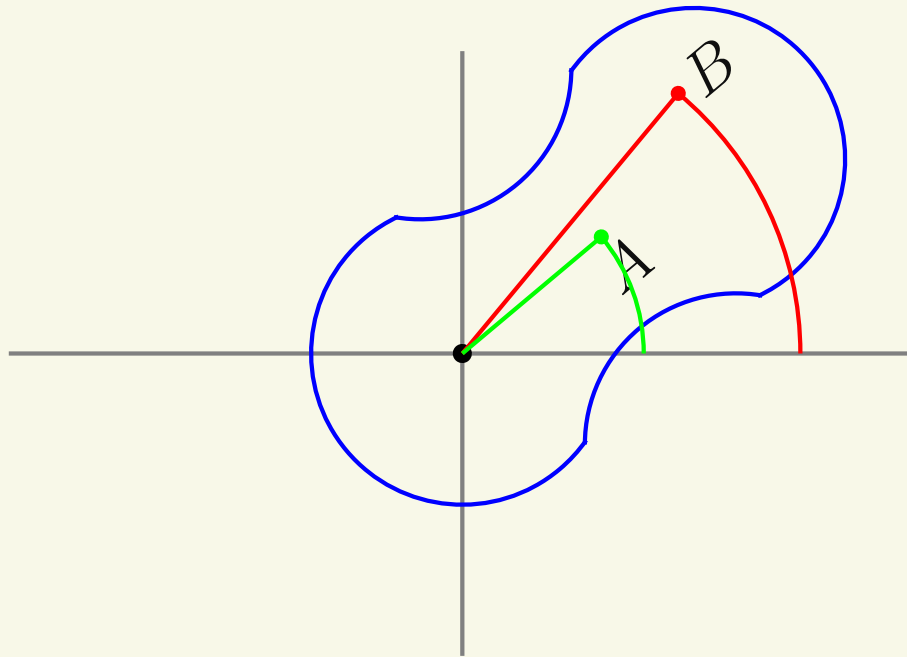
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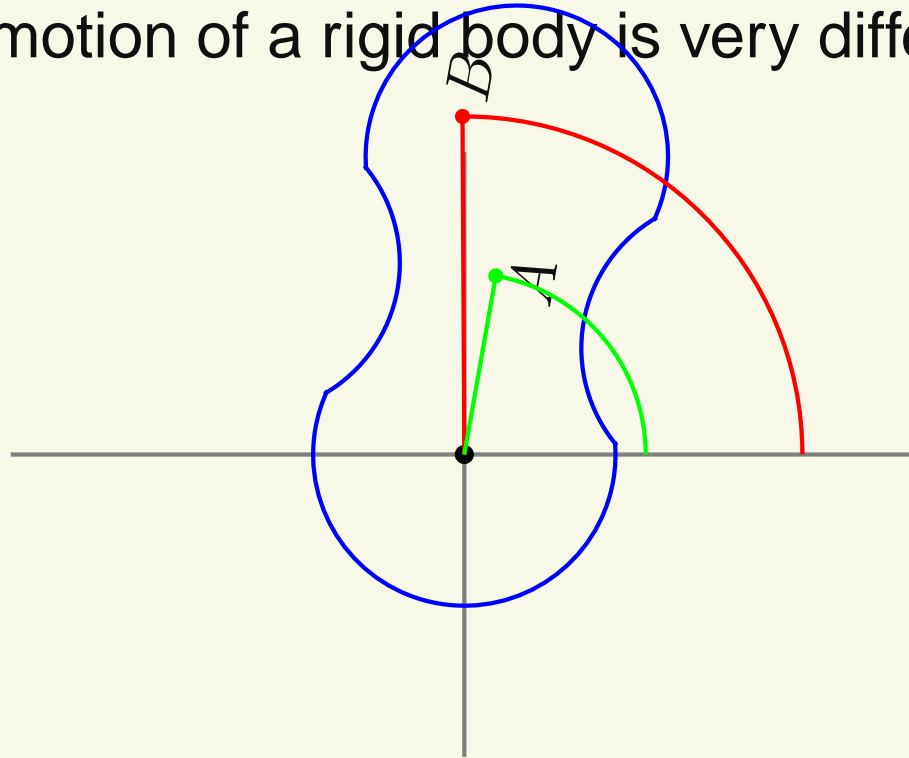
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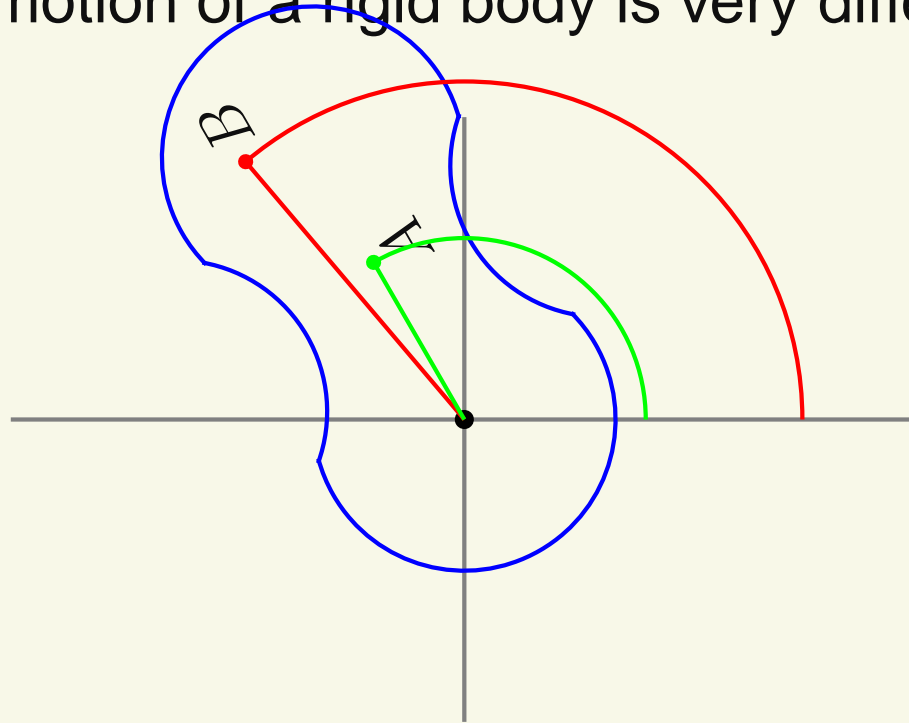
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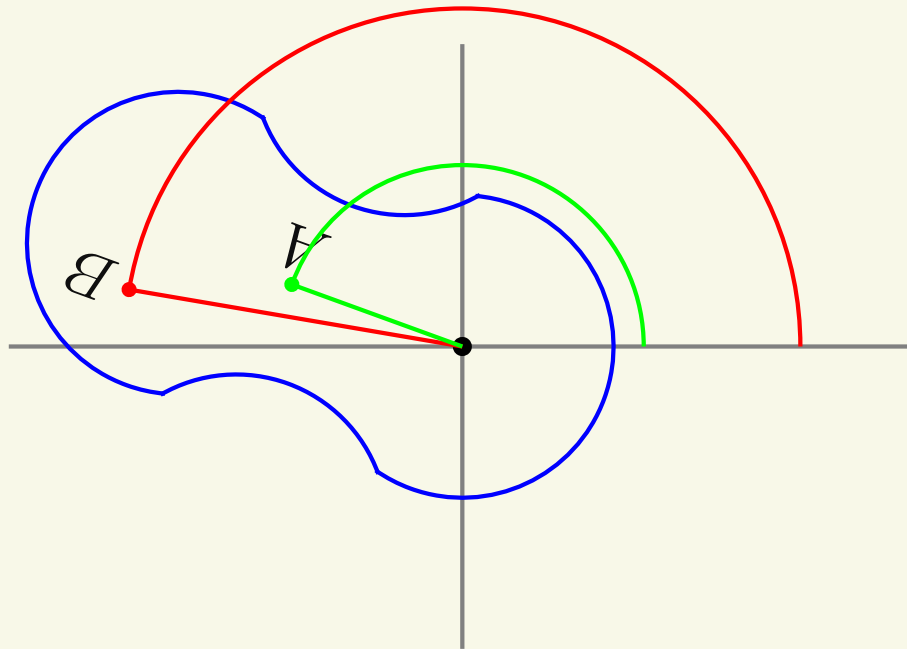
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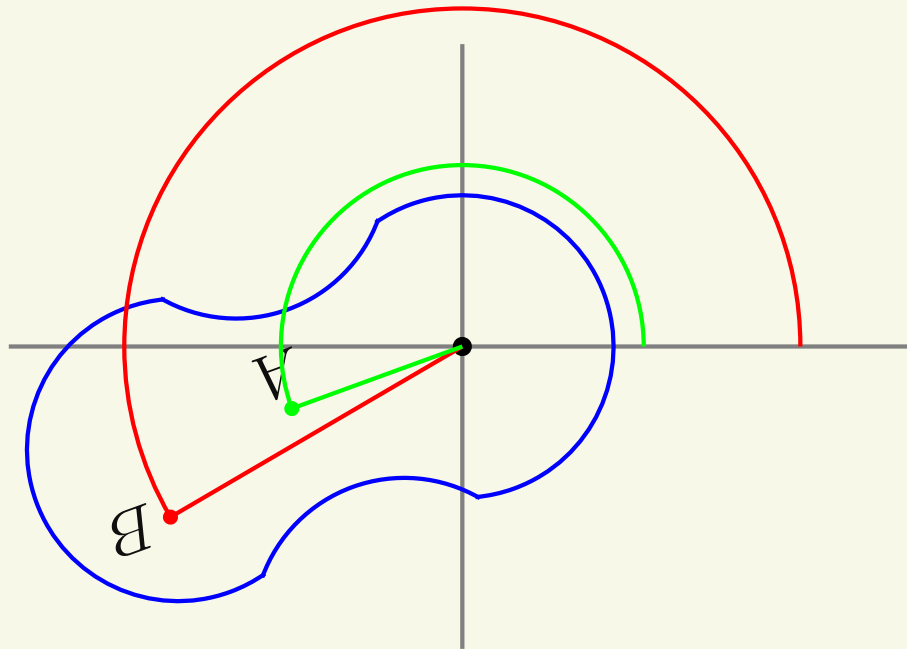


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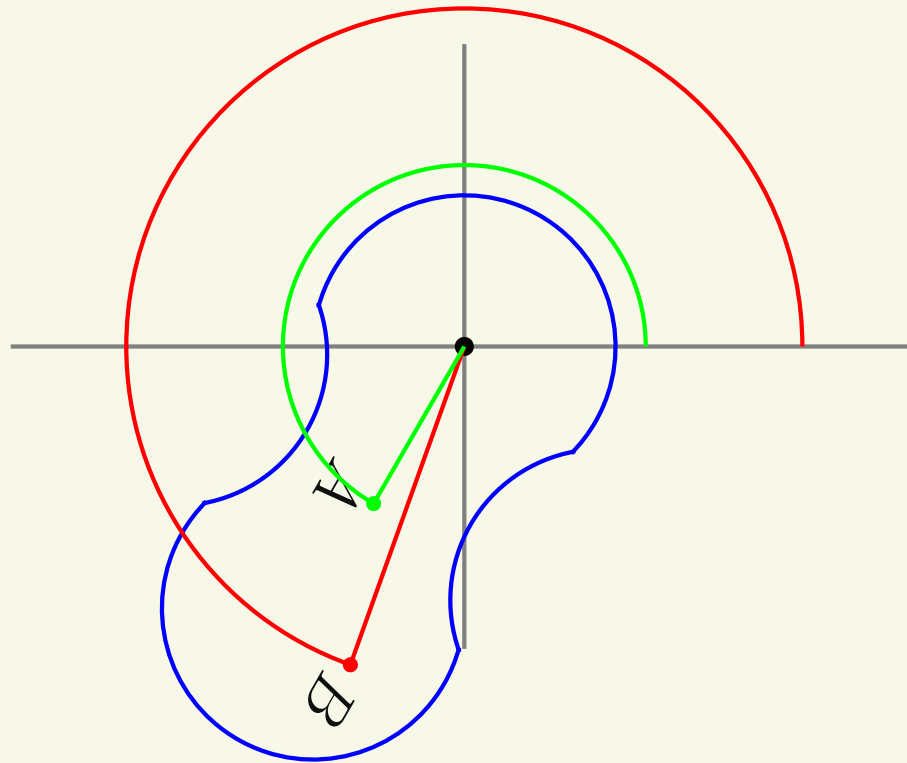
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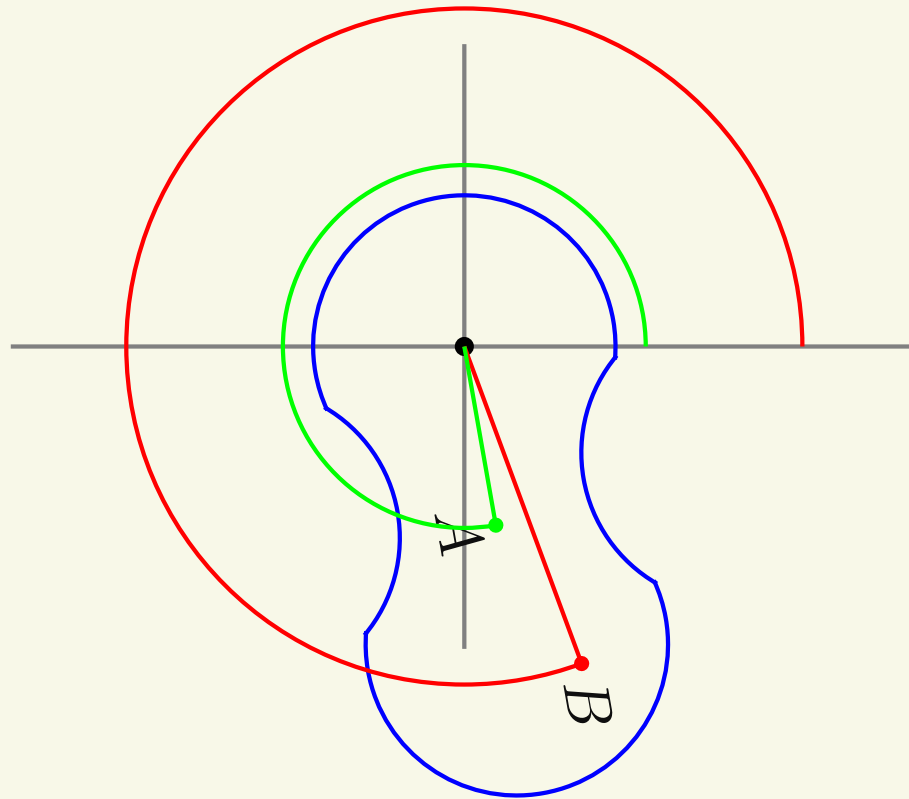
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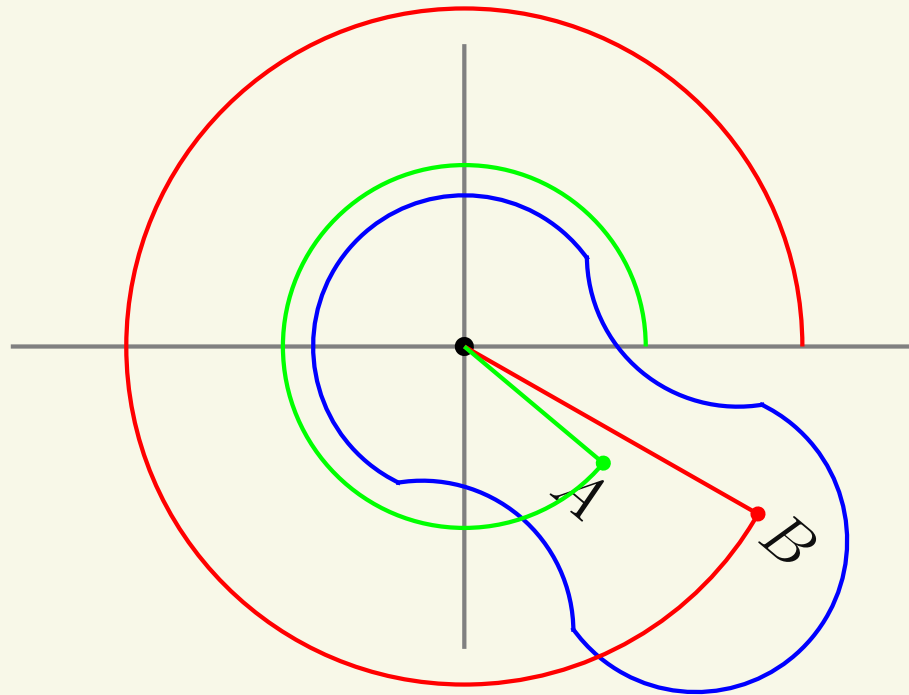
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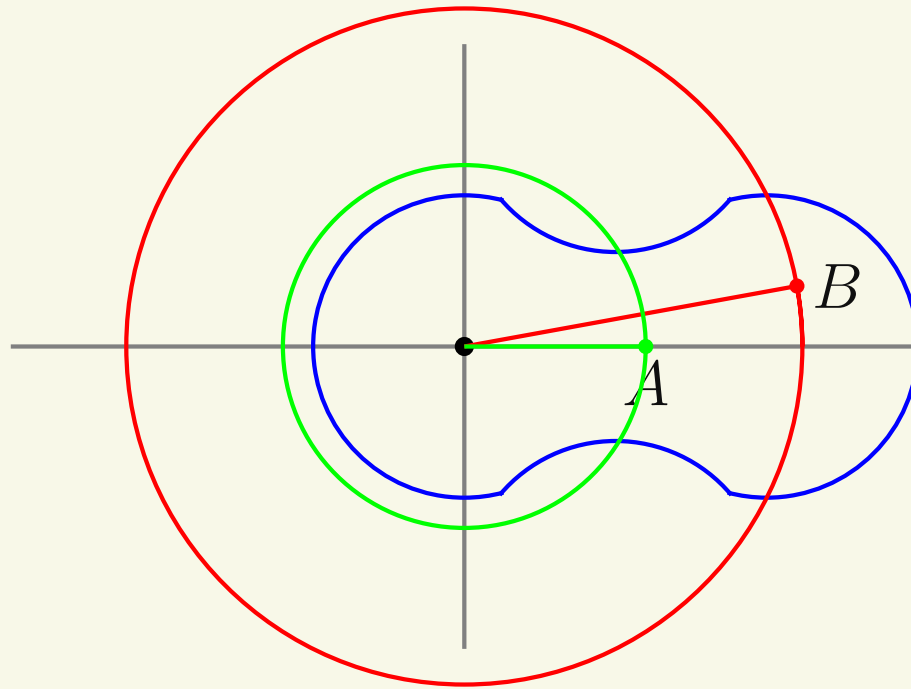
The motion of a rigid body is very different than a particle



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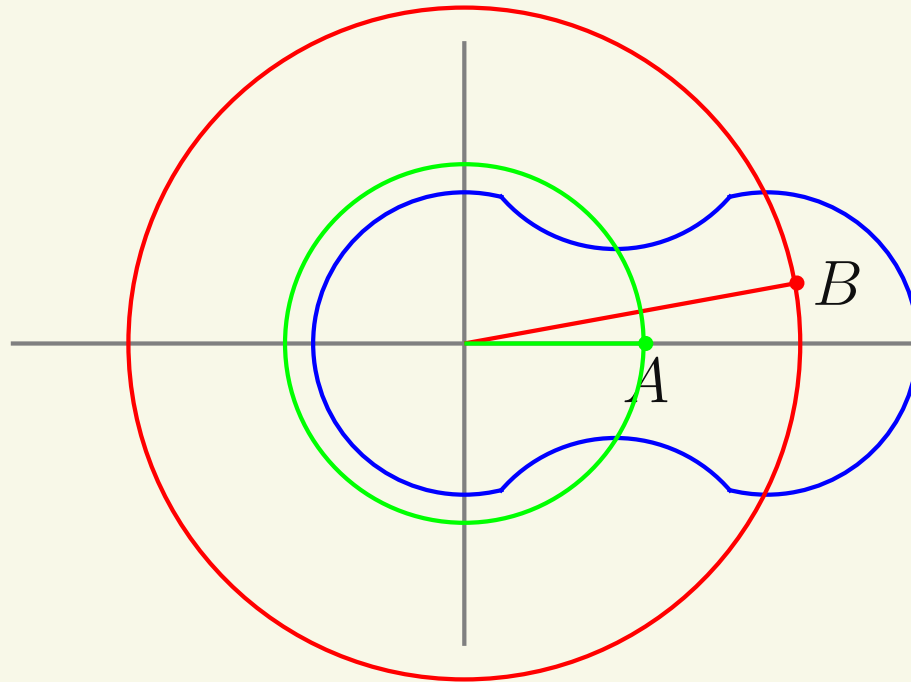
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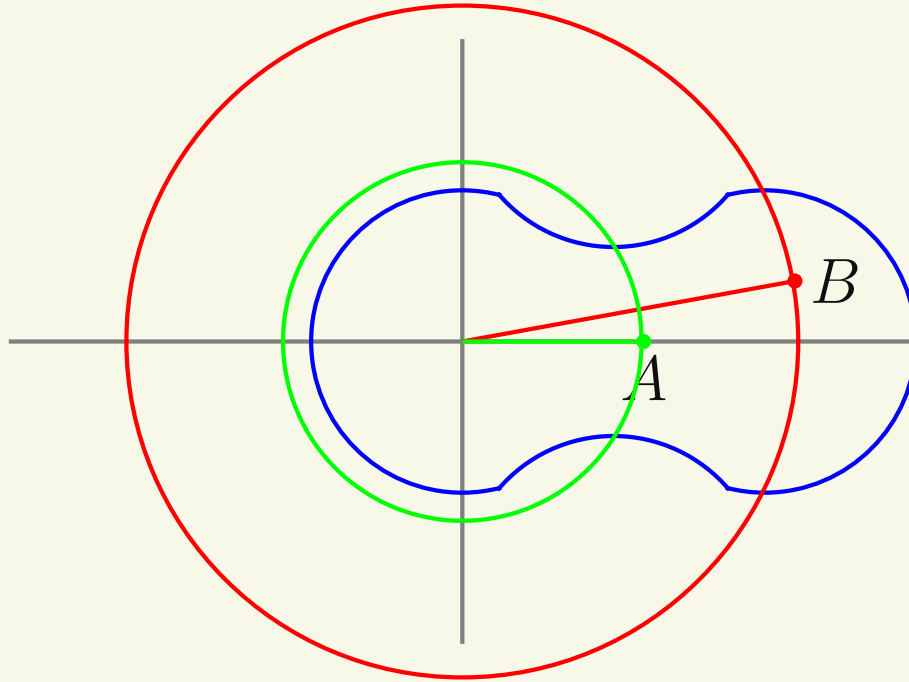


Pick two points

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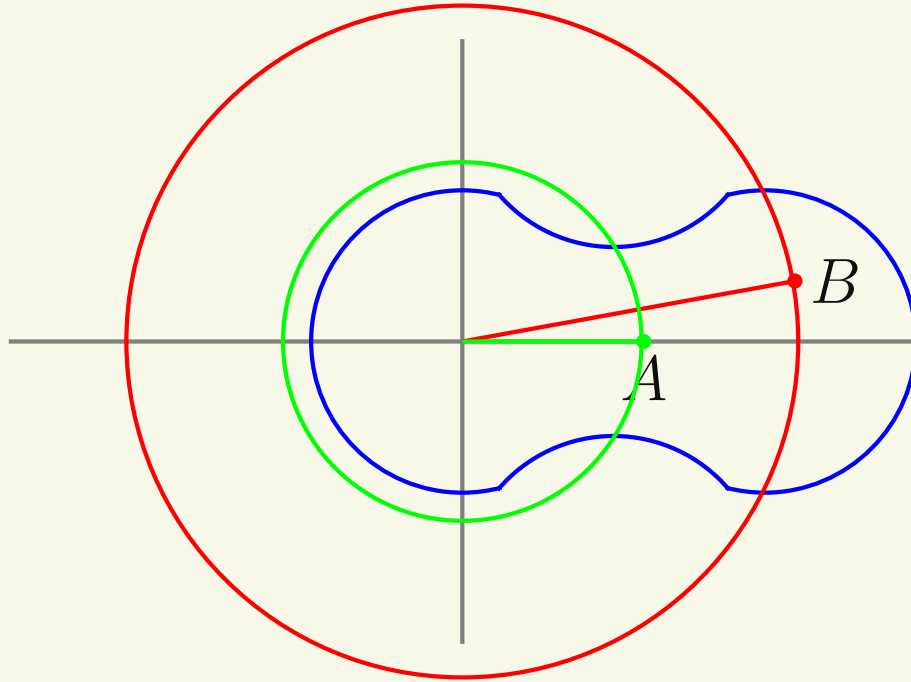
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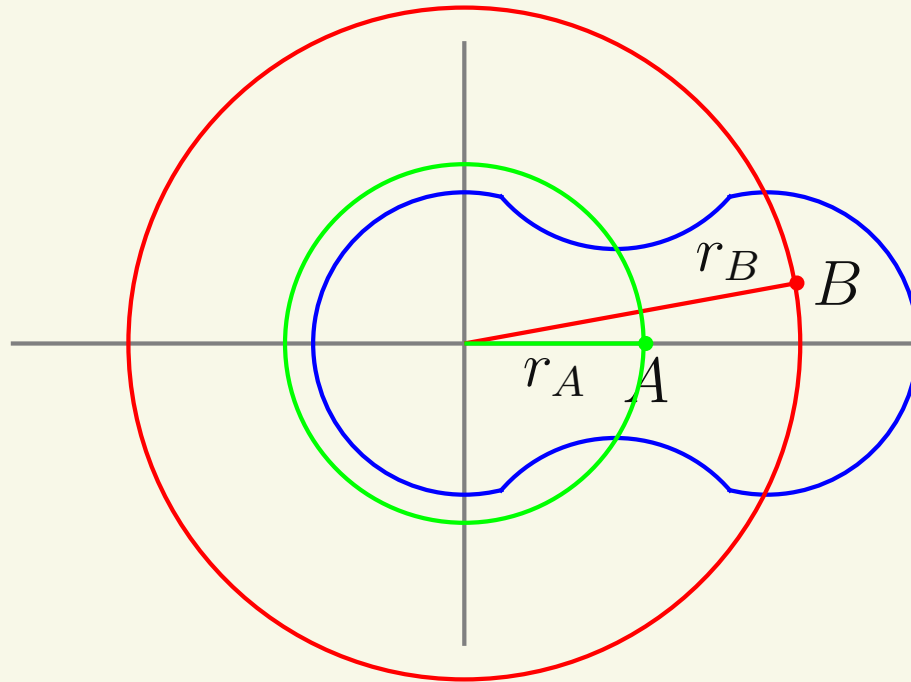
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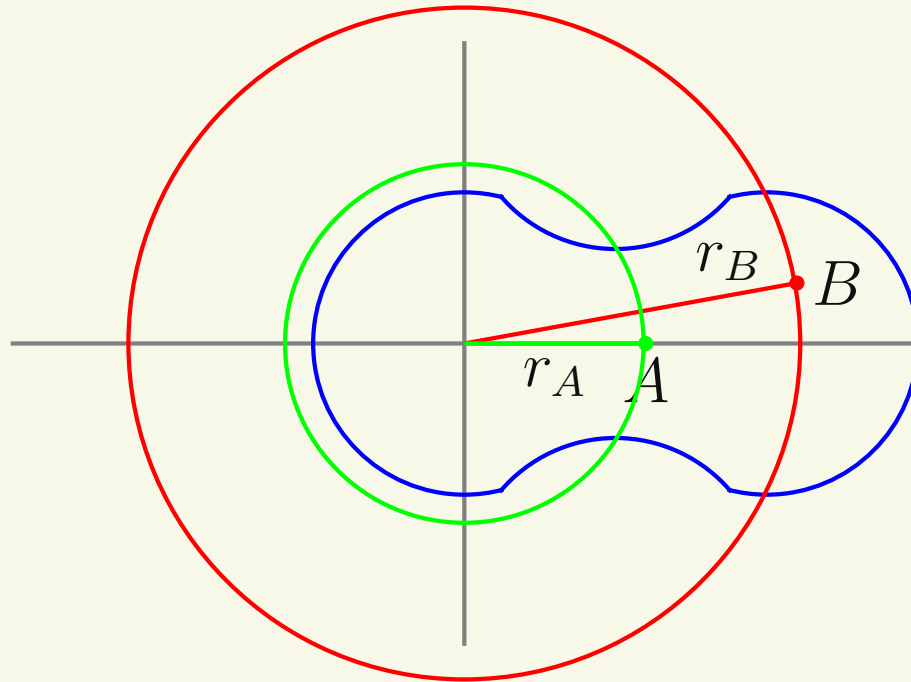
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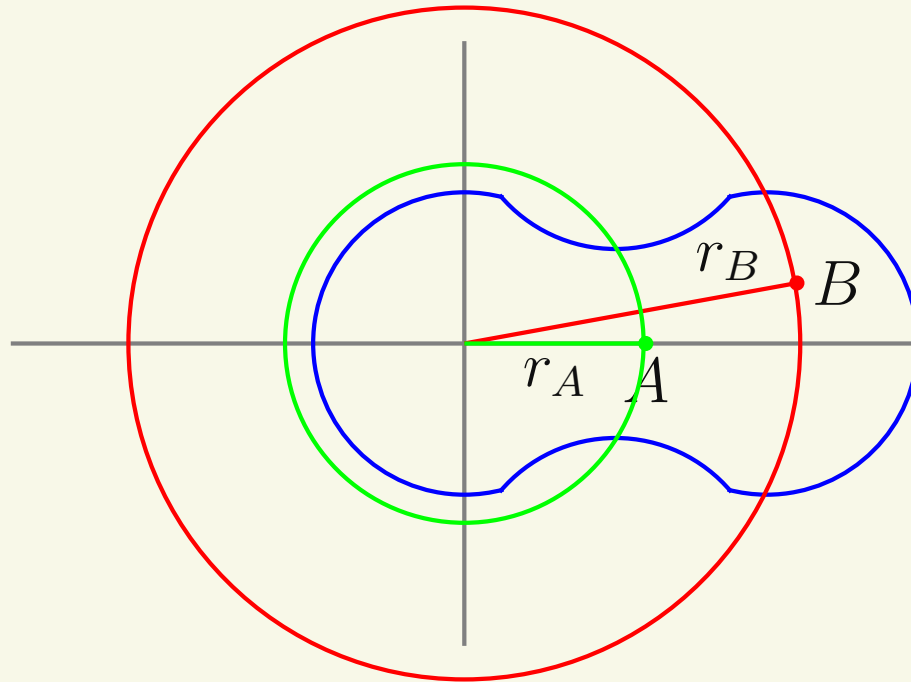
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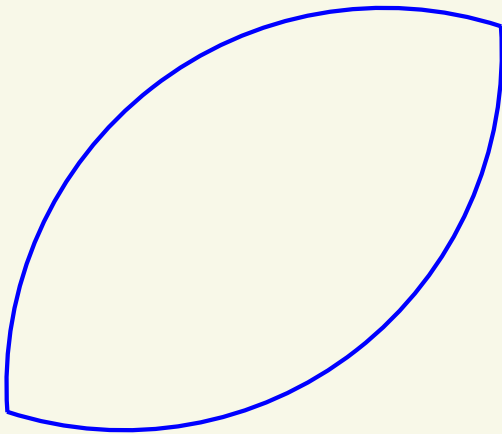
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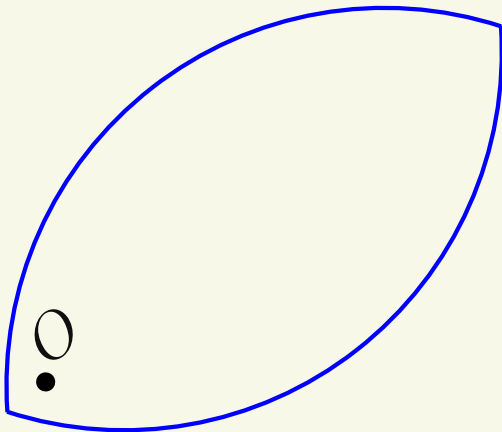
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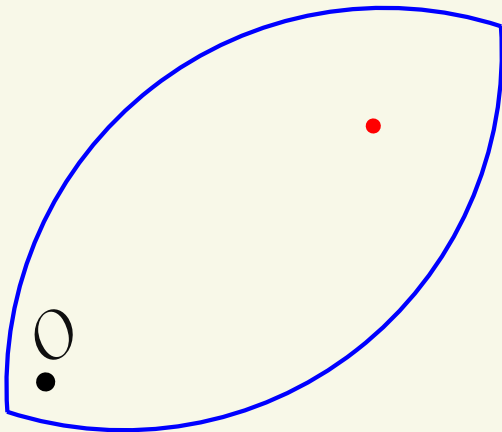
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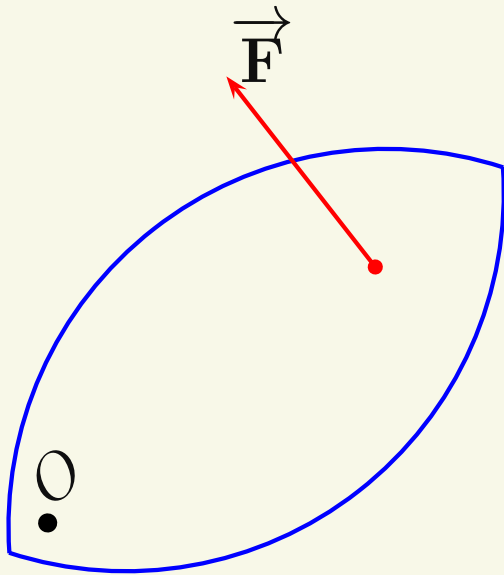


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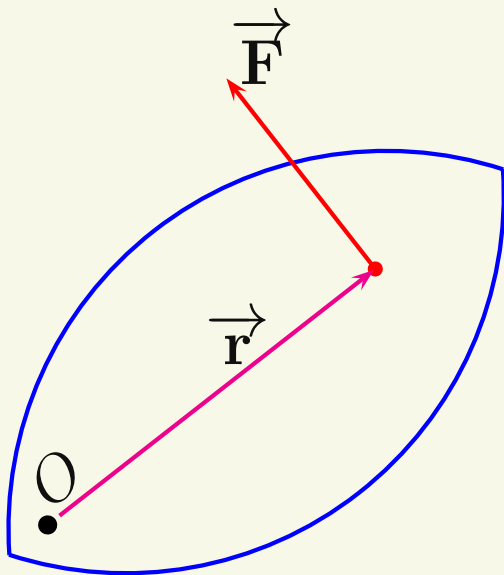
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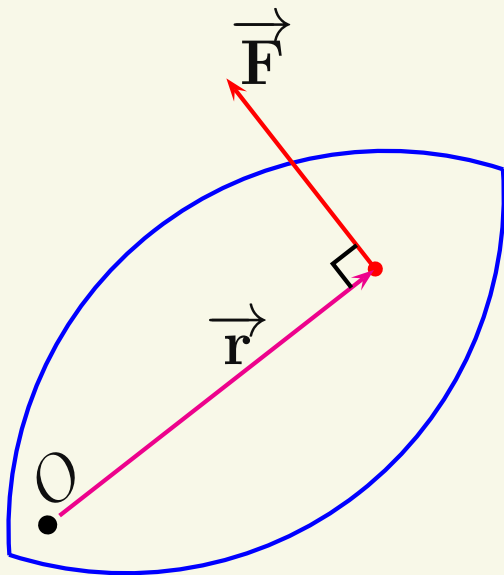
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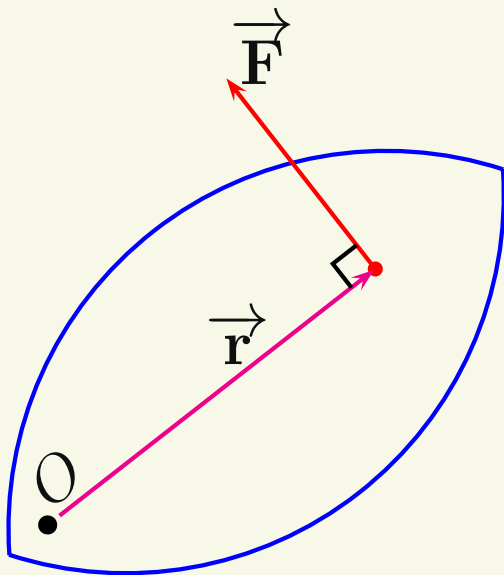
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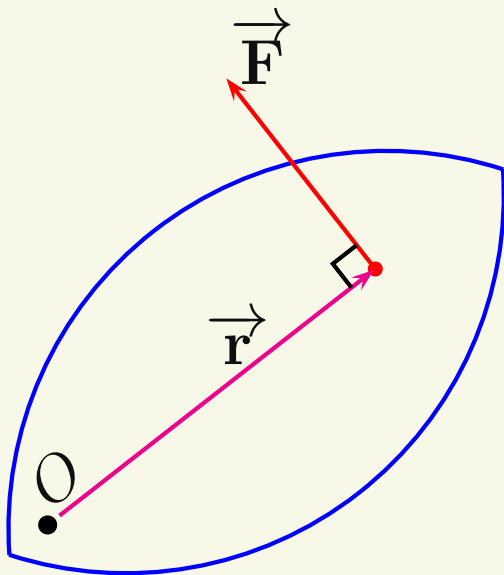


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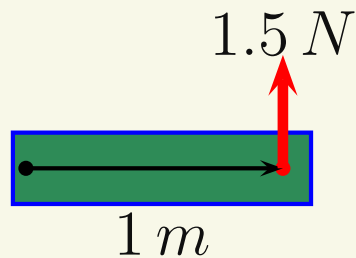
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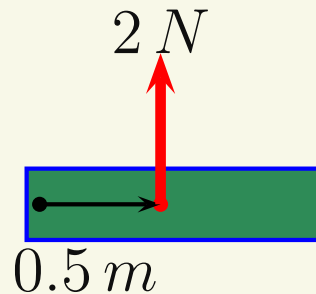
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For the three situations shown, which is the correct ranking of torque from smallest to largest?

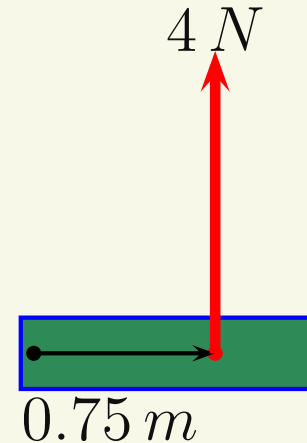
#1



#2

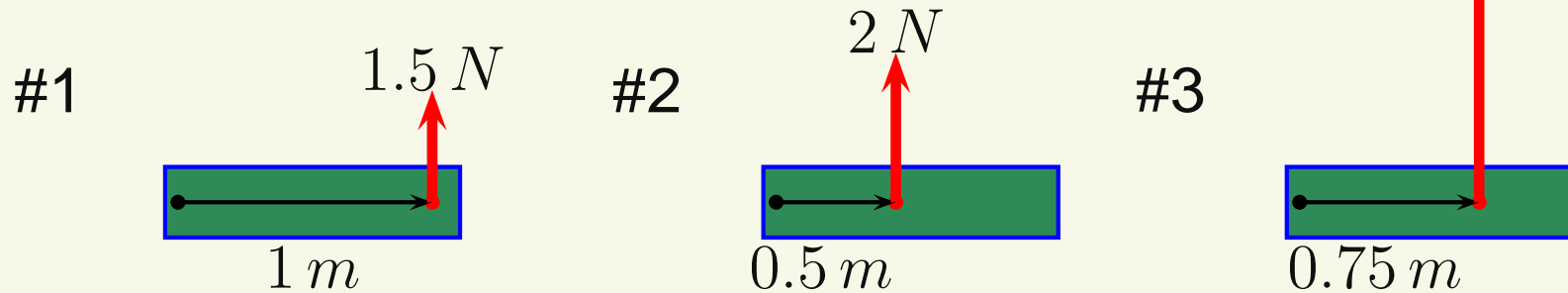


#3



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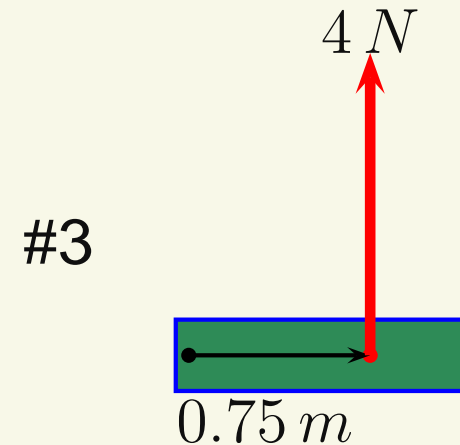
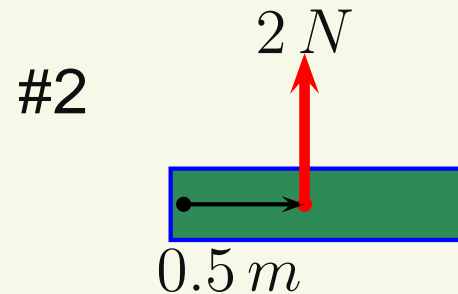
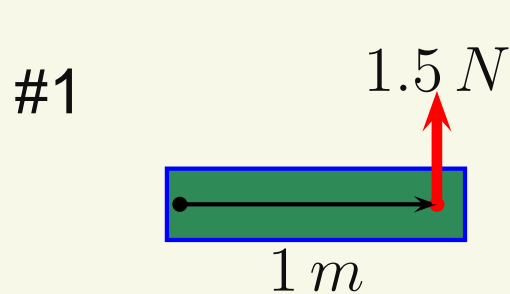
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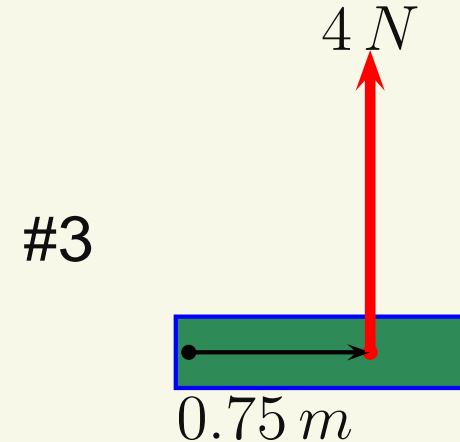
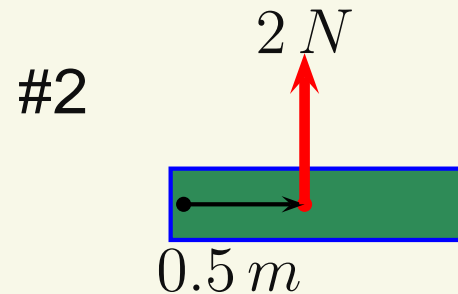
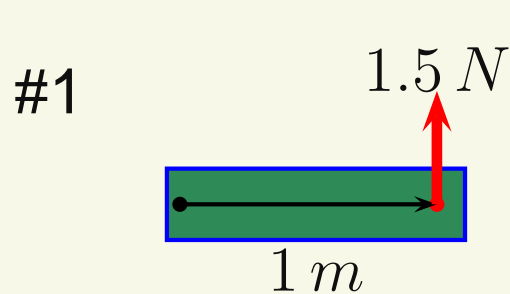


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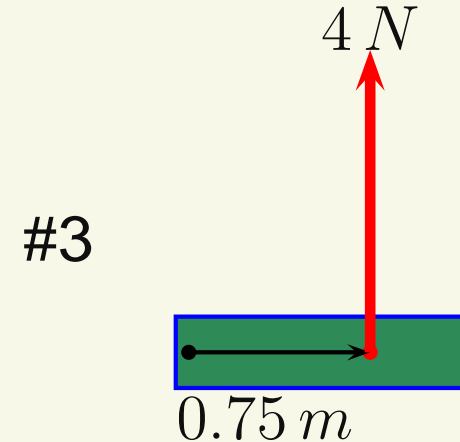
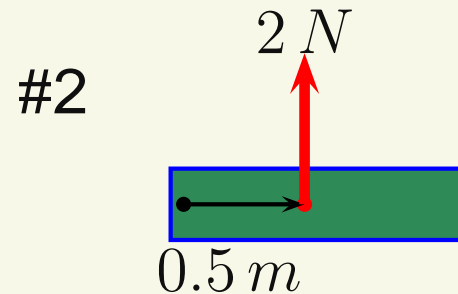
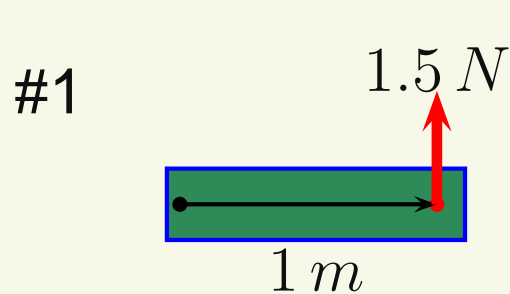
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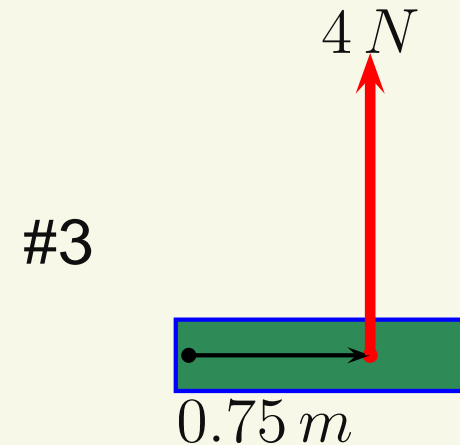
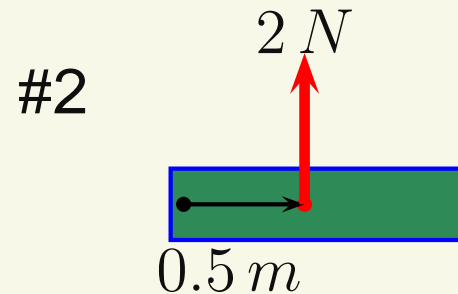
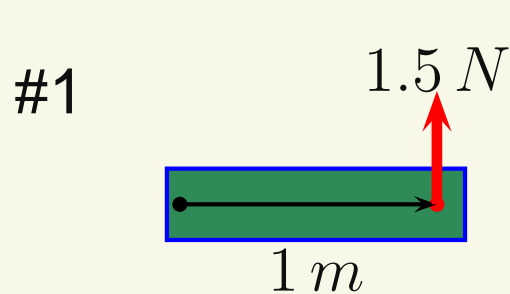
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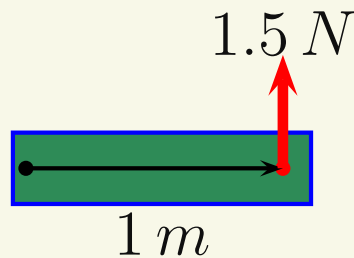
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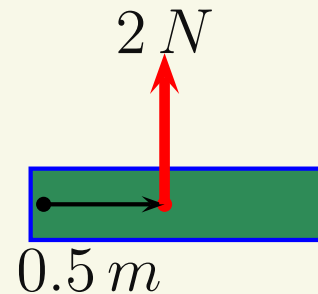
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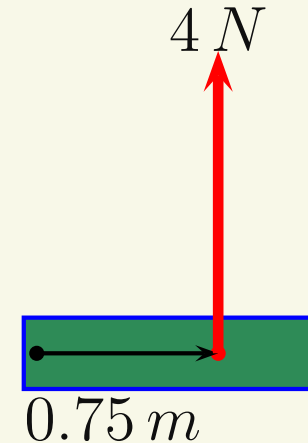
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#2



#3



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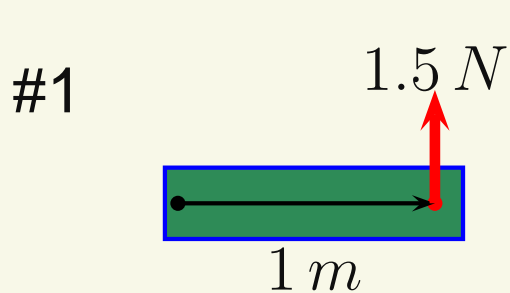
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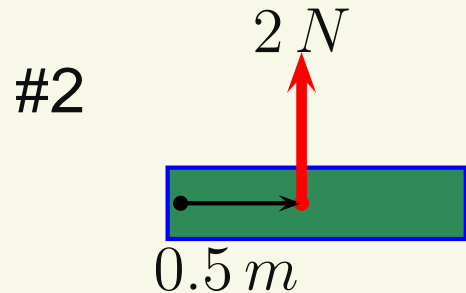


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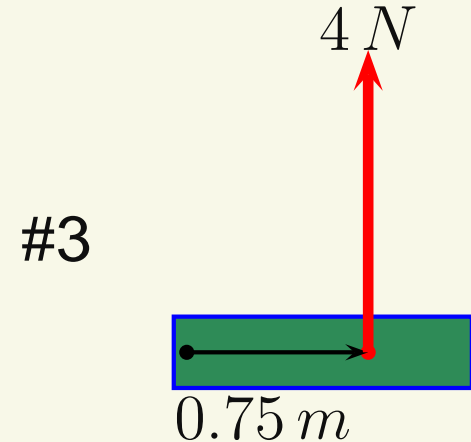
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$$\tau_1 = 1.5\text{ N} \cdot \text{m}$$



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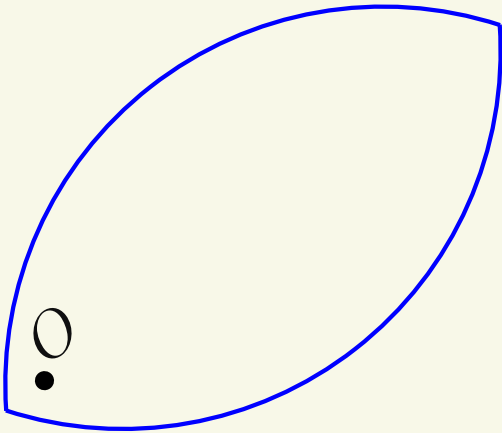
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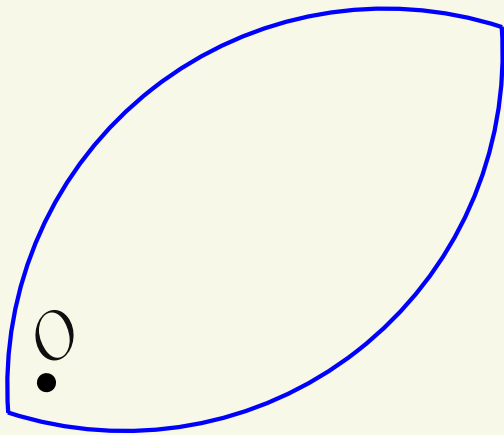
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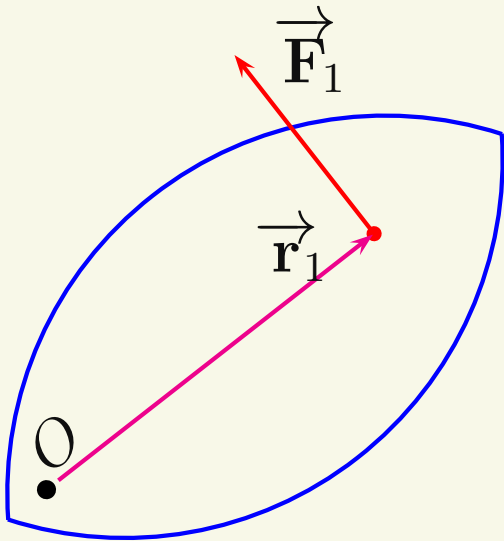
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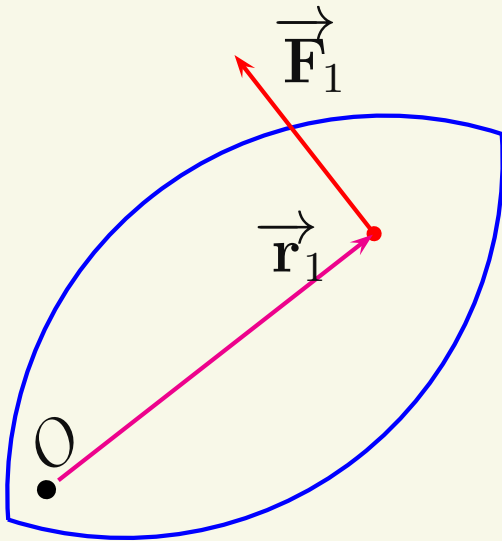
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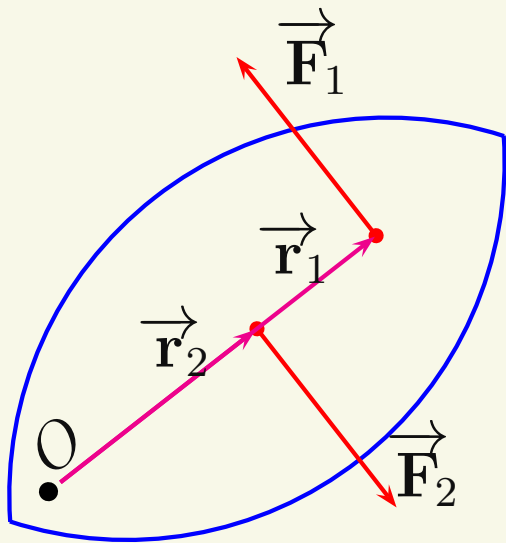


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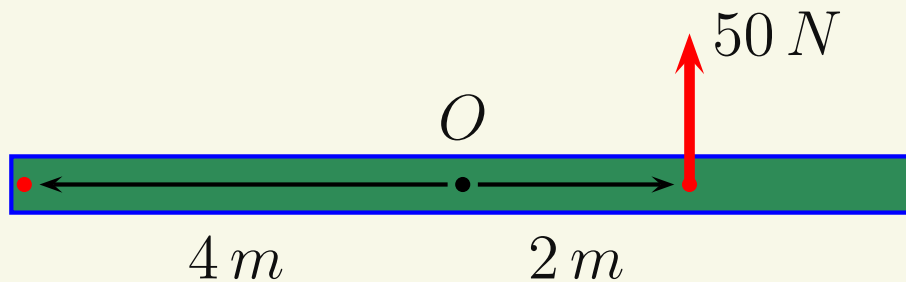


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 $\tau_2$  is negative

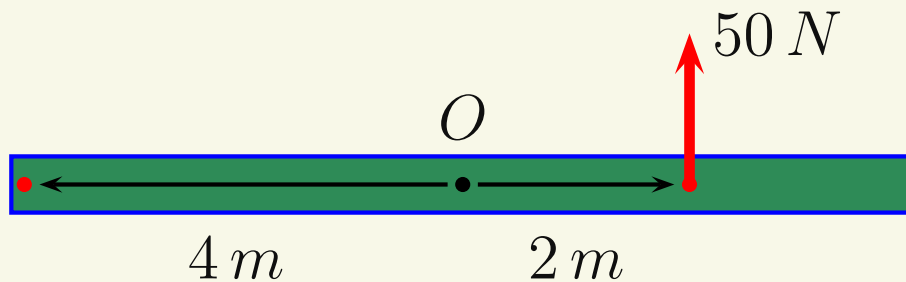
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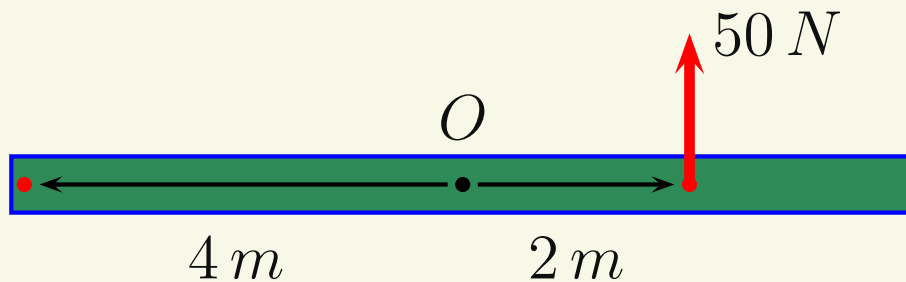


(a)  $25\text{ }N$ , up



## Torque Sign Exercise

An  $8\text{-m}$  long beam which can rotate about its center has an upwards  $50\text{-N}$  force applied  $2\text{ m}$  to the right of its center. What force, both magnitude and direction, must be applied  $4\text{ m}$  to the left of the center to make the net torque zero?

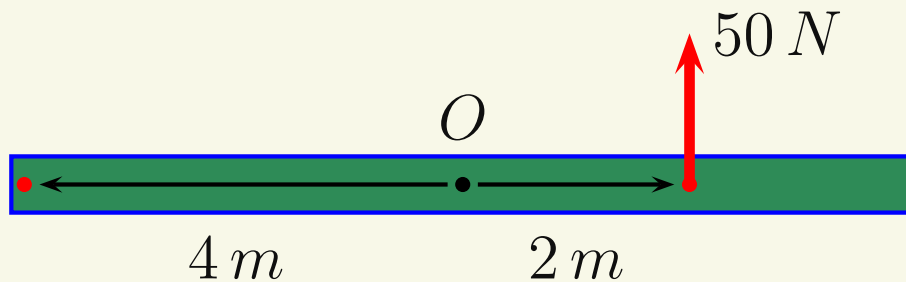


(a)  $25\text{ N}$ , up

(b)  $25\text{ N}$ , down

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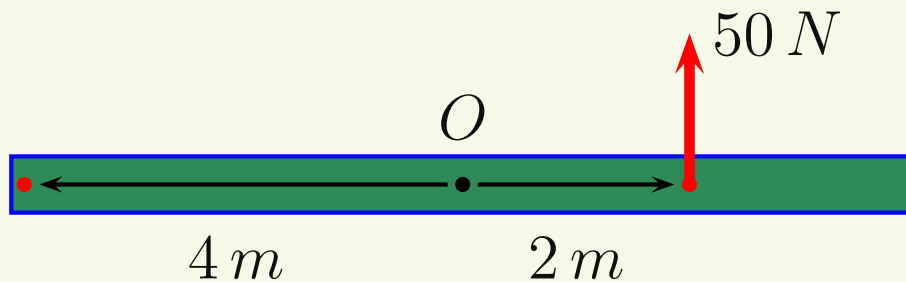
(a)  $25\text{ N}$ , up

(b)  $25\text{ N}$ , down

(c)  $50\text{ N}$ , up

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(a)  $25\text{ N}$ , up

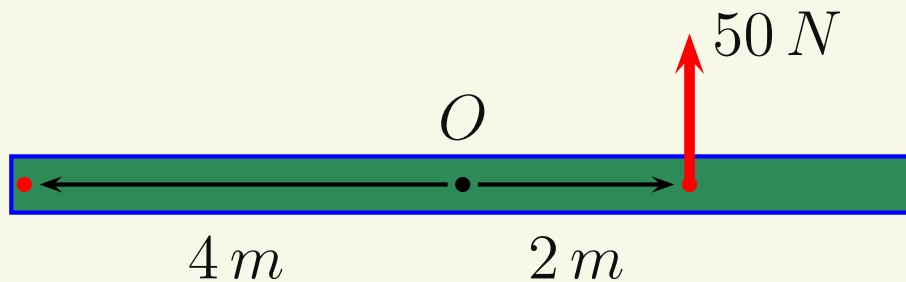
(b)  $25\text{ N}$ , down

(c)  $50\text{ N}$ , up

(d)  $100\text{ N}$ , up

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(a)  $25\text{ N}$ , up

(b)  $25\text{ N}$ , down

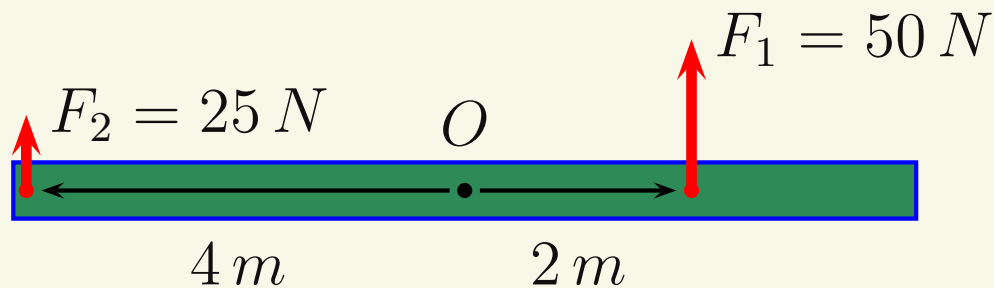
(c)  $50\text{ N}$ , up

(d)  $100\text{ N}$ , up

(e)  $100\text{ N}$ , down

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(a)  $25\text{ N}$ , up

(b)  $25\text{ N}$ , down

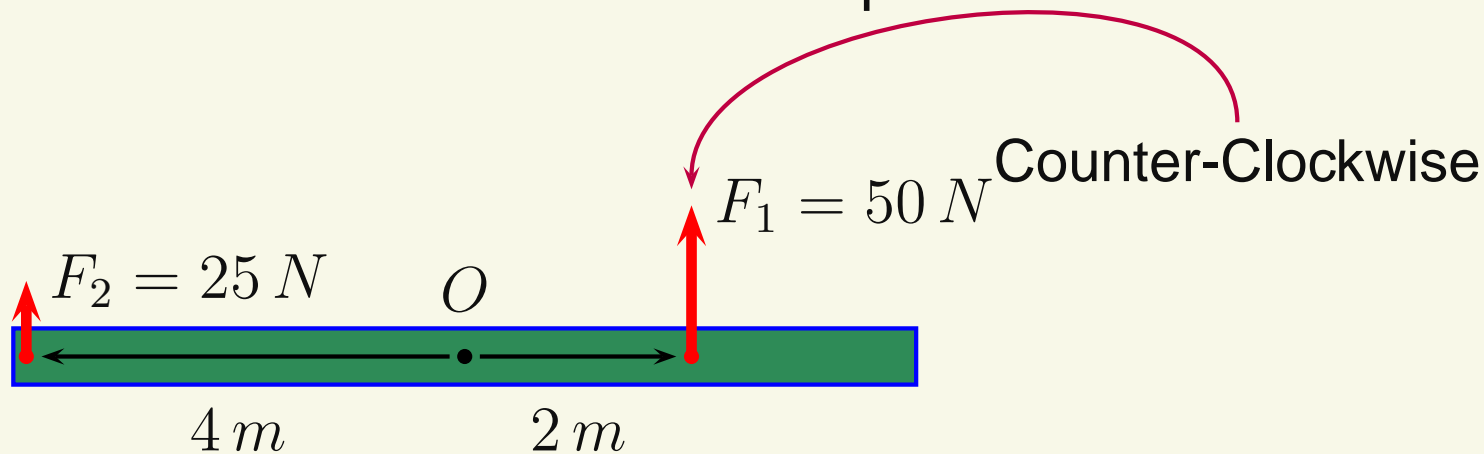
(c)  $50\text{ N}$ , up

(d)  $100\text{ N}$ , up

(e)  $100\text{ N}$ , down

## Torque Sign Exercise

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(a)  $25\text{ N}$ , up

(b)  $25\text{ N}$ , down

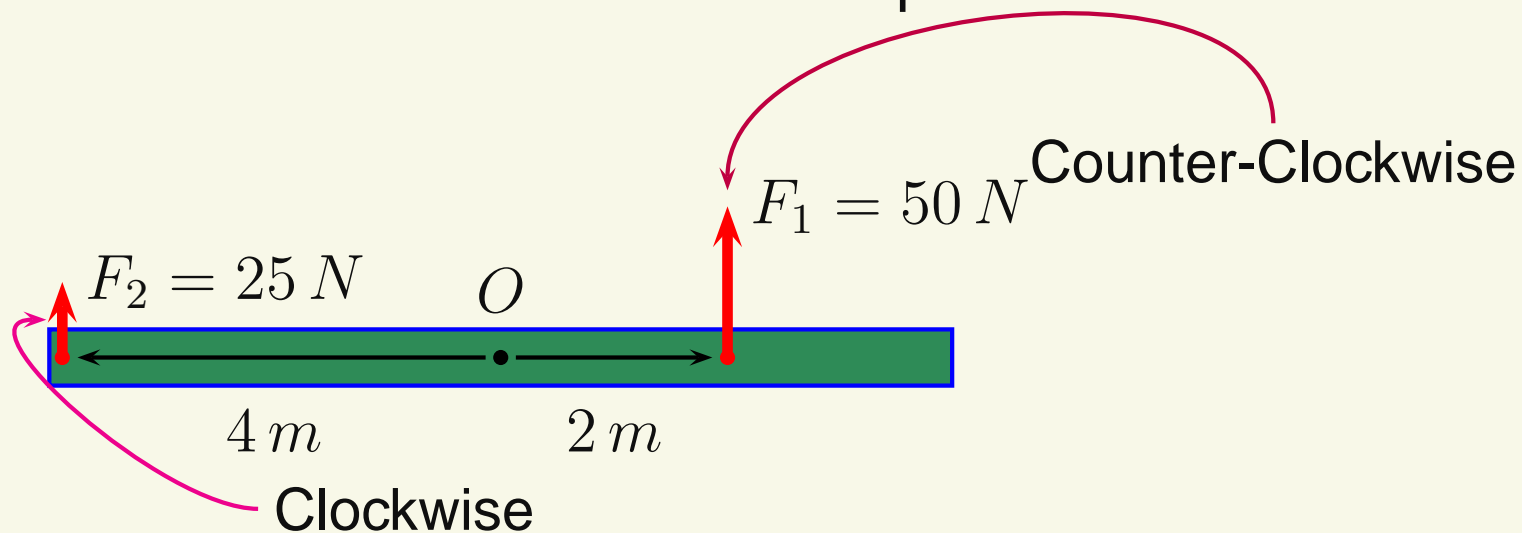
(c)  $50\text{ N}$ , up

(d)  $100\text{ N}$ , up

(e)  $100\text{ N}$ , down

## Torque Sign Exercise

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(a)  $25\text{ N}$ , up

(b)  $25\text{ N}$ , down

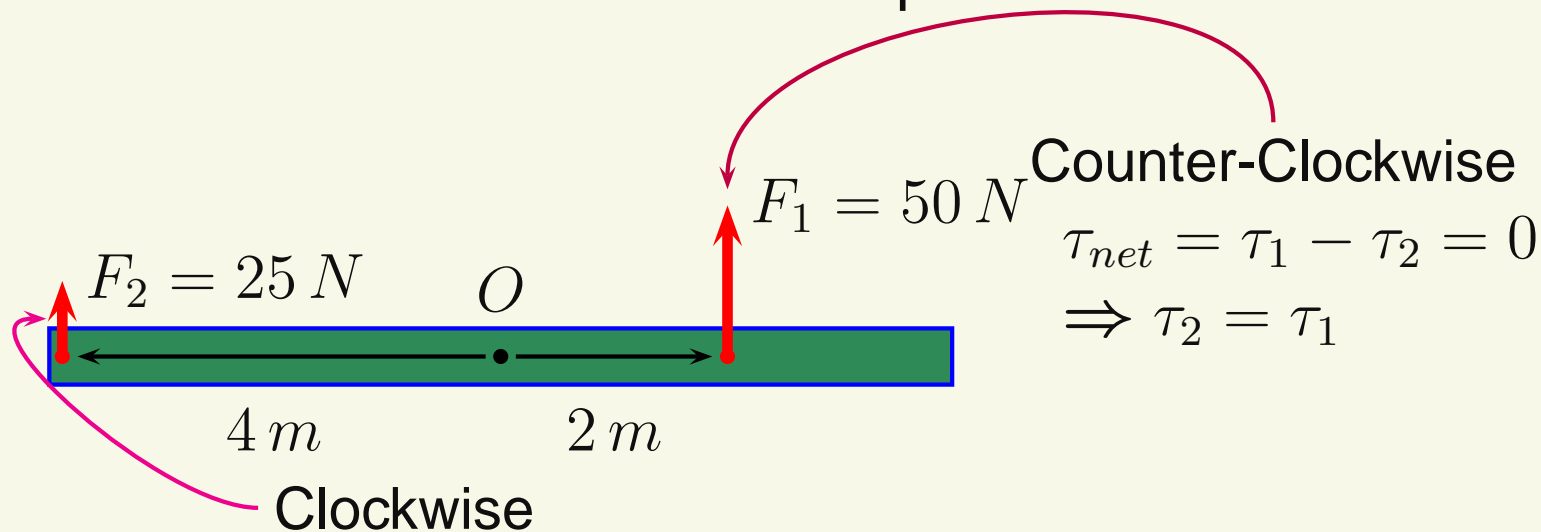
(c)  $50\text{ N}$ , up

(d)  $100\text{ N}$ , up

(e)  $100\text{ N}$ , down

## Torque Sign Exercise

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(a)  $25\text{ N}$ , up

(b)  $25\text{ N}$ , down

(c)  $50\text{ N}$ , up

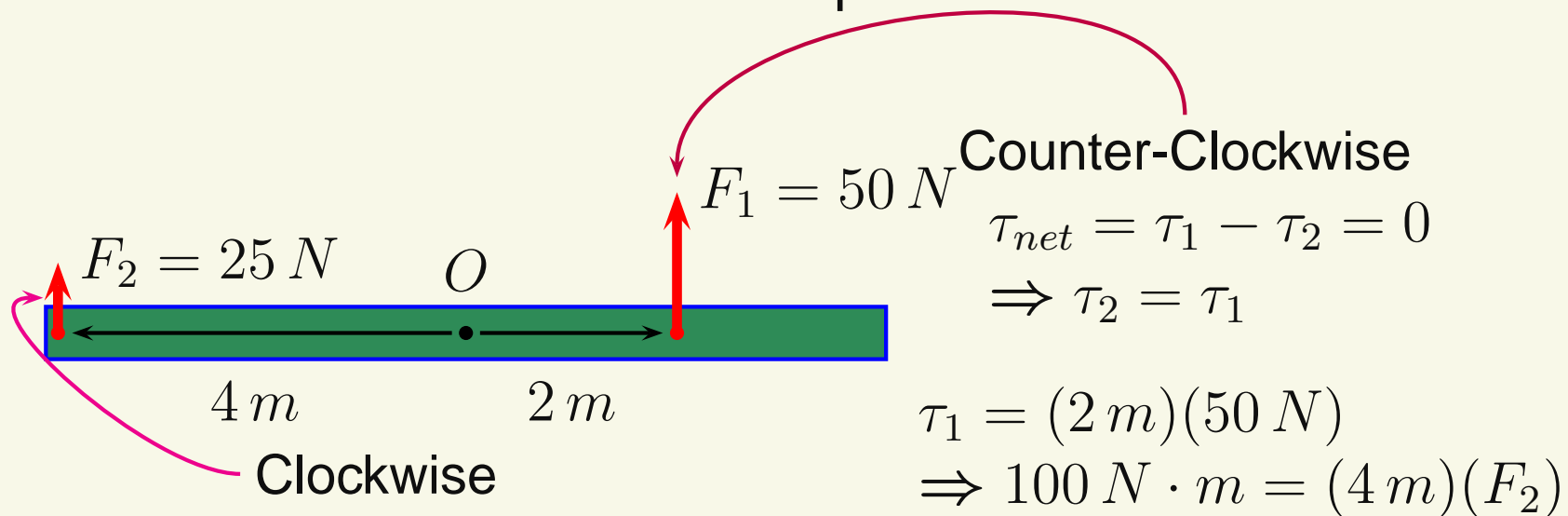
(d)  $100\text{ N}$ , up

(e)  $100\text{ N}$ , down



## Torque Sign Exercise

An  $8\text{-m}$  long beam which can rotate about its center has an upwards  $50\text{-N}$  force applied  $2\text{ m}$  to the right of its center. What force, both magnitude and direction, must be applied  $4\text{ m}$  to the left of the center to make the net torque zero?



(a)  $25\text{ N}$ , up

(b)  $25\text{ N}$ , down

(c)  $50\text{ N}$ , up

(d)  $100\text{ N}$ , up

(e)  $100\text{ N}$ , down