

July 1, Week 5

Today: Finish Chapter 6 and start Chapter 9

Homework Assignment #5 - Due Monday, July 7 at 5:00PM.

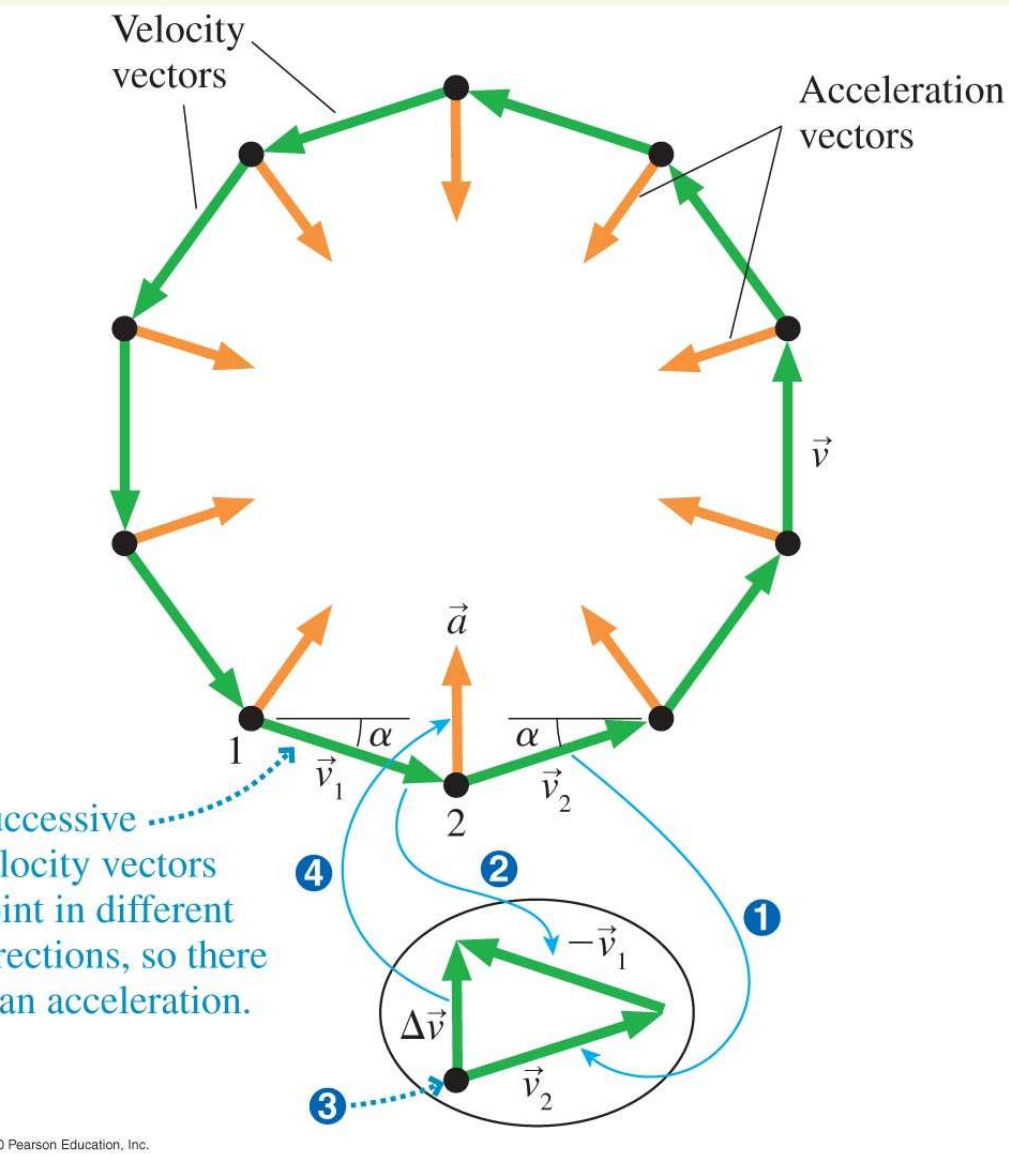
No office hours on Friday.

Circular Dynamics

Objects in circular motion must have an inwards acceleration in order to change direction.

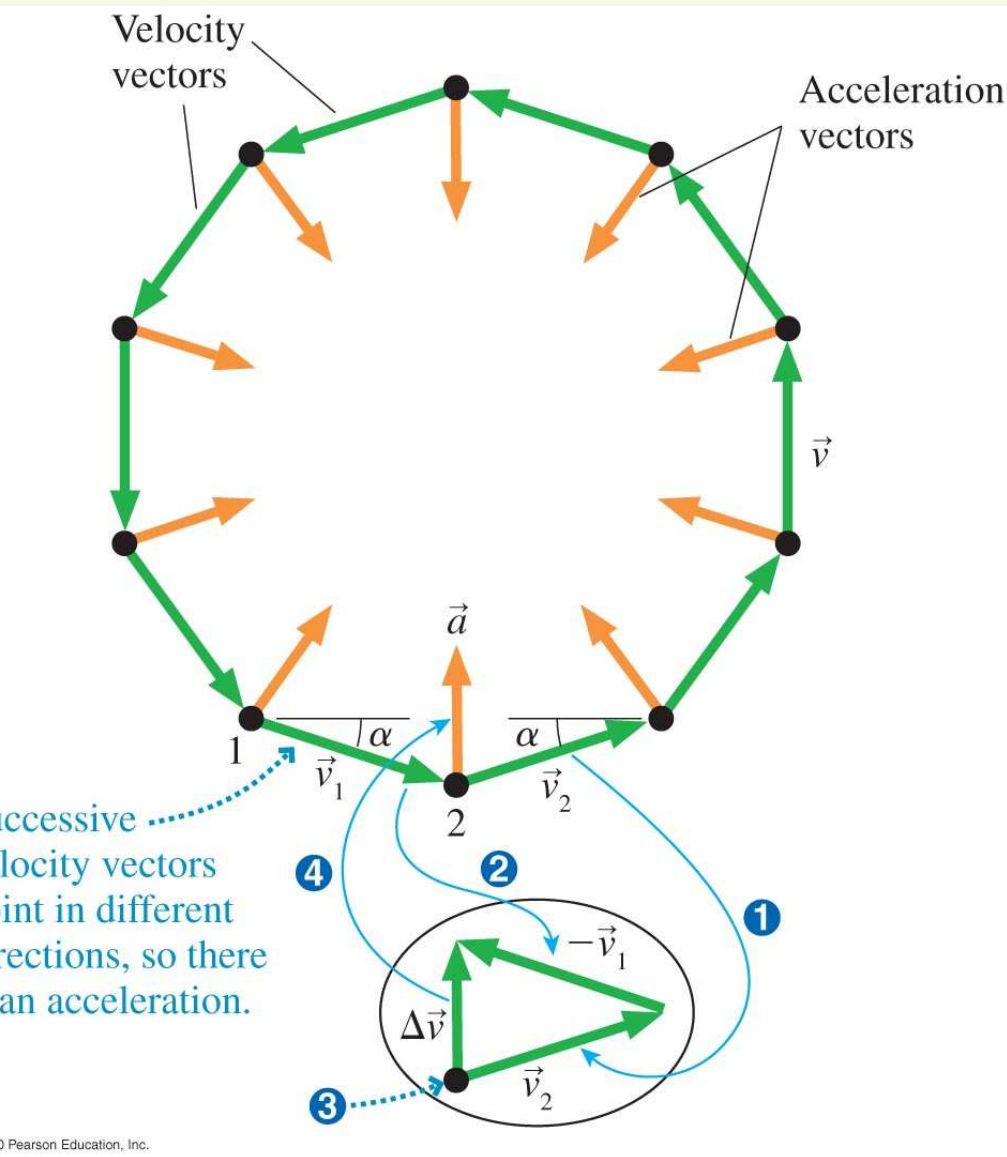
Circular Dynamics

Objects in circular motion must have an inwards acceleration in order to change direction.



Circular Dynamics

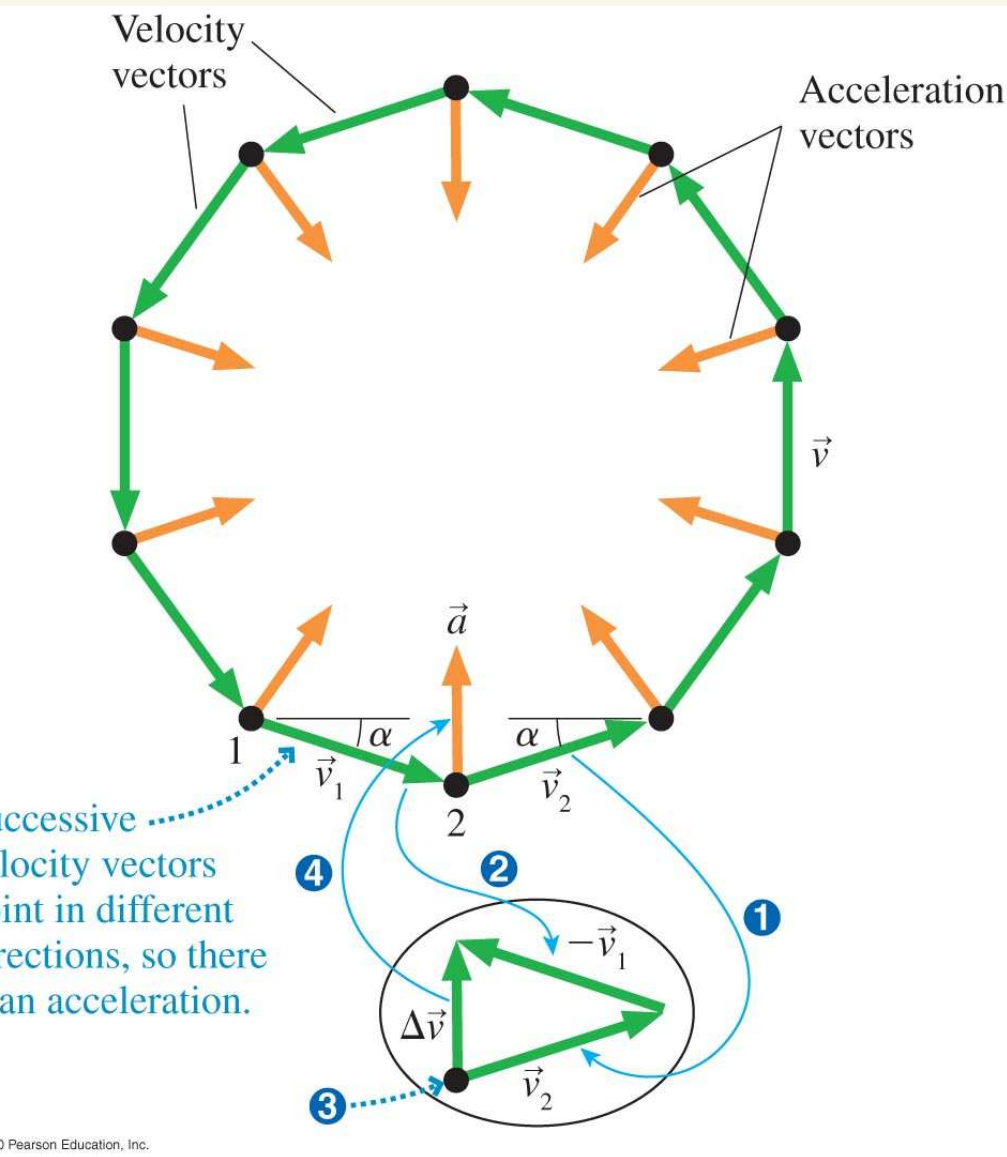
Objects in circular motion must have an inwards acceleration in order to change direction.



The Centripetal Acceleration -
The acceleration towards the center necessary for circular motion

Circular Dynamics

Objects in circular motion must have an inwards acceleration in order to change direction.



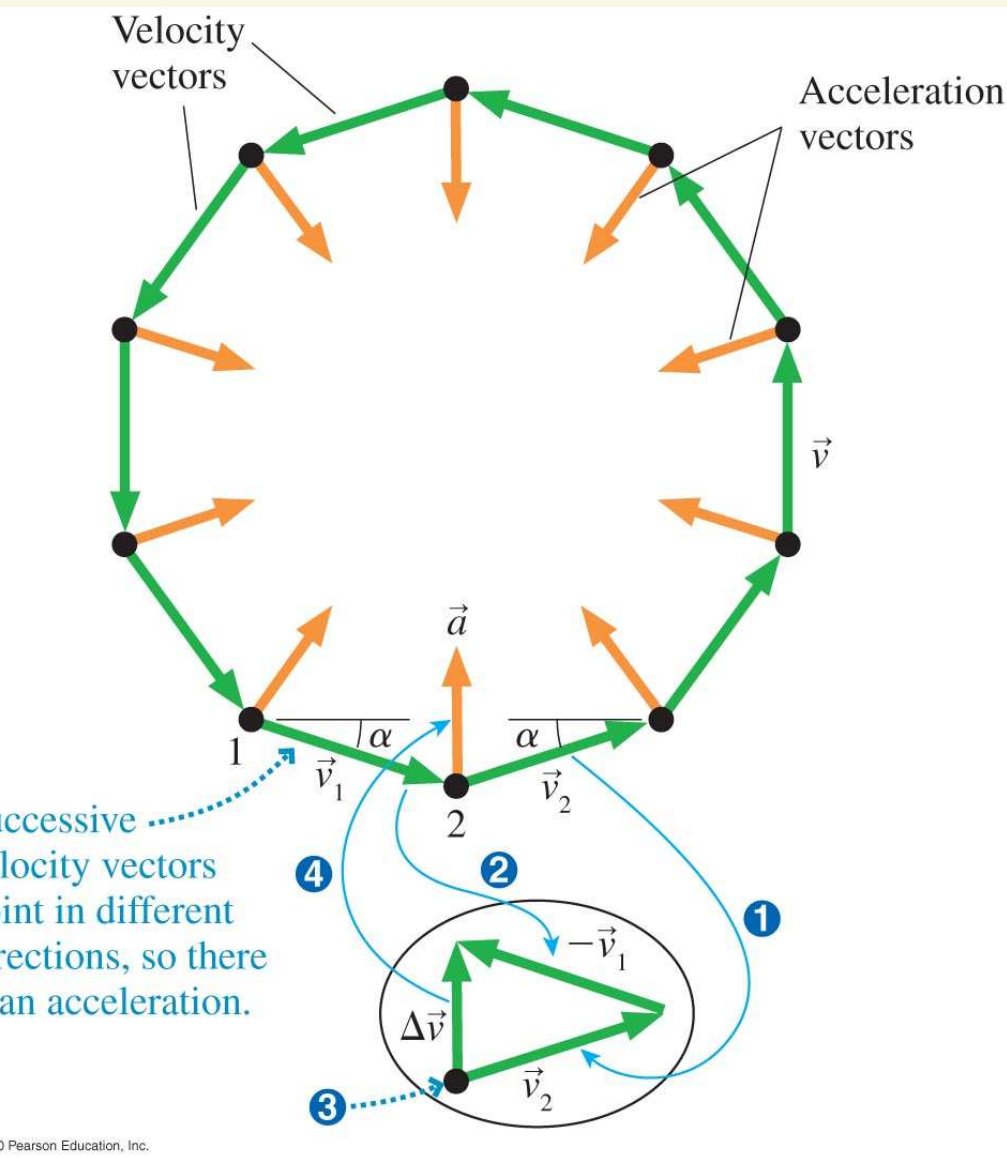
The Centripetal Acceleration -
The acceleration towards the center necessary for circular motion

$$a = \frac{v^2}{r} = \omega^2 r$$

Section 3.8

Circular Dynamics

Objects in circular motion must have an inwards acceleration in order to change direction.



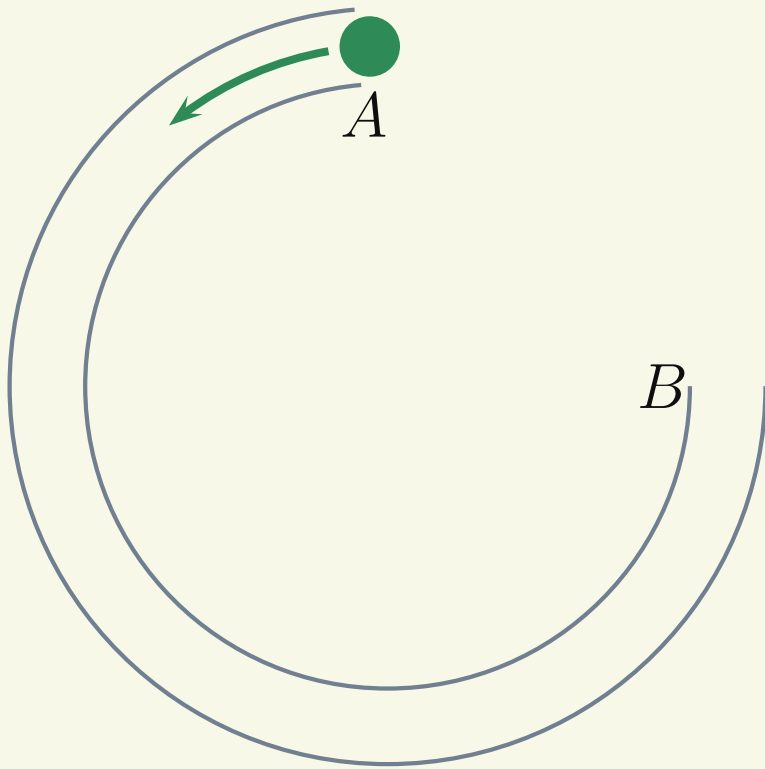
The Centripetal Acceleration -
The acceleration towards the
center necessary for circular
motion

$$a = \frac{v^2}{r} = \omega^2 r \quad \text{Section 3.8}$$

The centripetal acceleration like any other is **NOT** put on free-body diagrams. It is created by other forces like weight, tension, normal, *etc.*

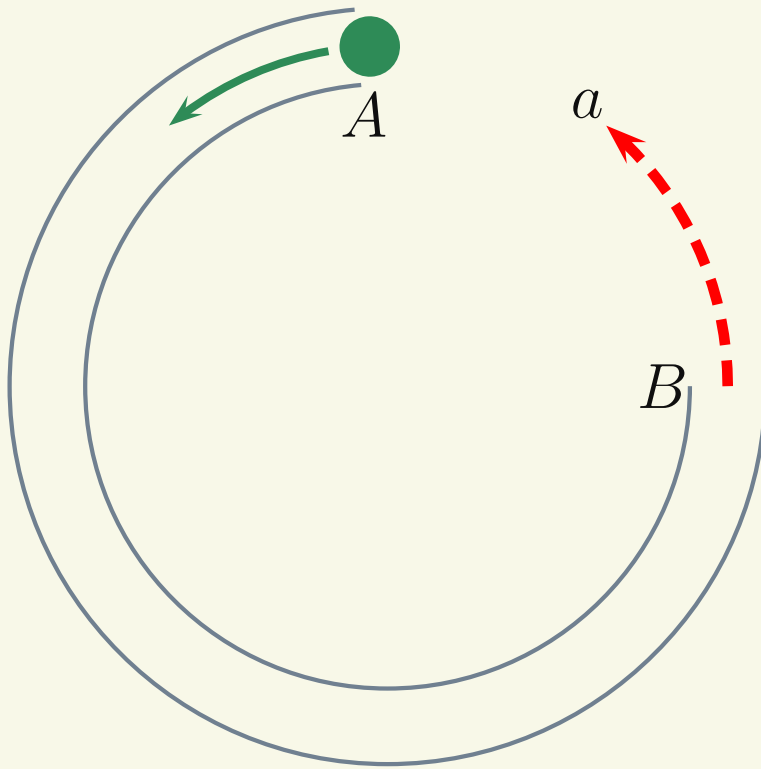
Centripetal-Acceleration Exercise

The figure shows a *top view* of a plastic tube that is fixed on a horizontal table top. A marble is shot into the tube at A . Which of the following is the correct trajectory for the marble after it leaves the tube at B ?



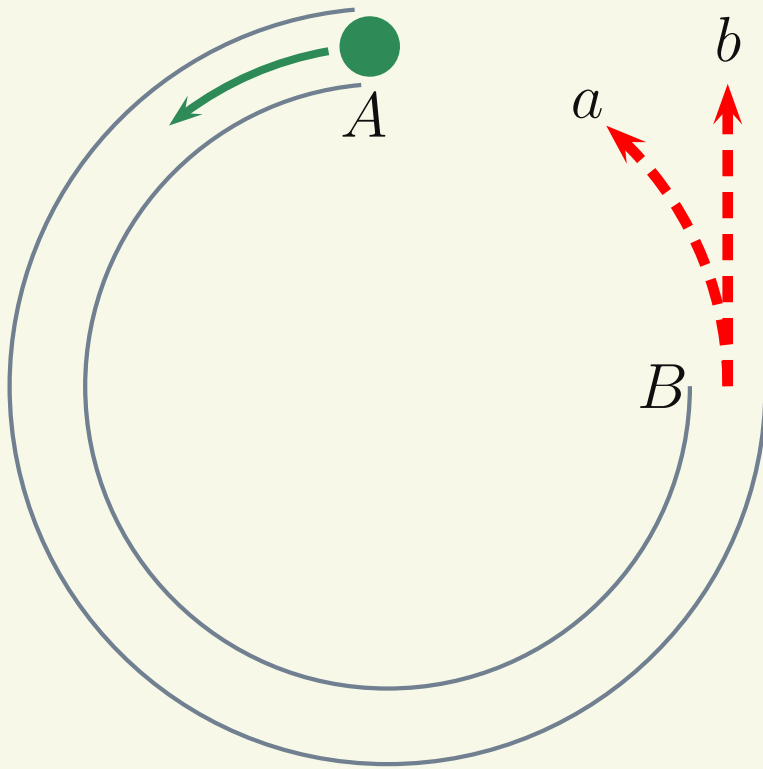
Centripetal-Acceleration Exercise

The figure shows a *top view* of a plastic tube that is fixed on a horizontal table top. A marble is shot into the tube at A . Which of the following is the correct trajectory for the marble after it leaves the tube at B ?



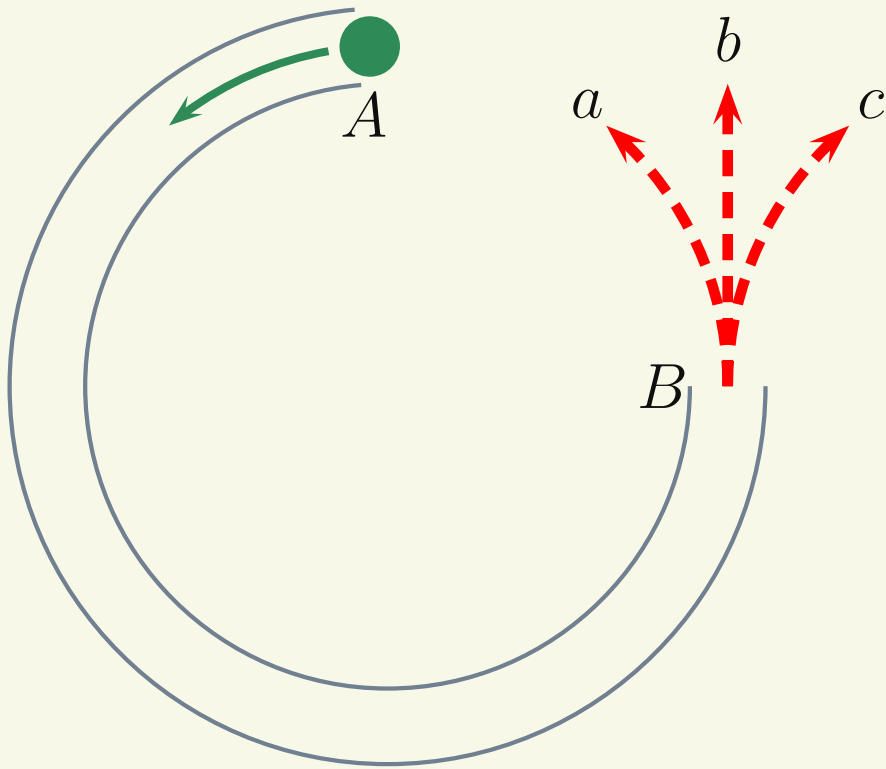
Centripetal-Acceleration Exercise

The figure shows a *top view* of a plastic tube that is fixed on a horizontal table top. A marble is shot into the tube at A . Which of the following is the correct trajectory for the marble after it leaves the tube at B ?



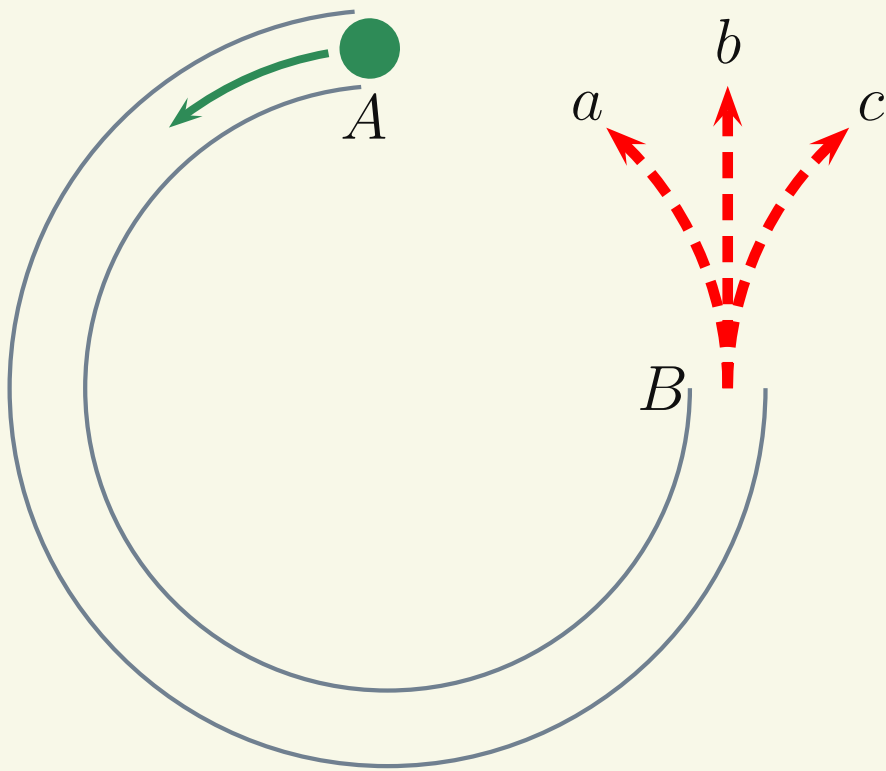
Centripetal-Acceleration Exercise

The figure shows a *top view* of a plastic tube that is fixed on a horizontal table top. A marble is shot into the tube at A . Which of the following is the correct trajectory for the marble after it leaves the tube at B ?



Centripetal-Acceleration Exercise

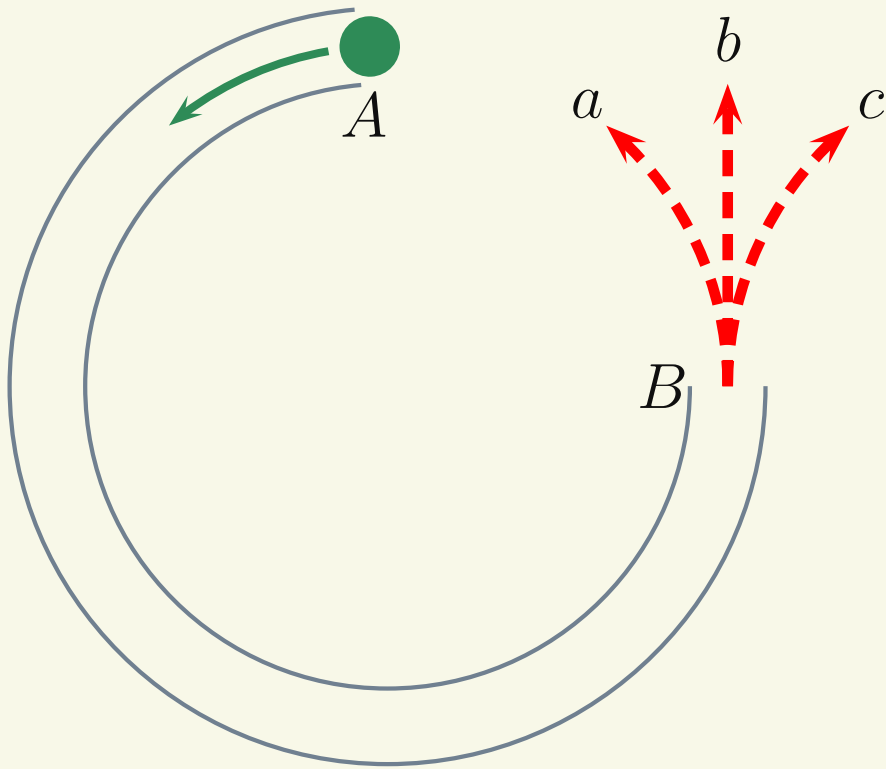
The figure shows a *top view* of a plastic tube that is fixed on a horizontal table top. A marble is shot into the tube at A . Which of the following is the correct trajectory for the marble after it leaves the tube at B ?



(d) Any of these are possible.

Centripetal-Acceleration Exercise

The figure shows a *top view* of a plastic tube that is fixed on a horizontal table top. A marble is shot into the tube at A . Which of the following is the correct trajectory for the marble after it leaves the tube at B ?

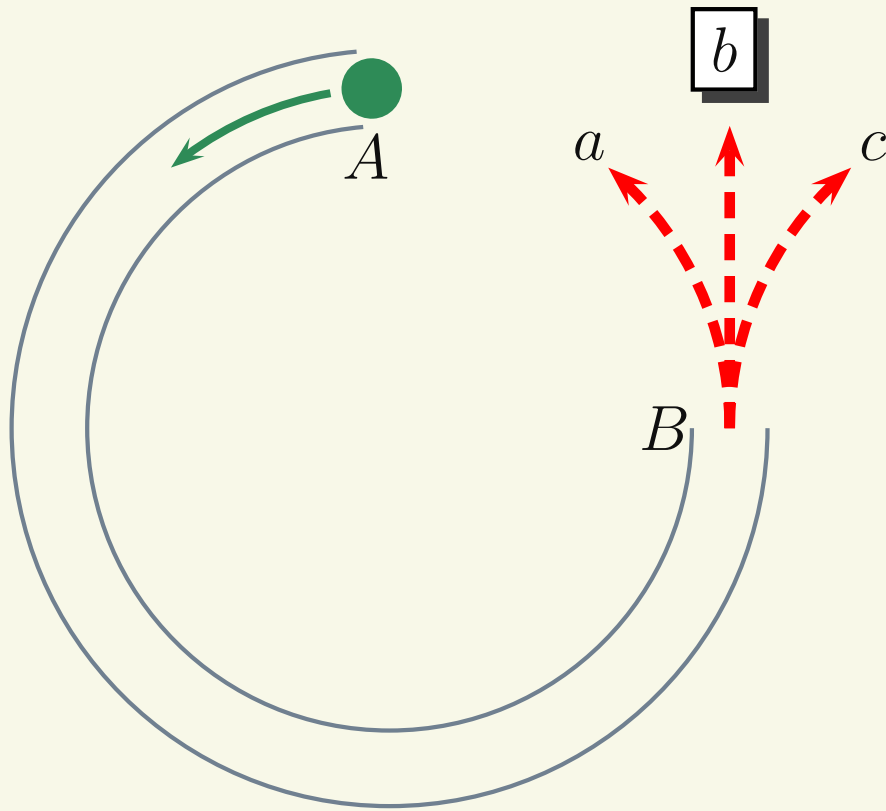


(d) Any of these are possible.

(e) None of these are possible.

Centripetal-Acceleration Exercise

The figure shows a *top view* of a plastic tube that is fixed on a horizontal table top. A marble is shot into the tube at A . Which of the following is the correct trajectory for the marble after it leaves the tube at B ?

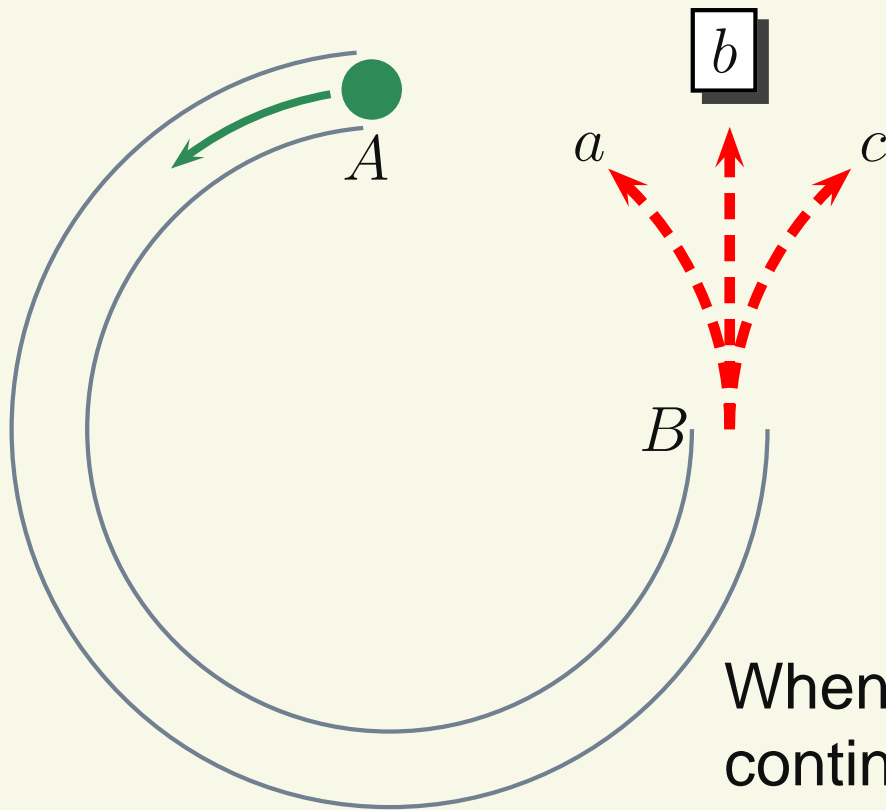


(d) Any of these are possible.

(e) None of these are possible.

Centripetal-Acceleration Exercise

The figure shows a *top view* of a plastic tube that is fixed on a horizontal table top. A marble is shot into the tube at *A*. Which of the following is the correct trajectory for the marble after it leaves the tube at *B*?



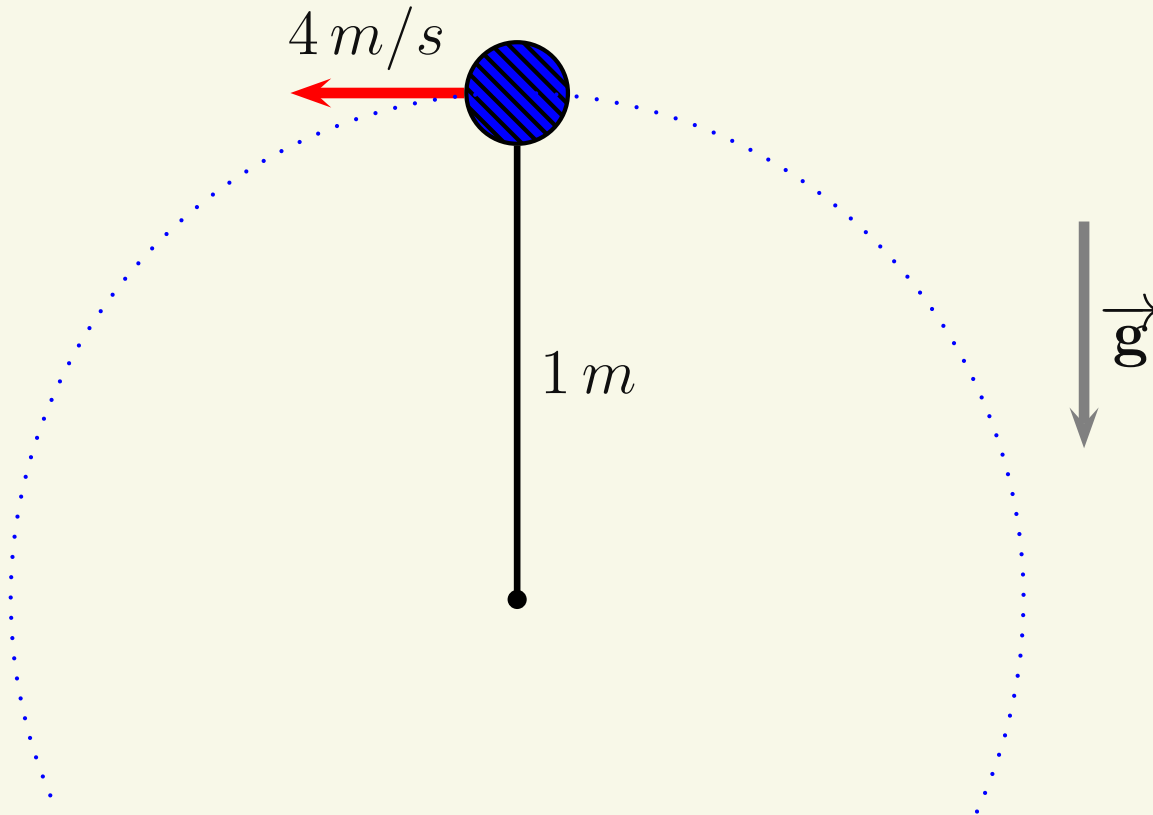
(d) Any of these are possible.

(e) None of these are possible.

When the centripetal force ends, an object continues in the direction of its velocity

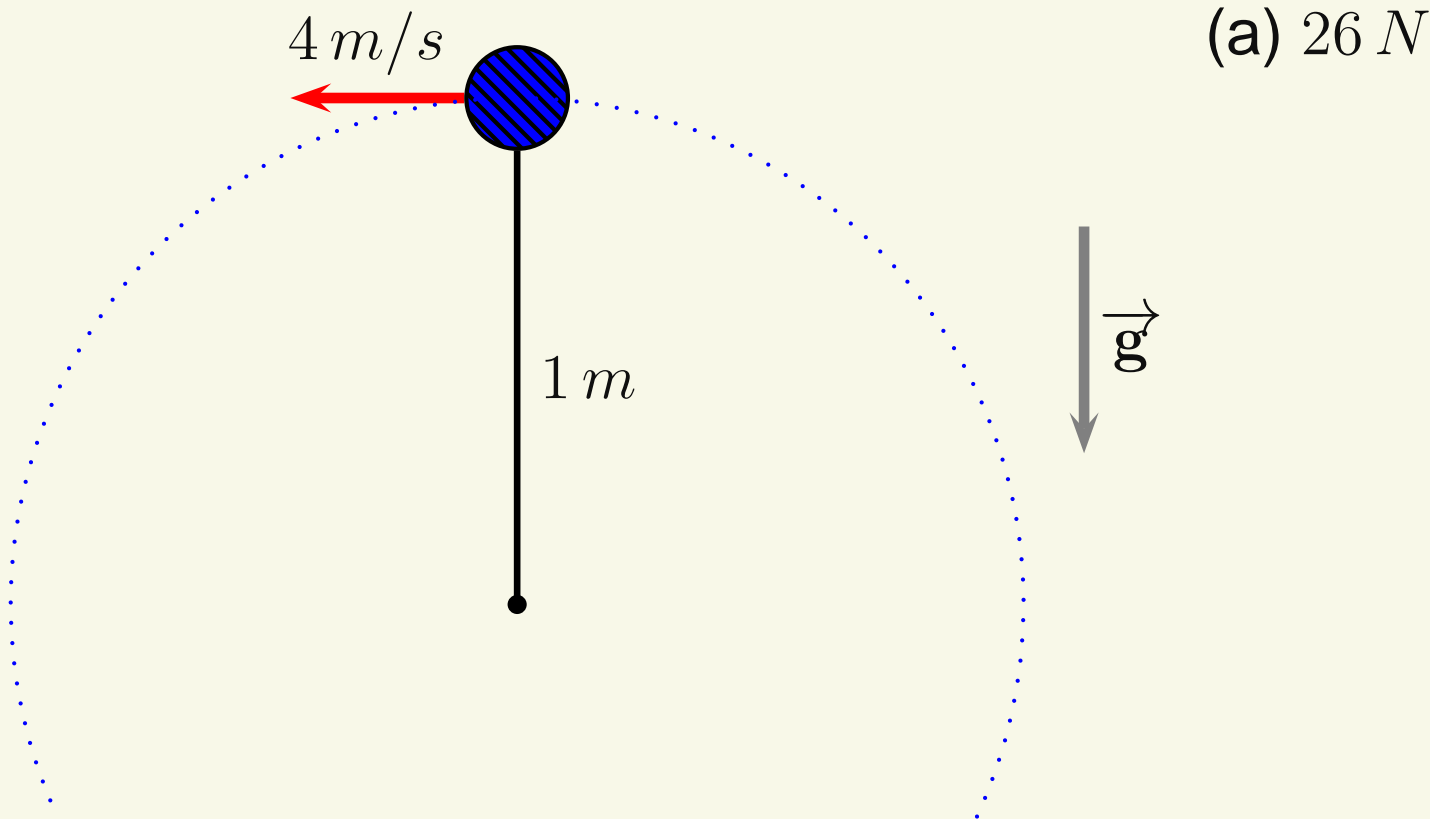
Calculation Exercise

A 10-N ball, attached to a massless string, is swung in a vertical circle of radius 1 m . If at the top of the circle the ball's speed is 4 m/s , what is tension in the string? For ease of calculation assume $g = 10\text{ m/s}^2$ so that $m = 1\text{ kg}$.



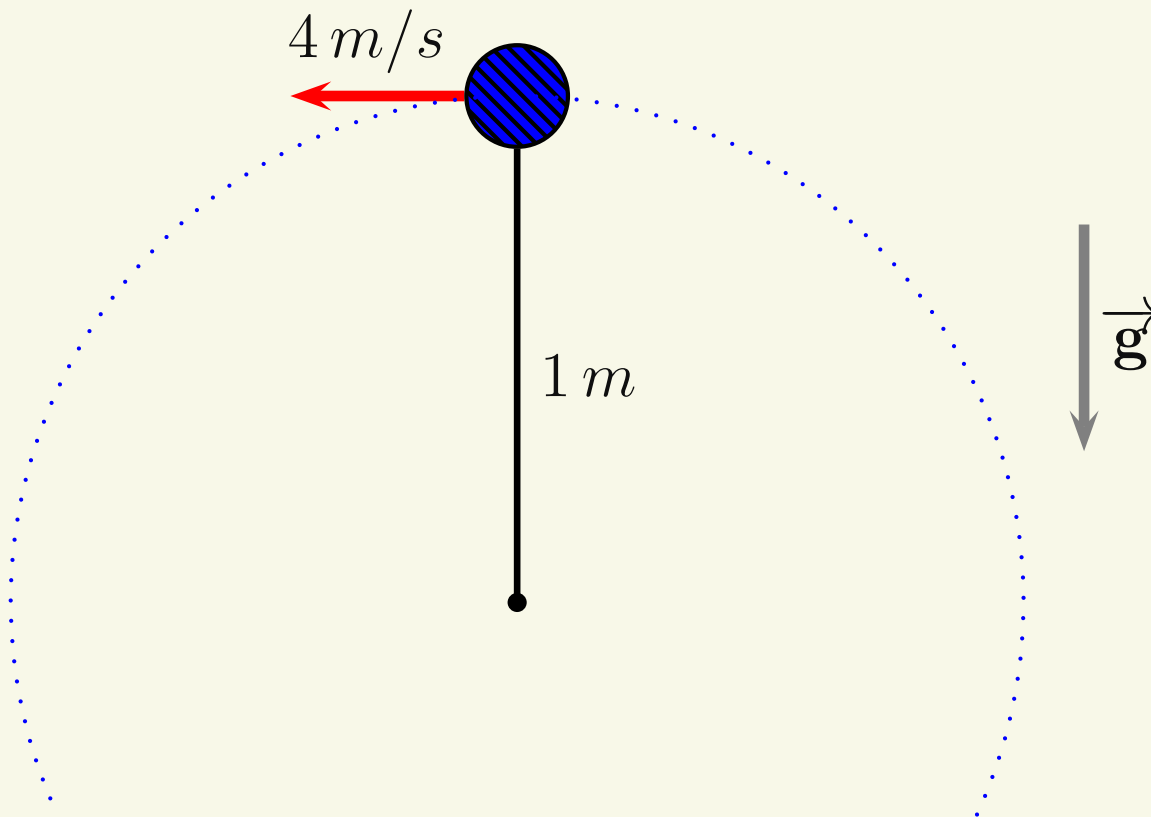
Calculation Exercise

A $10\text{-}N$ ball, attached to a massless string, is swung in a vertical circle of radius 1 m . If at the top of the circle the ball's speed is 4 m/s , what is tension in the string? For ease of calculation assume $g = 10\text{ m/s}^2$ so that $m = 1\text{ kg}$.



Calculation Exercise

A $10\text{-}N$ ball, attached to a massless string, is swung in a vertical circle of radius 1 m . If at the top of the circle the ball's speed is 4 m/s , what is tension in the string? For ease of calculation assume $g = 10\text{ m/s}^2$ so that $m = 1\text{ kg}$.

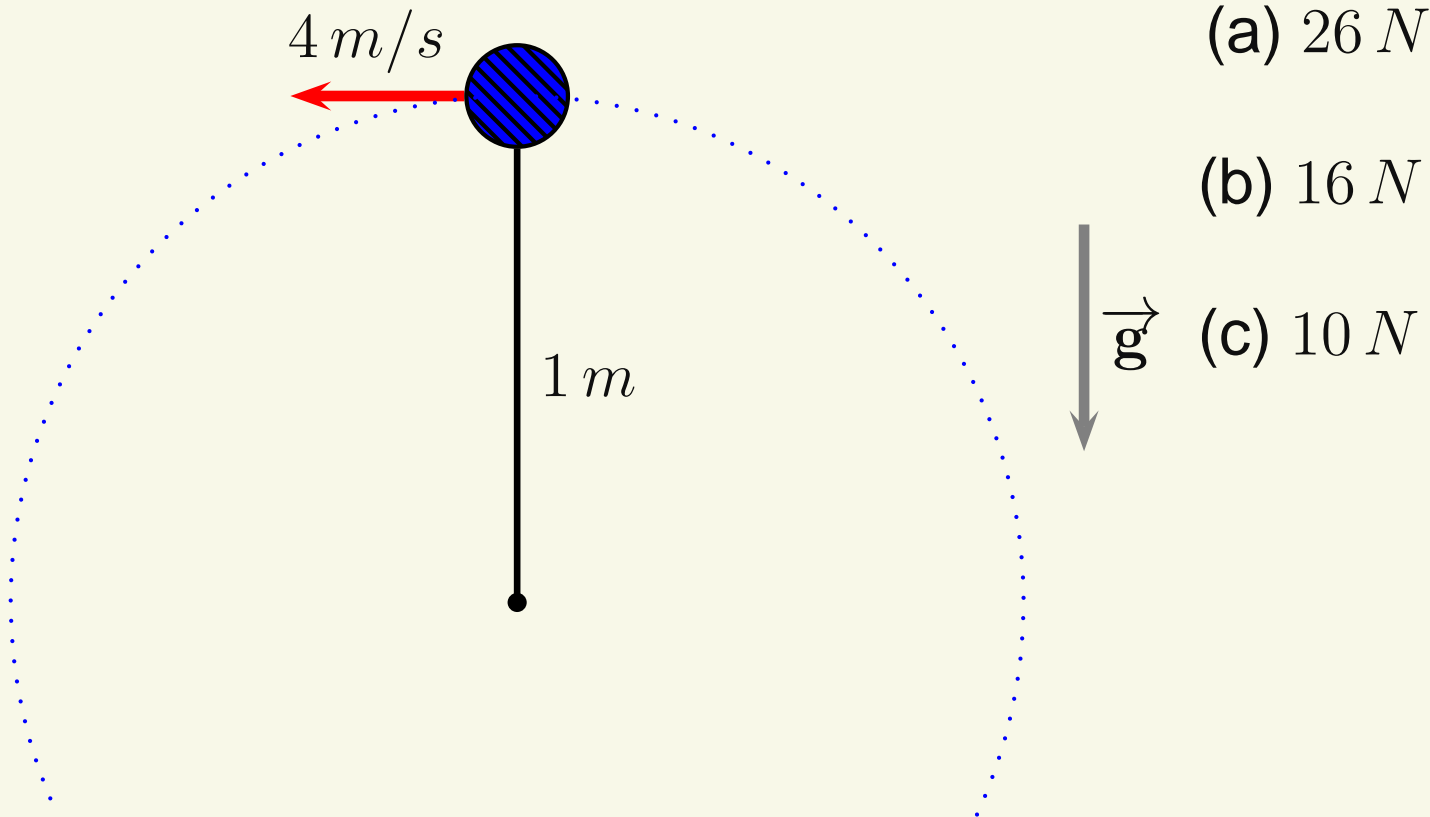


(a) 26 N

(b) 16 N

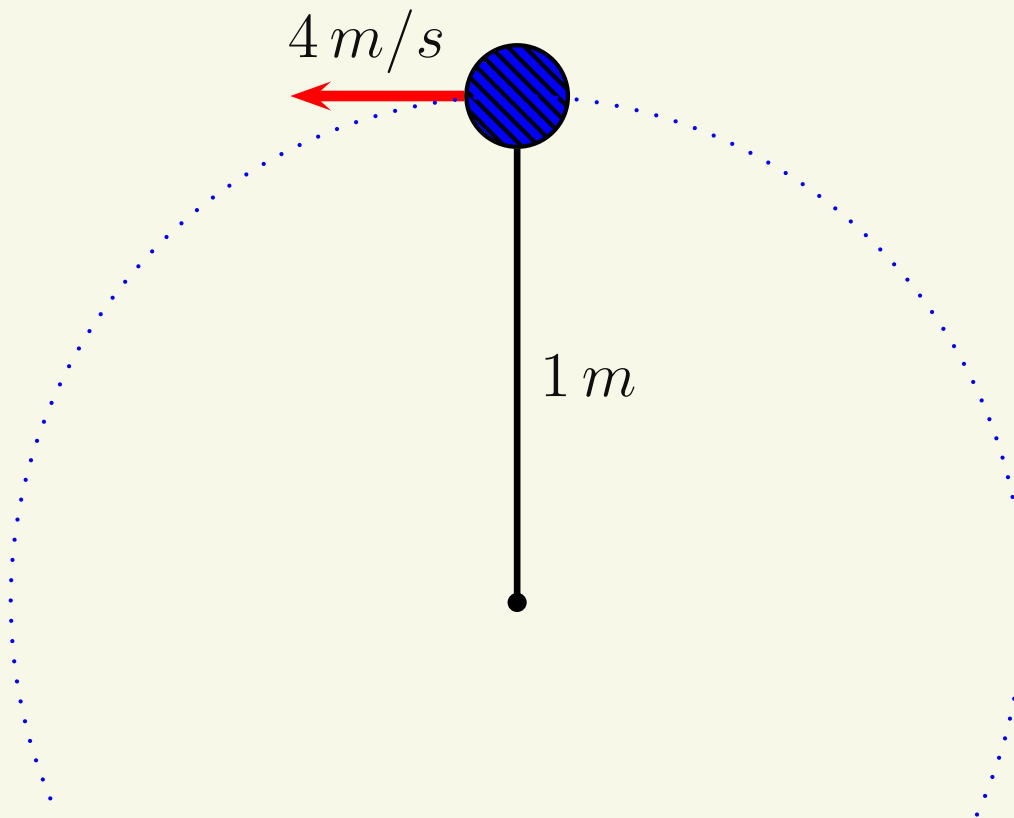
Calculation Exercise

A $10\text{-}N$ ball, attached to a massless string, is swung in a vertical circle of radius 1 m . If at the top of the circle the ball's speed is 4 m/s , what is tension in the string? For ease of calculation assume $g = 10\text{ m/s}^2$ so that $m = 1\text{ kg}$.



Calculation Exercise

A $10\text{-}N$ ball, attached to a massless string, is swung in a vertical circle of radius 1 m . If at the top of the circle the ball's speed is 4 m/s , what is tension in the string? For ease of calculation assume $g = 10\text{ m/s}^2$ so that $m = 1\text{ kg}$.



(a) 26 N

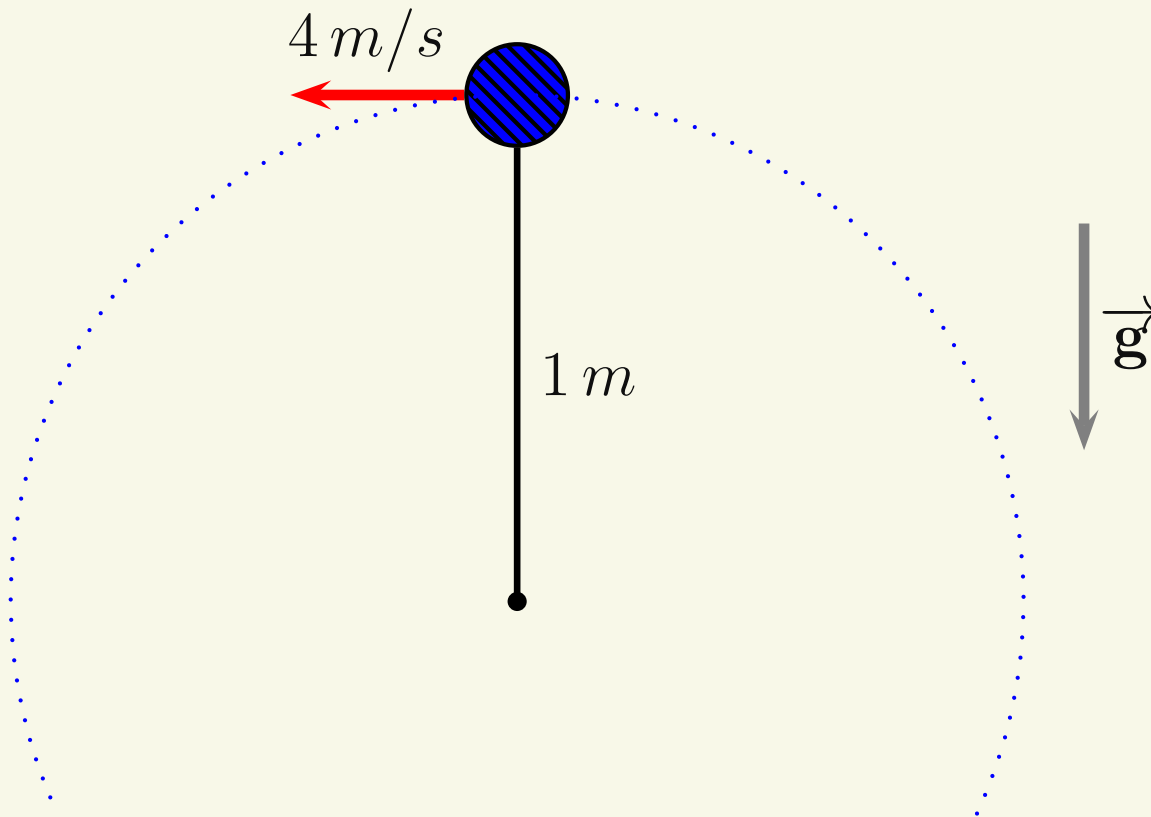
(b) 16 N

(c) 10 N

(d) 6 N

Calculation Exercise

A $10\text{-}N$ ball, attached to a massless string, is swung in a vertical circle of radius 1 m . If at the top of the circle the ball's speed is 4 m/s , what is tension in the string? For ease of calculation assume $g = 10\text{ m/s}^2$ so that $m = 1\text{ kg}$.



(a) 26 N

(b) 16 N

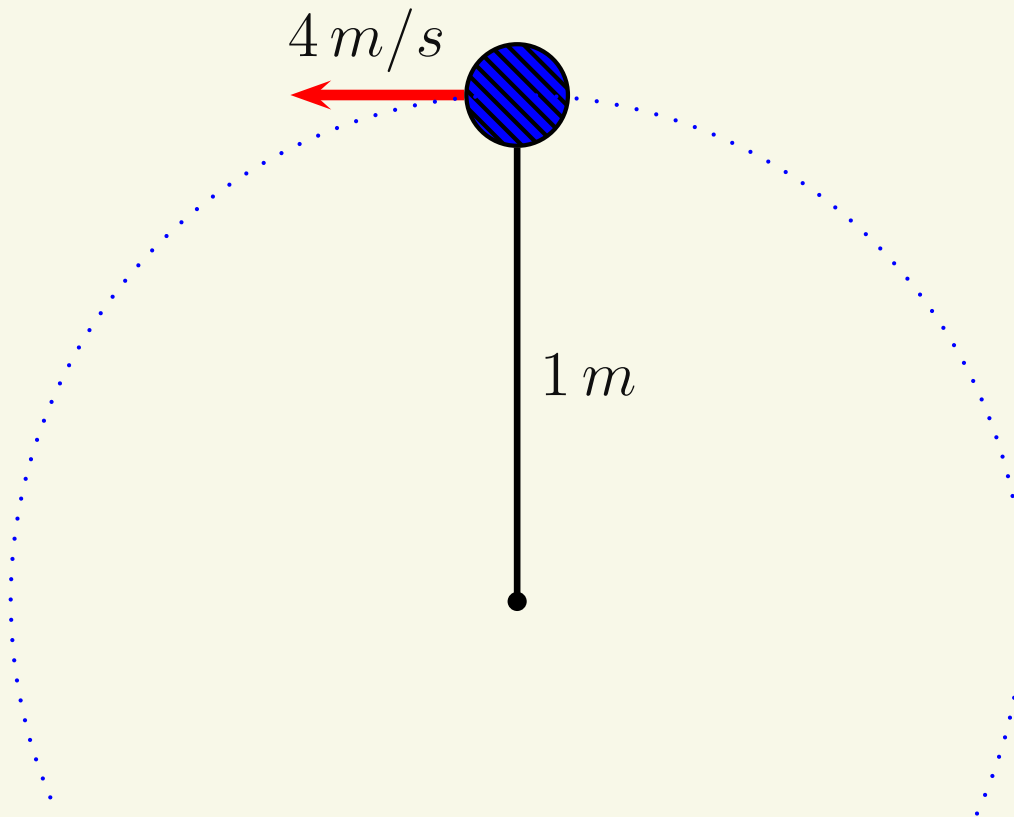
(c) 10 N

(d) 6 N

(e) 0 N

Calculation Exercise

A 10-N ball, attached to a massless string, is swung in a vertical circle of radius 1 m . If at the top of the circle the ball's speed is 4 m/s , what is tension in the string? For ease of calculation assume $g = 10\text{ m/s}^2$ so that $m = 1\text{ kg}$.



(a) 26 N

(b) 16 N

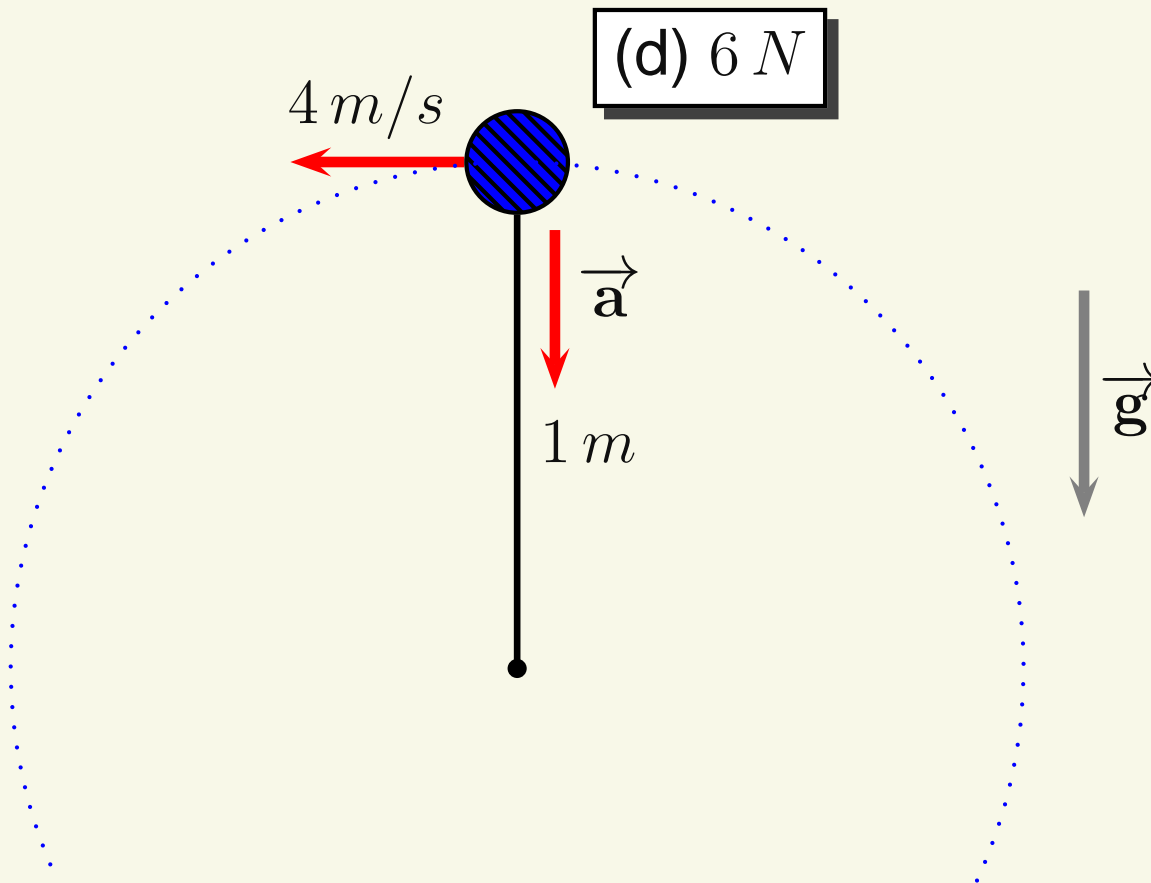
(c) 10 N

(d) 6 N

(e) 0 N

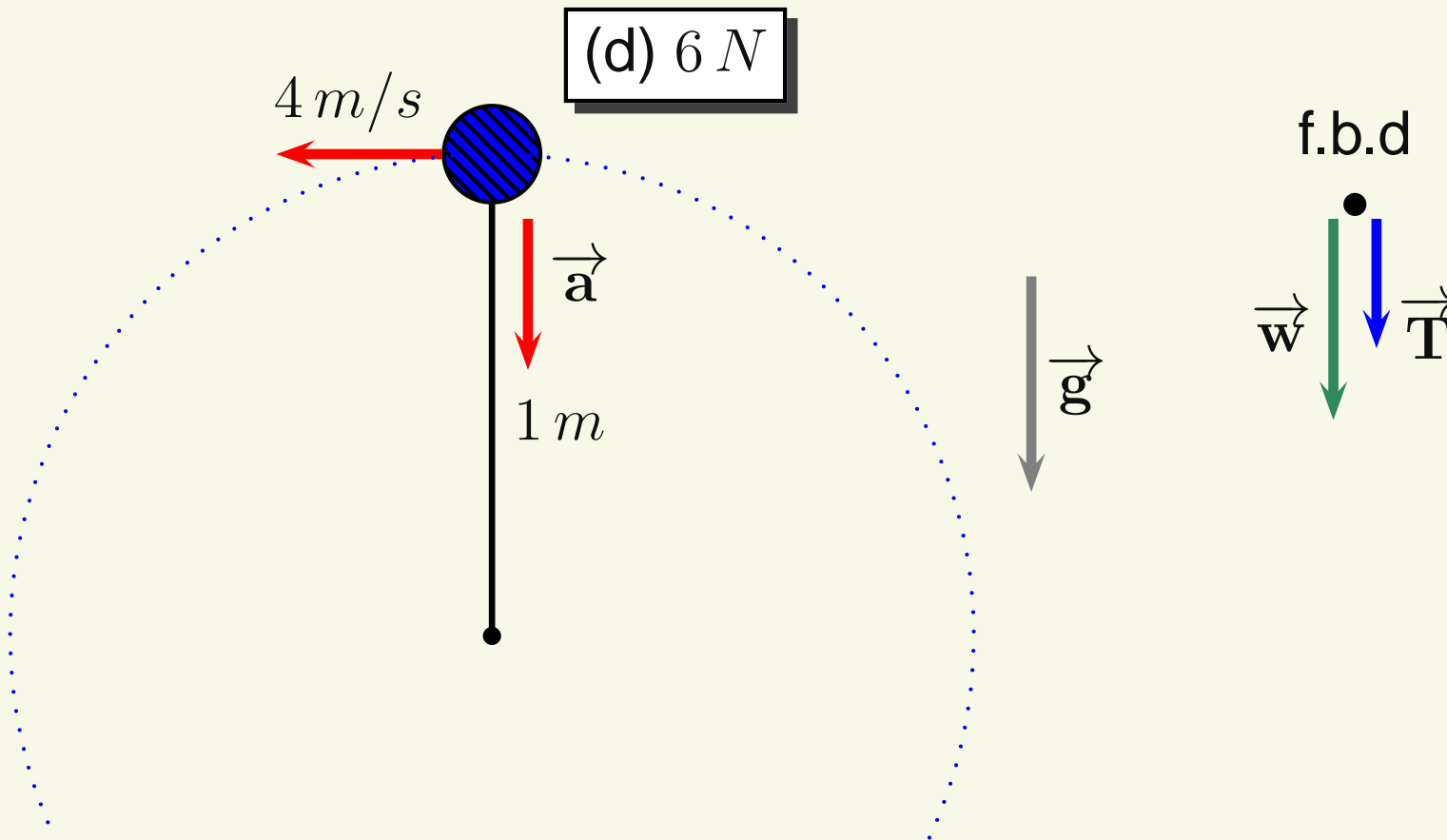
Calculation Exercise

A $10\text{-}N$ ball, attached to a massless string, is swung in a vertical circle of radius 1 m . If at the top of the circle the ball's speed is 4 m/s , what is tension in the string? For ease of calculation assume $g = 10\text{ m/s}^2$ so that $m = 1\text{ kg}$.



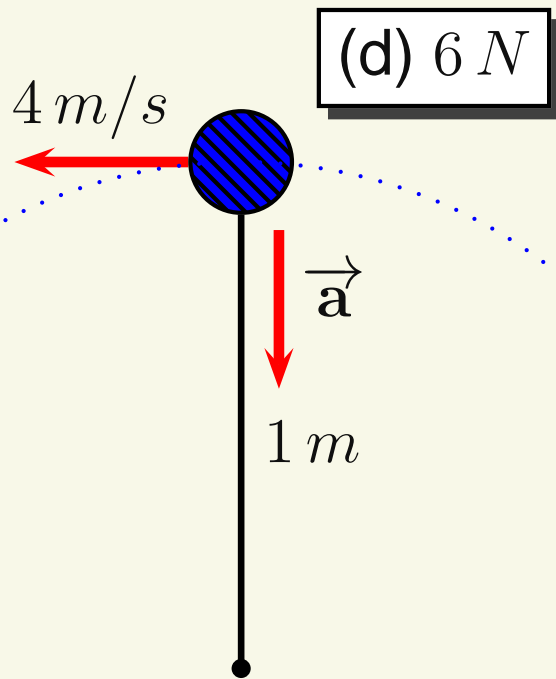
Calculation Exercise

A 10-N ball, attached to a massless string, is swung in a vertical circle of radius 1 m . If at the top of the circle the ball's speed is 4 m/s , what is tension in the string? For ease of calculation assume $g = 10\text{ m/s}^2$ so that $m = 1\text{ kg}$.



Calculation Exercise

A 10-N ball, attached to a massless string, is swung in a vertical circle of radius 1 m . If at the top of the circle the ball's speed is 4 m/s , what is tension in the string? For ease of calculation assume $g = 10\text{ m/s}^2$ so that $m = 1\text{ kg}$.



f.b.d

The free body diagram shows a black dot representing the ball. Two downward arrows originate from the dot: a green arrow labeled \vec{w} (weight) and a blue arrow labeled \vec{T} (tension). To the left of the diagram is a grey arrow pointing downwards labeled g .

$$\begin{aligned}\sum F_y &= ma_y \Rightarrow \\ T_y + w_y &= ma_y \Rightarrow \\ -T - w &= m(-v^2/r) \Rightarrow \\ -T - 10\text{ N} &= -(1\text{ kg})(16\text{ m/s}^2)\end{aligned}$$

Momentum

We can rewrite Newton's Second law in a slightly different way:

$$\sum \vec{\mathbf{F}} = m \vec{\mathbf{a}}$$

Momentum

We can rewrite Newton's Second law in a slightly different way:

$$\sum \vec{\mathbf{F}} = m \vec{\mathbf{a}} \Rightarrow \vec{\mathbf{F}}_{av} = m \vec{\mathbf{a}}_{av}$$

Momentum

We can rewrite Newton's Second law in a slightly different way:

$$\sum \vec{\mathbf{F}} = m \vec{\mathbf{a}} \Rightarrow \vec{\mathbf{F}}_{av} = m \vec{\mathbf{a}}_{av}$$

$$m \vec{\mathbf{a}}_{av}$$

Momentum

We can rewrite Newton's Second law in a slightly different way:

$$\sum \vec{\mathbf{F}} = m \vec{\mathbf{a}} \Rightarrow \vec{\mathbf{F}}_{av} = m \vec{\mathbf{a}}_{av}$$

$$m \vec{\mathbf{a}}_{av} = m \left(\frac{\Delta \vec{\mathbf{v}}}{\Delta t} \right)$$

Momentum

We can rewrite Newton's Second law in a slightly different way:

$$\sum \vec{\mathbf{F}} = m \vec{\mathbf{a}} \Rightarrow \vec{\mathbf{F}}_{av} = m \vec{\mathbf{a}}_{av}$$

$$m \vec{\mathbf{a}}_{av} = m \left(\frac{\Delta \vec{\mathbf{v}}}{\Delta t} \right) = m \left(\frac{\vec{\mathbf{v}}_f - \vec{\mathbf{v}}_i}{\Delta t} \right)$$

Momentum

We can rewrite Newton's Second law in a slightly different way:

$$\sum \vec{\mathbf{F}} = m \vec{\mathbf{a}} \Rightarrow \vec{\mathbf{F}}_{av} = m \vec{\mathbf{a}}_{av}$$

$$m \vec{\mathbf{a}}_{av} = m \left(\frac{\Delta \vec{\mathbf{v}}}{\Delta t} \right) = m \left(\frac{\vec{\mathbf{v}}_f - \vec{\mathbf{v}}_i}{\Delta t} \right) = \frac{m \vec{\mathbf{v}}_f - m \vec{\mathbf{v}}_i}{\Delta t}$$

Momentum

We can rewrite Newton's Second law in a slightly different way:

$$\sum \vec{\mathbf{F}} = m \vec{\mathbf{a}} \Rightarrow \vec{\mathbf{F}}_{av} = m \vec{\mathbf{a}}_{av}$$

$$m \vec{\mathbf{a}}_{av} = m \left(\frac{\Delta \vec{\mathbf{v}}}{\Delta t} \right) = m \left(\frac{\vec{\mathbf{v}}_f - \vec{\mathbf{v}}_i}{\Delta t} \right) = \frac{m \vec{\mathbf{v}}_f - m \vec{\mathbf{v}}_i}{\Delta t}$$

$$\boxed{\vec{\mathbf{F}}_{av} = \frac{\Delta \vec{\mathbf{p}}}{\Delta t}}$$

Momentum

We can rewrite Newton's Second law in a slightly different way:

$$\sum \vec{\mathbf{F}} = m \vec{\mathbf{a}} \Rightarrow \vec{\mathbf{F}}_{av} = m \vec{\mathbf{a}}_{av}$$

$$m \vec{\mathbf{a}}_{av} = m \left(\frac{\Delta \vec{\mathbf{v}}}{\Delta t} \right) = m \left(\frac{\vec{\mathbf{v}}_f - \vec{\mathbf{v}}_i}{\Delta t} \right) = \frac{m \vec{\mathbf{v}}_f - m \vec{\mathbf{v}}_i}{\Delta t}$$

$$\vec{\mathbf{F}}_{av} = \frac{\Delta \vec{\mathbf{p}}}{\Delta t}$$

Momentum: $\vec{\mathbf{p}} = m \vec{\mathbf{v}}$

Momentum

We can rewrite Newton's Second law in a slightly different way:

$$\sum \vec{\mathbf{F}} = m \vec{\mathbf{a}} \Rightarrow \vec{\mathbf{F}}_{av} = m \vec{\mathbf{a}}_{av}$$

$$m \vec{\mathbf{a}}_{av} = m \left(\frac{\Delta \vec{\mathbf{v}}}{\Delta t} \right) = m \left(\frac{\vec{\mathbf{v}}_f - \vec{\mathbf{v}}_i}{\Delta t} \right) = \frac{m \vec{\mathbf{v}}_f - m \vec{\mathbf{v}}_i}{\Delta t}$$

$$\vec{\mathbf{F}}_{av} = \frac{\Delta \vec{\mathbf{p}}}{\Delta t}$$

Momentum: $\vec{\mathbf{p}} = m \vec{\mathbf{v}}$

Unit: $kg \cdot m/s$


No fancy name!

Momentum

We can rewrite Newton's Second law in a slightly different way:

$$\sum \vec{\mathbf{F}} = m \vec{\mathbf{a}} \Rightarrow \vec{\mathbf{F}}_{av} = m \vec{\mathbf{a}}_{av}$$

$$m \vec{\mathbf{a}}_{av} = m \left(\frac{\Delta \vec{\mathbf{v}}}{\Delta t} \right) = m \left(\frac{\vec{\mathbf{v}}_f - \vec{\mathbf{v}}_i}{\Delta t} \right) = \frac{m \vec{\mathbf{v}}_f - m \vec{\mathbf{v}}_i}{\Delta t}$$

$$\vec{\mathbf{F}}_{av} = \frac{\Delta \vec{\mathbf{p}}}{\Delta t}$$

Momentum: $\vec{\mathbf{p}} = m \vec{\mathbf{v}}$

Unit: $kg \cdot m/s$

 No fancy name!

Momentum measures how “hard” it is to change the velocity of an object in a given period of time.

Impulse

Related to Momentum is Impulse, \vec{J} :

Impulse

Related to Momentum is Impulse, \vec{J} :

$$\vec{J} = \vec{F}_{av} \Delta t$$

$$\text{Unit: } N \cdot s = (kg \cdot m/s^2) \cdot s = kg \cdot m/s$$

Impulse

Related to Momentum is Impulse, \vec{J} :

$$\boxed{\vec{J} = \vec{F}_{av} \Delta t} \quad \text{Unit: } N \cdot s = (kg \cdot m/s^2) \cdot s = kg \cdot m/s$$

Impulse-Momentum Theorem (Average Force Version):

Impulse

Related to Momentum is Impulse, \vec{J} :

$$\boxed{\vec{J} = \vec{F}_{av} \Delta t} \quad \text{Unit: } N \cdot s = (kg \cdot m/s^2) \cdot s = kg \cdot m/s$$

Impulse-Momentum Theorem (Average Force Version):

$$\vec{F}_{av} = \frac{\Delta \vec{p}}{\Delta t}$$

Impulse

Related to Momentum is Impulse, \vec{J} :

$$\boxed{\vec{J} = \vec{F}_{av} \Delta t} \quad \text{Unit: } N \cdot s = (kg \cdot m/s^2) \cdot s = kg \cdot m/s$$

Impulse-Momentum Theorem (Average Force Version):

$$\vec{F}_{av} = \frac{\Delta \vec{p}}{\Delta t} \Rightarrow \vec{F}_{av} \Delta t = \Delta \vec{p}$$

Impulse

Related to Momentum is Impulse, \vec{J} :

$$\boxed{\vec{J} = \vec{F}_{av} \Delta t} \quad \text{Unit: } N \cdot s = (kg \cdot m/s^2) \cdot s = kg \cdot m/s$$

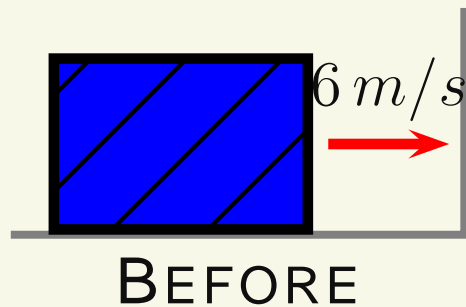
Impulse-Momentum Theorem (Average Force Version):

$$\vec{F}_{av} = \frac{\Delta \vec{p}}{\Delta t} \Rightarrow \vec{F}_{av} \Delta t = \Delta \vec{p} \Rightarrow \boxed{\vec{J} = \Delta \vec{p}}$$

Impulse-Momentum Exercise I

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

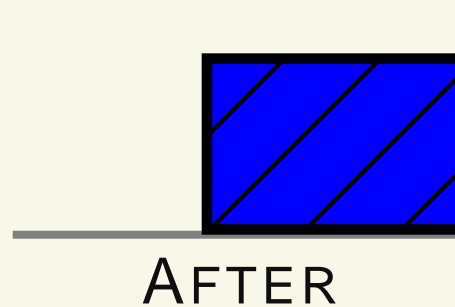
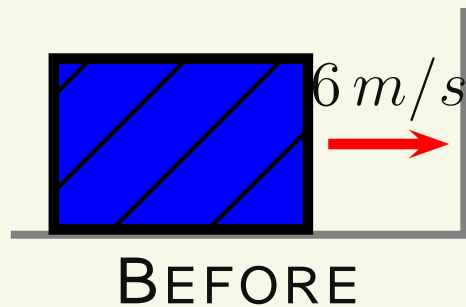
A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. What impulse is imparted to the block?



Impulse-Momentum Exercise I

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

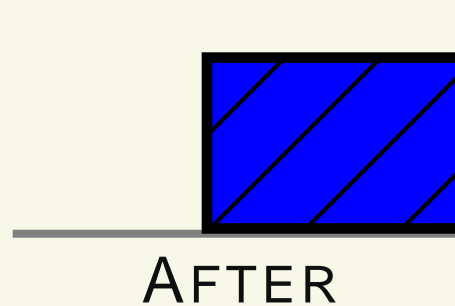
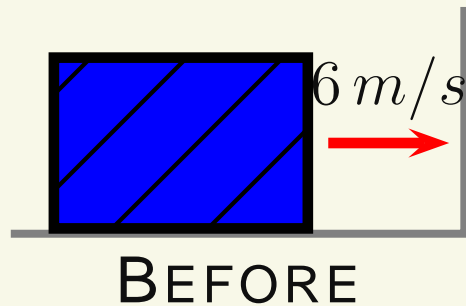
A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. What impulse is imparted to the block?



Impulse-Momentum Exercise I

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. What impulse is imparted to the block?

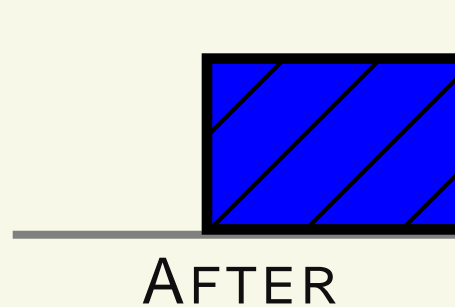
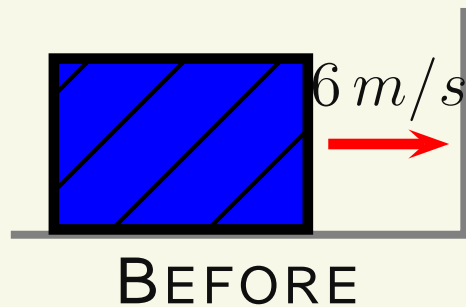


(a) $60\text{ kg} \cdot \text{m/s}$, \leftarrow

Impulse-Momentum Exercise I

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. What impulse is imparted to the block?

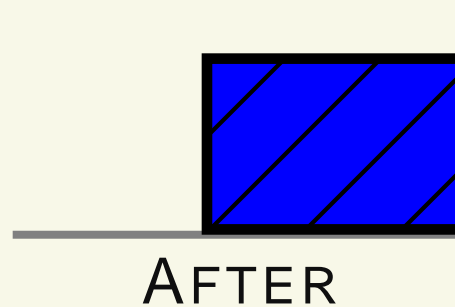
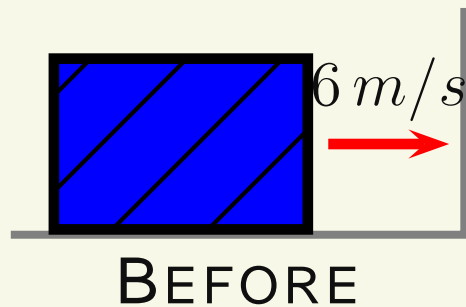


- (a) $60\text{ kg} \cdot \text{m/s}$, \leftarrow (b) $60\text{ kg} \cdot \text{m/s}$, \rightarrow

Impulse-Momentum Exercise I

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. What impulse is imparted to the block?

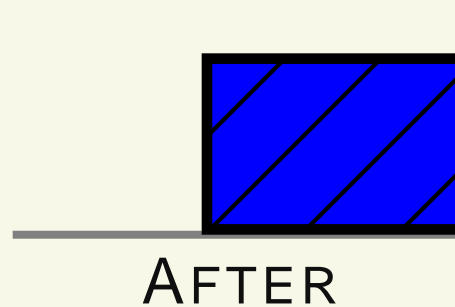
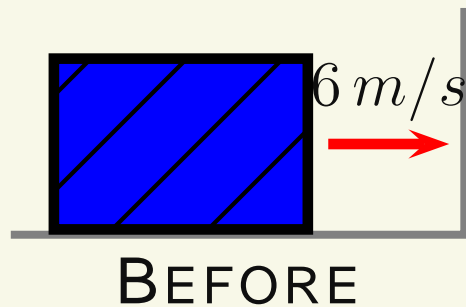


- (a) $60\text{ kg} \cdot \text{m/s}$, \leftarrow (b) $60\text{ kg} \cdot \text{m/s}$, \rightarrow (c) $30\text{ kg} \cdot \text{m/s}$, \leftarrow

Impulse-Momentum Exercise I

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. What impulse is imparted to the block?

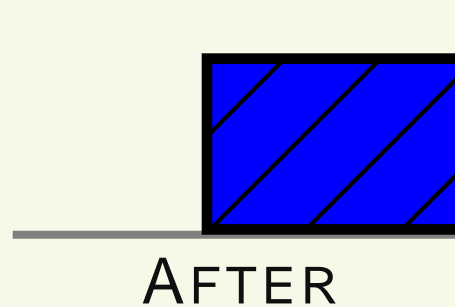
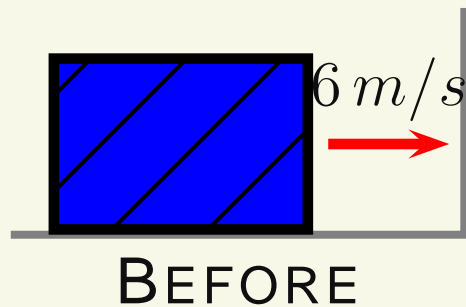


- (a) $60\text{ kg} \cdot \text{m/s}, \leftarrow$ (b) $60\text{ kg} \cdot \text{m/s}, \rightarrow$ (c) $30\text{ kg} \cdot \text{m/s}, \leftarrow$
(d) $30\text{ kg} \cdot \text{m/s}, \rightarrow$

Impulse-Momentum Exercise I

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. What impulse is imparted to the block?

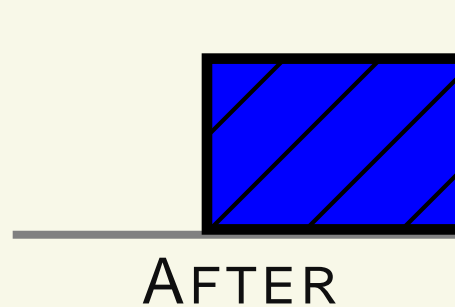
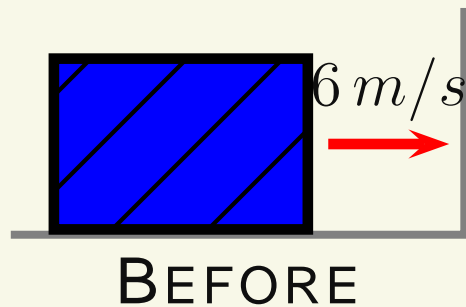


- (a) $60\text{ kg} \cdot \text{m/s}, \leftarrow$ (b) $60\text{ kg} \cdot \text{m/s}, \rightarrow$ (c) $30\text{ kg} \cdot \text{m/s}, \leftarrow$
(d) $30\text{ kg} \cdot \text{m/s}, \rightarrow$ (e) $15\text{ kg} \cdot \text{m/s}, \leftarrow$

Impulse-Momentum Exercise I

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. What impulse is imparted to the block?



(a) $60\text{ kg} \cdot \text{m/s}$, \leftarrow

(b) $60\text{ kg} \cdot \text{m/s}$, \rightarrow

(c) $30\text{ kg} \cdot \text{m/s}$, \leftarrow

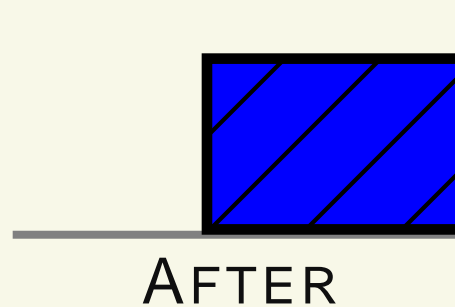
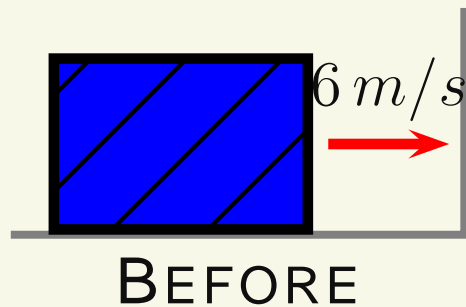
(d) $30\text{ kg} \cdot \text{m/s}$, \rightarrow

(e) $15\text{ kg} \cdot \text{m/s}$, \leftarrow

Impulse-Momentum Exercise I

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. What impulse is imparted to the block?



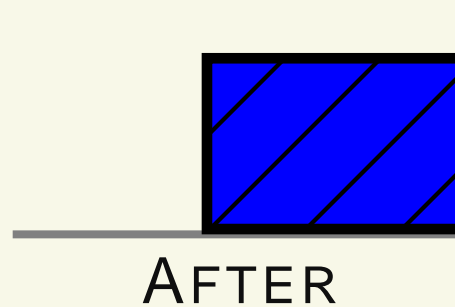
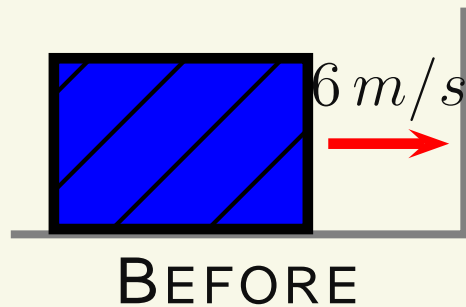
$$(c) 30\text{ kg} \cdot \text{m/s}, \leftarrow$$

$$J_x = \Delta p_x = 0 - 30\text{ kg} \cdot \text{m/s} = -30\text{ kg} \cdot \text{m/s}$$

Impulse-Momentum Exercise II

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

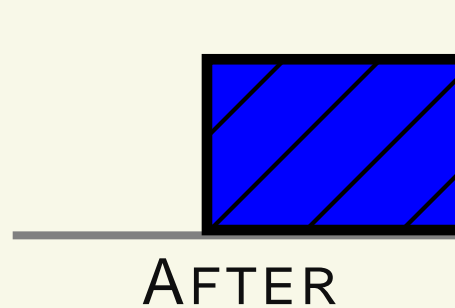
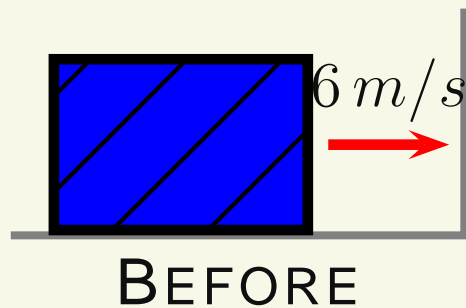
A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. If the block stops in 0.1 s , what is the average force acting on it?



Impulse-Momentum Exercise II

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. If the block stops in 0.1 s , what is the average force acting on it?

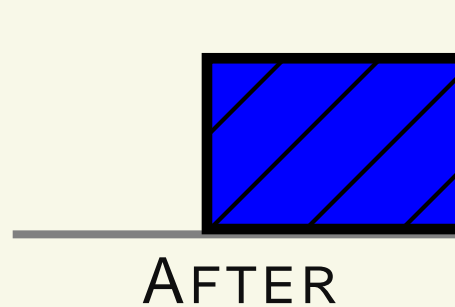
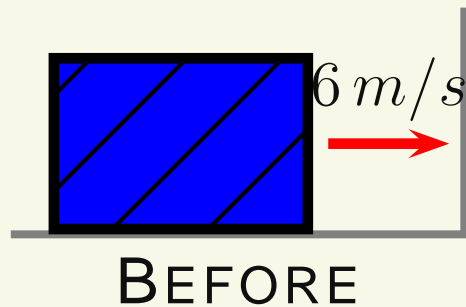


(a) 300 N , \leftarrow

Impulse-Momentum Exercise II

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. If the block stops in 0.1 s , what is the average force acting on it?



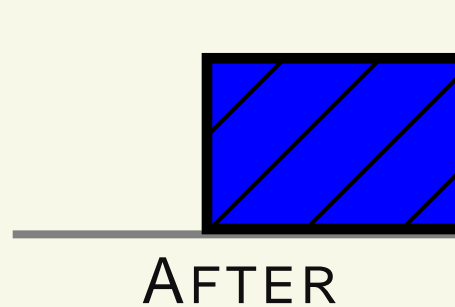
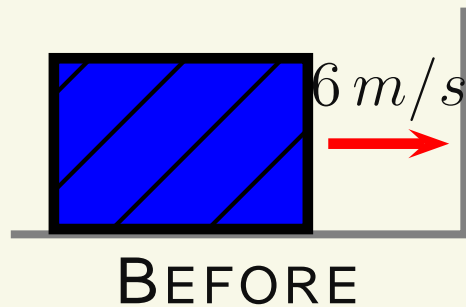
(a) 300 N , \leftarrow

(b) 300 N , \rightarrow

Impulse-Momentum Exercise II

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. If the block stops in 0.1 s , what is the average force acting on it?



(a) 300 N , \leftarrow

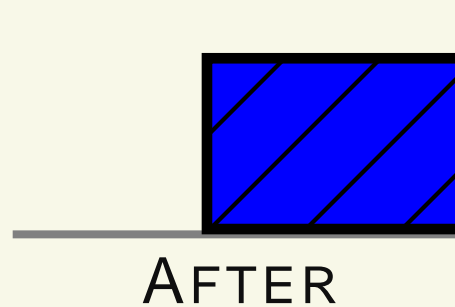
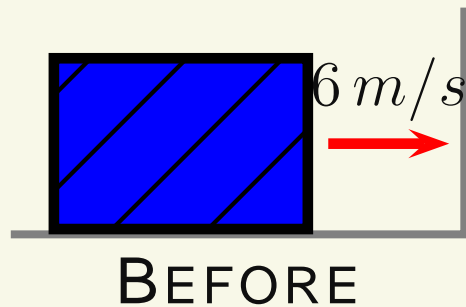
(b) 300 N , \rightarrow

(c) 3 N , \leftarrow

Impulse-Momentum Exercise II

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. If the block stops in 0.1 s , what is the average force acting on it?



(a) 300 N , \leftarrow

(b) 300 N , \rightarrow

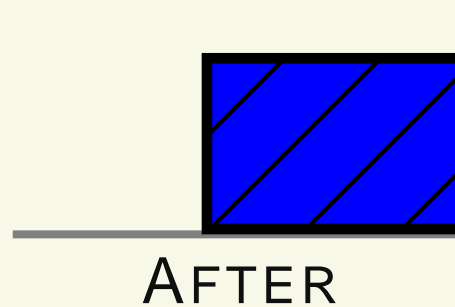
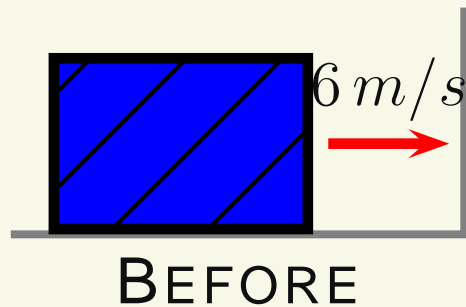
(c) 3 N , \leftarrow

(d) 3 N , \rightarrow

Impulse-Momentum Exercise II

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. If the block stops in 0.1 s , what is the average force acting on it?



(a) 300 N , \leftarrow

(b) 300 N , \rightarrow

(c) 3 N , \leftarrow

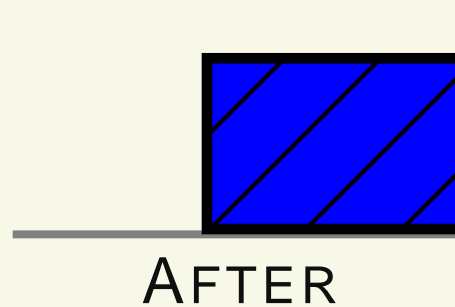
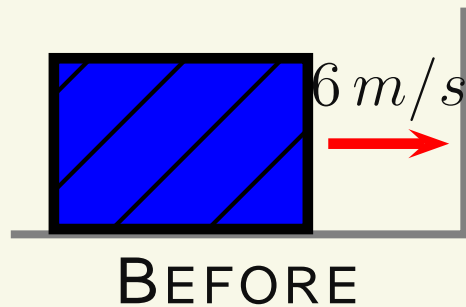
(d) 3 N , \rightarrow

(e) 600 N , \leftarrow

Impulse-Momentum Exercise II

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. If the block stops in 0.1 s , what is the average force acting on it?



(a) 300 N , \leftarrow

(b) 300 N , \rightarrow

(c) 3 N , \leftarrow

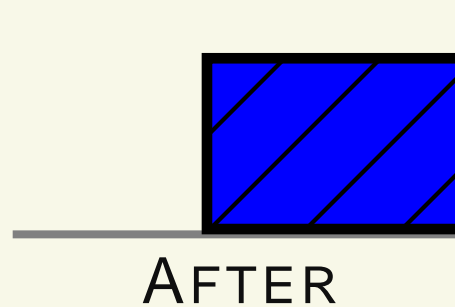
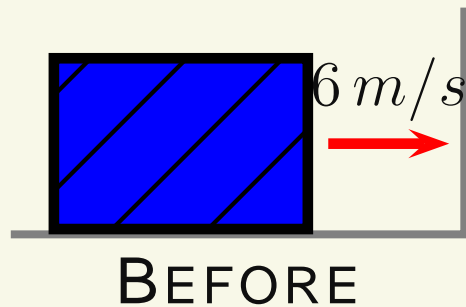
(d) 3 N , \rightarrow

(e) 600 N , \leftarrow

Impulse-Momentum Exercise II

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. If the block stops in 0.1 s , what is the average force acting on it?



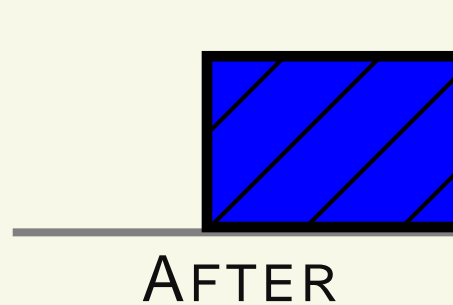
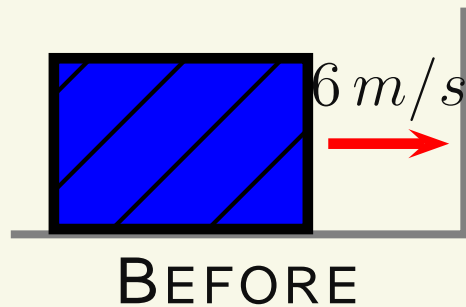
(a) $300\text{ N}, \leftarrow$

$$F_{av} = \frac{\Delta p}{\Delta t} = \frac{J}{\Delta t}$$

Impulse-Momentum Exercise II

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the right when it hits a wall and stops. If the block stops in 0.1 s , what is the average force acting on it?



(a) 300 N , \leftarrow

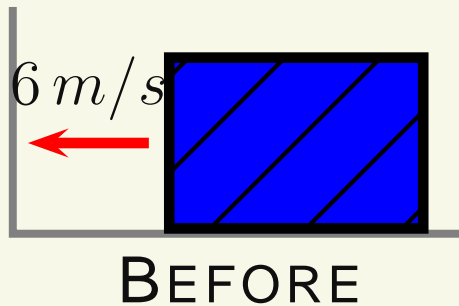
$$F_{av} = \frac{\Delta p}{\Delta t} = \frac{J}{\Delta t}$$

Average force, impulse, and change in momentum always have the same direction

Impulse-Momentum Exercise III

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

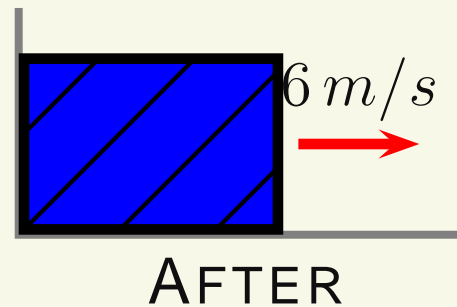
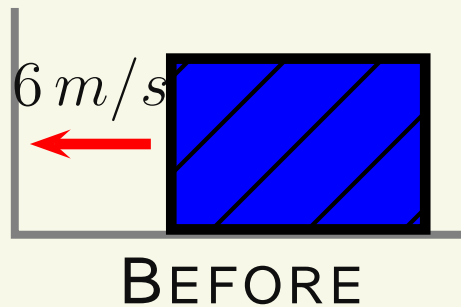
A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. What impulse is imparted to the block?



Impulse-Momentum Exercise III

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

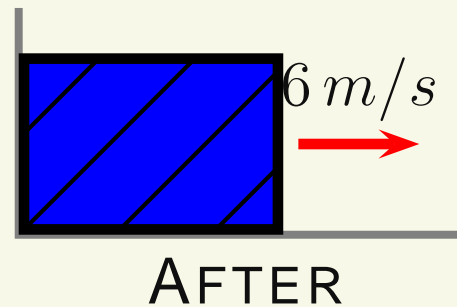
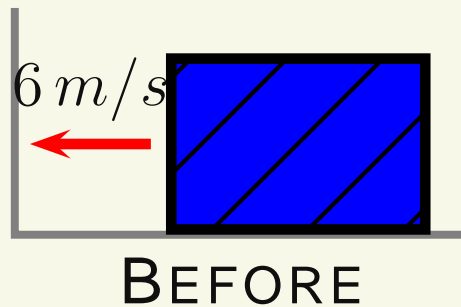
A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. What impulse is imparted to the block?



Impulse-Momentum Exercise III

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. What impulse is imparted to the block?

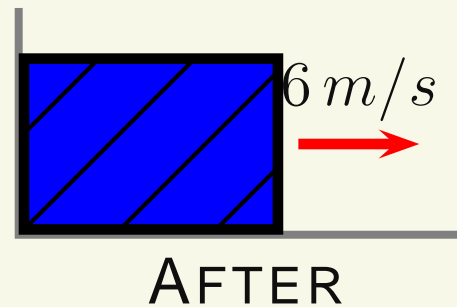
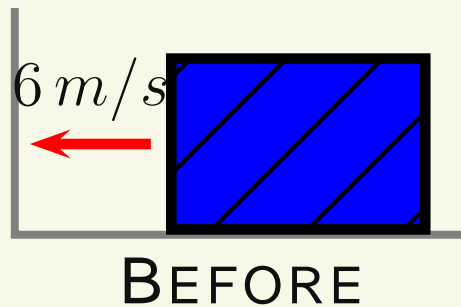


(a) $60\text{ kg} \cdot \text{m/s}$, \leftarrow

Impulse-Momentum Exercise III

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. What impulse is imparted to the block?

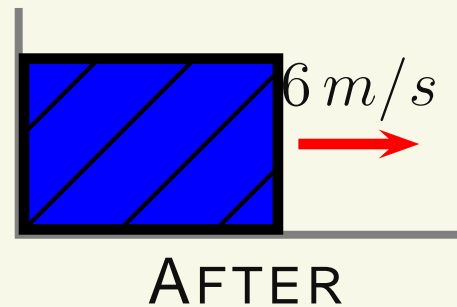
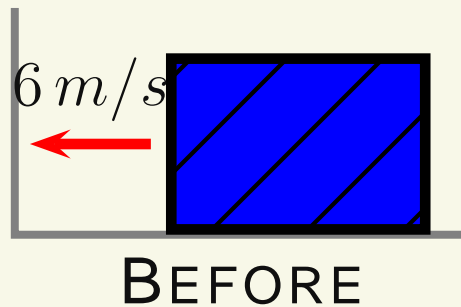


- (a) $60\text{ kg} \cdot \text{m/s}$, \leftarrow (b) $60\text{ kg} \cdot \text{m/s}$, \rightarrow

Impulse-Momentum Exercise III

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. What impulse is imparted to the block?

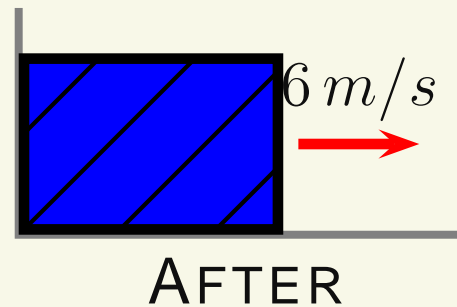
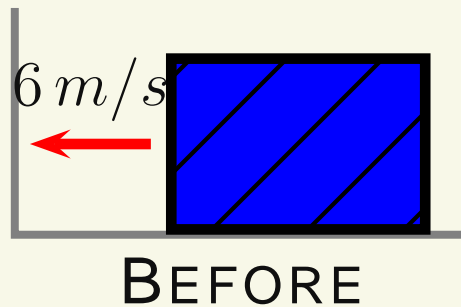


- (a) $60\text{ kg} \cdot \text{m/s}, \leftarrow$ (b) $60\text{ kg} \cdot \text{m/s}, \rightarrow$ (c) $30\text{ kg} \cdot \text{m/s}, \leftarrow$

Impulse-Momentum Exercise III

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. What impulse is imparted to the block?

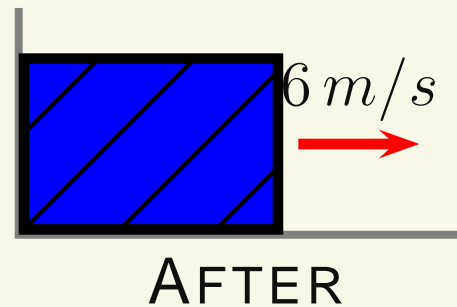
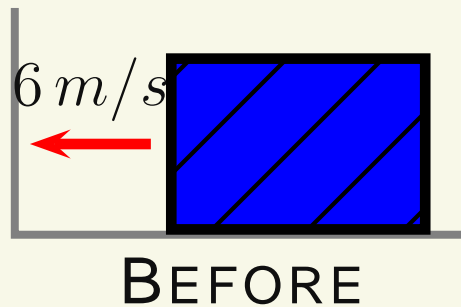


- (a) $60\text{ kg} \cdot \text{m/s}, \leftarrow$ (b) $60\text{ kg} \cdot \text{m/s}, \rightarrow$ (c) $30\text{ kg} \cdot \text{m/s}, \leftarrow$
(d) $30\text{ kg} \cdot \text{m/s}, \rightarrow$

Impulse-Momentum Exercise III

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. What impulse is imparted to the block?

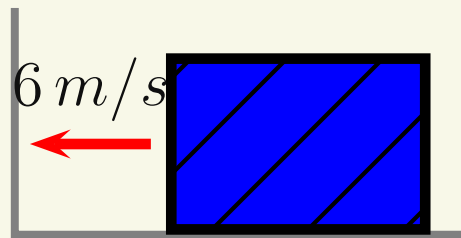


- (a) $60\text{ kg} \cdot \text{m/s}, \leftarrow$ (b) $60\text{ kg} \cdot \text{m/s}, \rightarrow$ (c) $30\text{ kg} \cdot \text{m/s}, \leftarrow$
(d) $30\text{ kg} \cdot \text{m/s}, \rightarrow$ (e) $0\text{ kg} \cdot \text{m/s}, \leftarrow$

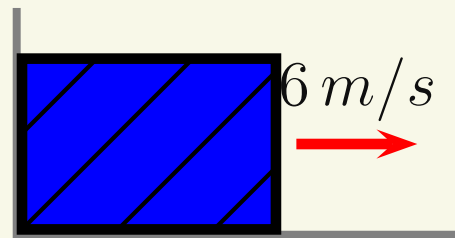
Impulse-Momentum Exercise III

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. What impulse is imparted to the block?



BEFORE



AFTER

(a) $60\text{ kg} \cdot \text{m/s}$, \leftarrow

(b) $60\text{ kg} \cdot \text{m/s}$, \rightarrow

(c) $30\text{ kg} \cdot \text{m/s}$, \leftarrow

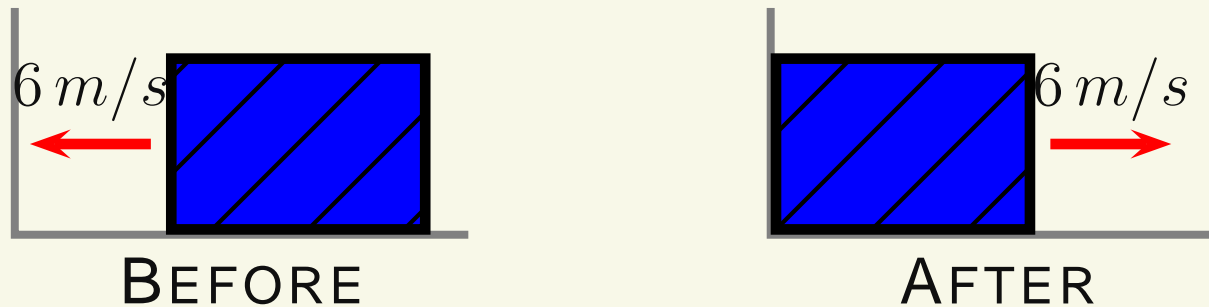
(d) $30\text{ kg} \cdot \text{m/s}$, \rightarrow

(e) $0\text{ kg} \cdot \text{m/s}$, \leftarrow

Impulse-Momentum Exercise III

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. What impulse is imparted to the block?



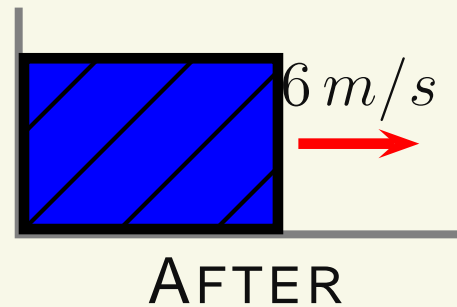
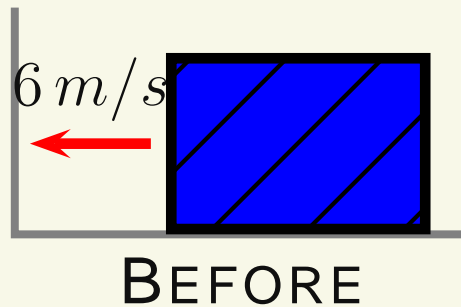
$$(b) 60\text{ kg} \cdot \text{m/s}, \rightarrow$$

$$J_x = \Delta p_x = +30\text{ kg} \cdot \text{m/s} - (-30\text{ kg} \cdot \text{m/s}) = +60\text{ kg} \cdot \text{m/s}$$

Impulse-Momentum Exercise IV

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

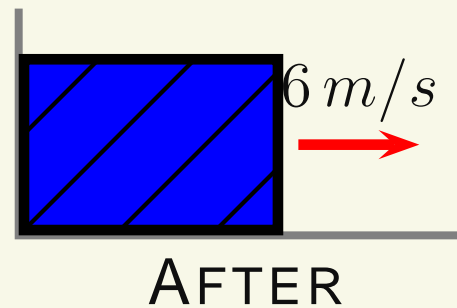
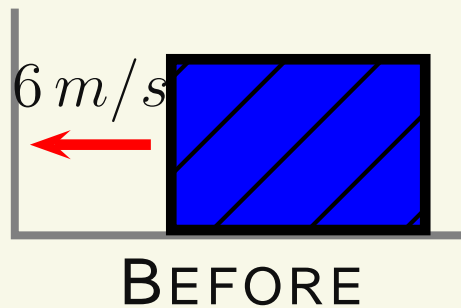
A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. If this bounce takes 0.1 s , what is the average force?



Impulse-Momentum Exercise IV

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. If this bounce takes 0.1 s , what is the average force?

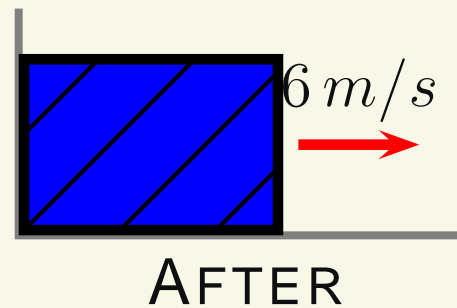
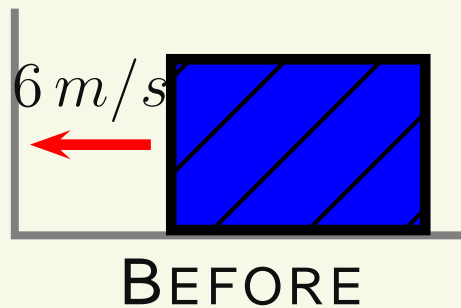


(a) $6\text{ N}, \rightarrow$

Impulse-Momentum Exercise IV

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. If this bounce takes 0.1 s , what is the average force?



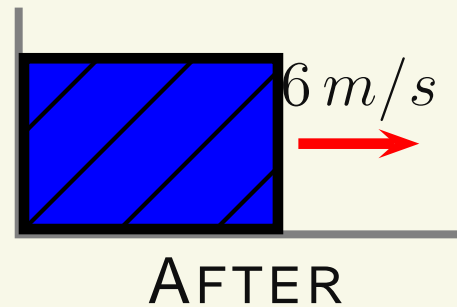
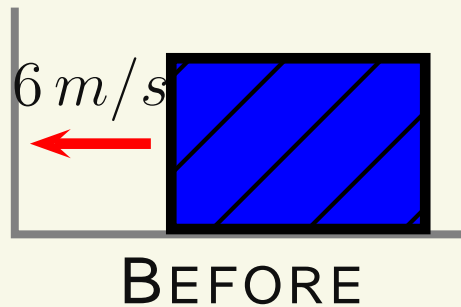
(a) $6\text{ N}, \rightarrow$

(b) $300\text{ N}, \leftarrow$

Impulse-Momentum Exercise IV

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. If this bounce takes 0.1 s , what is the average force?



(a) 6 N , \rightarrow

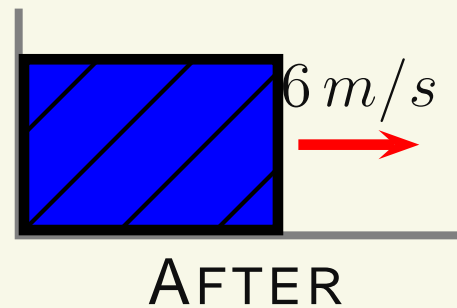
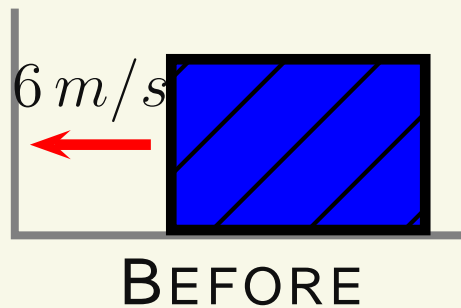
(b) 300 N , \leftarrow

(c) 300 N , \rightarrow

Impulse-Momentum Exercise IV

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. If this bounce takes 0.1 s , what is the average force?



(a) $6\text{ N}, \rightarrow$

(b) $300\text{ N}, \leftarrow$

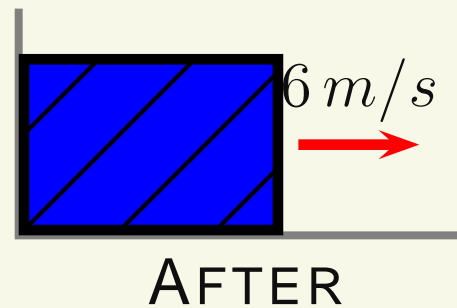
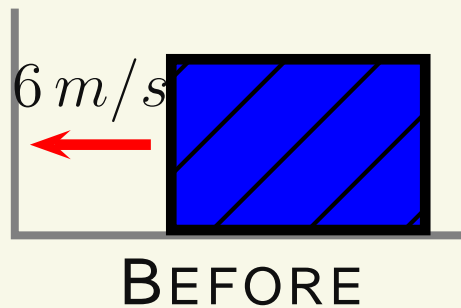
(c) $300\text{ N}, \rightarrow$

(d) $600\text{ N}, \leftarrow$

Impulse-Momentum Exercise IV

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. If this bounce takes 0.1 s , what is the average force?



(a) $6\text{ N}, \rightarrow$

(b) $300\text{ N}, \leftarrow$

(c) $300\text{ N}, \rightarrow$

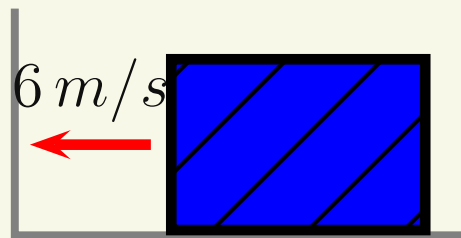
(d) $600\text{ N}, \leftarrow$

(e) $600\text{ N}, \rightarrow$

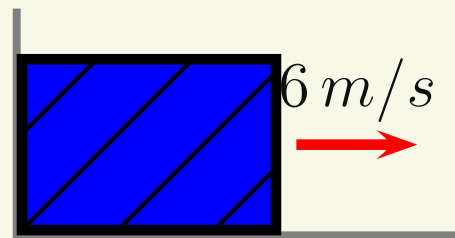
Impulse-Momentum Exercise IV

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. If this bounce takes 0.1 s , what is the average force?



BEFORE



AFTER

(a) $6\text{ N}, \rightarrow$

(b) $300\text{ N}, \leftarrow$

(c) $300\text{ N}, \rightarrow$

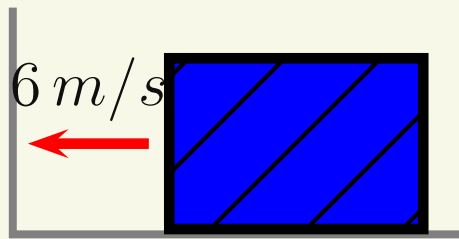
(d) $600\text{ N}, \leftarrow$

(e) $600\text{ N}, \rightarrow$

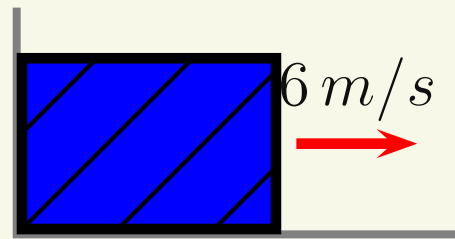
Impulse-Momentum Exercise IV

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. If this bounce takes 0.1 s , what is the average force?



BEFORE



AFTER

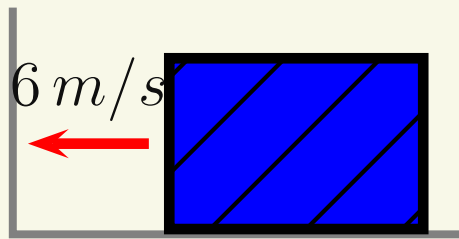
(e) $600\text{ N}, \rightarrow$

$$\vec{F}_{av} = \frac{\vec{J}}{\Delta t}$$

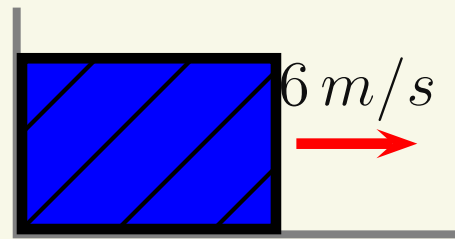
Impulse-Momentum Exercise IV

$$\vec{J} = \vec{F}_{av} \Delta t = \Delta \vec{p}$$

A 5.0-kg block is sliding on a frictionless, horizontal surface going 6.0 m/s to the left when it hits a wall and bounces back with the same speed. If this bounce takes 0.1 s , what is the average force?



BEFORE



AFTER

(e) $600\text{ N}, \rightarrow$

$$\vec{F}_{av} = \frac{\vec{J}}{\Delta t}$$

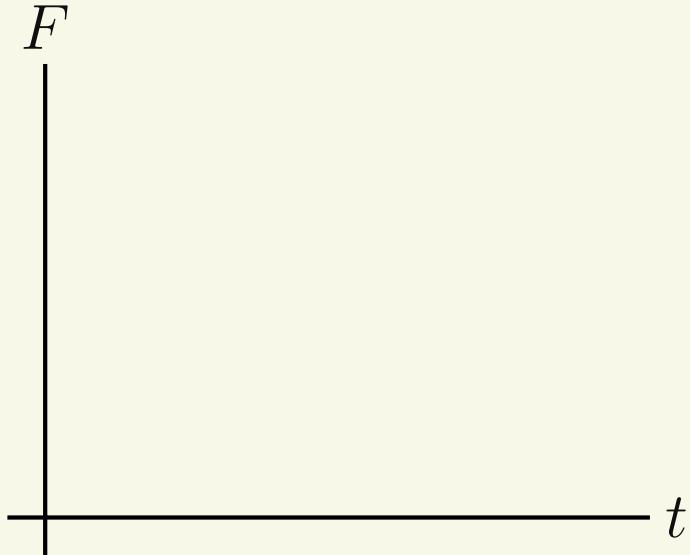
Bouncing doubles the force

Impulse-Momentum Theorem - Variable Forces

The Impulse-Momentum Theorem also holds for non-constant forces!

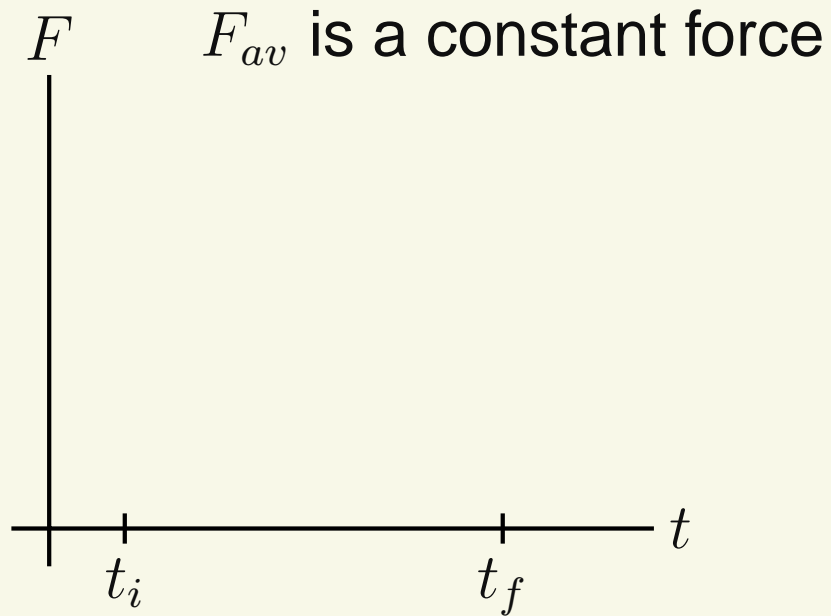
Impulse-Momentum Theorem - Variable Forces

The Impulse-Momentum Theorem also holds for non-constant forces!



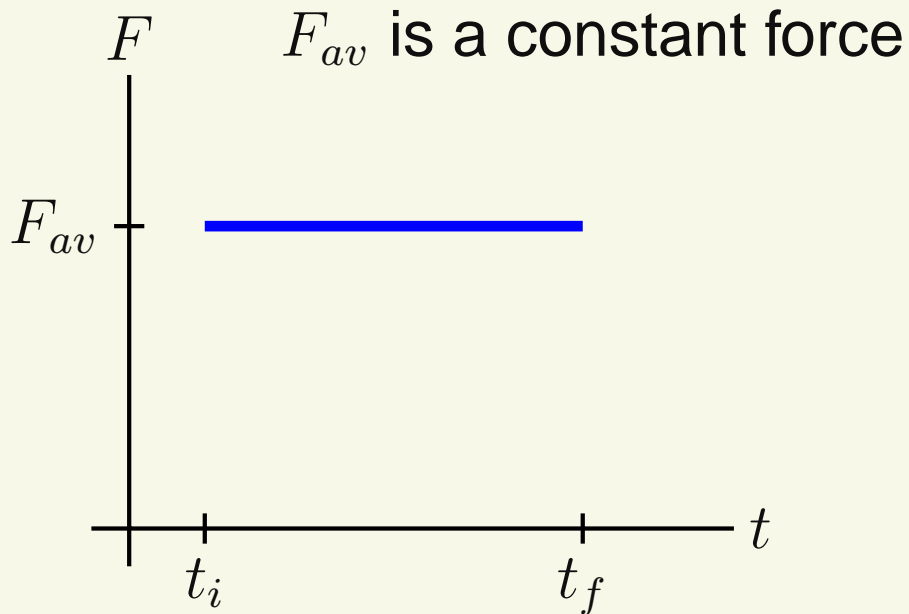
Impulse-Momentum Theorem - Variable Forces

The Impulse-Momentum Theorem also holds for non-constant forces!



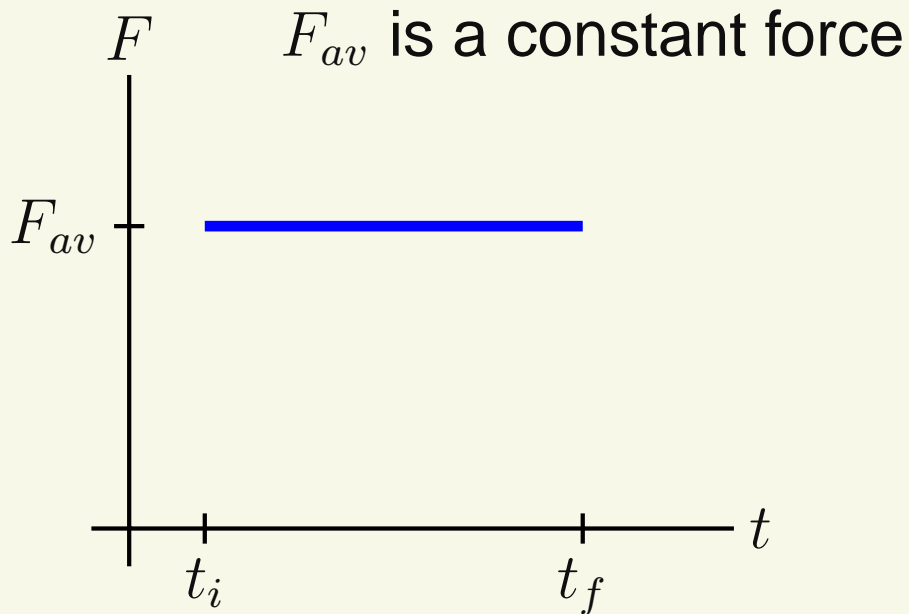
Impulse-Momentum Theorem - Variable Forces

The Impulse-Momentum Theorem also holds for non-constant forces!



Impulse-Momentum Theorem - Variable Forces

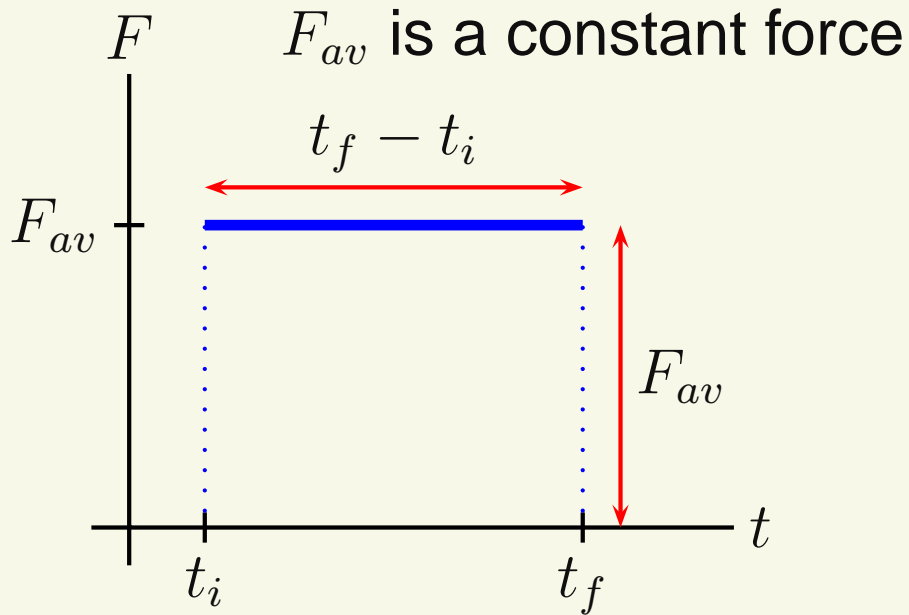
The Impulse-Momentum Theorem also holds for non-constant forces!



$$J = F_{av} \Delta t = F_{av} (t_f - t_i)$$

Impulse-Momentum Theorem - Variable Forces

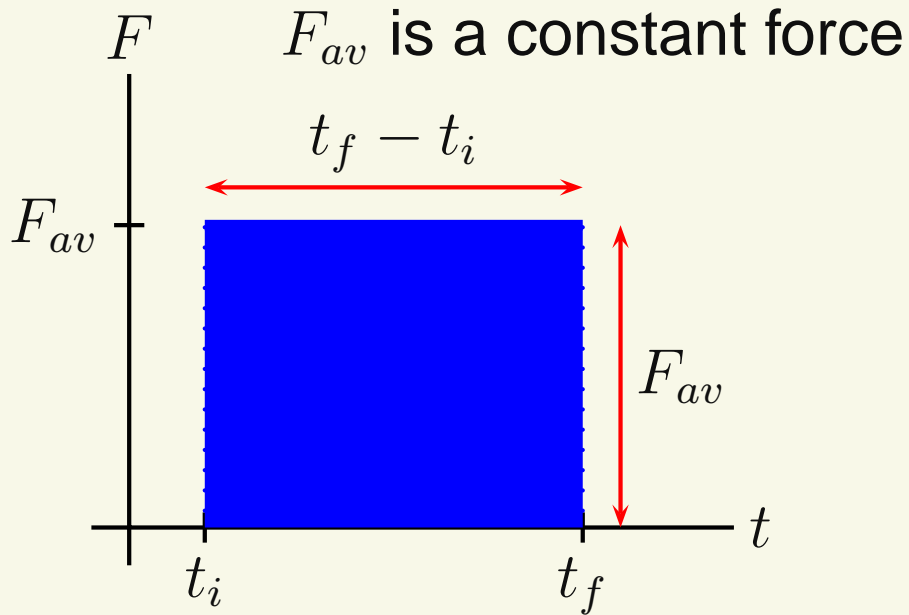
The Impulse-Momentum Theorem also holds for non-constant forces!



$$J = F_{av} \Delta t = F_{av} (t_f - t_i)$$

Impulse-Momentum Theorem - Variable Forces

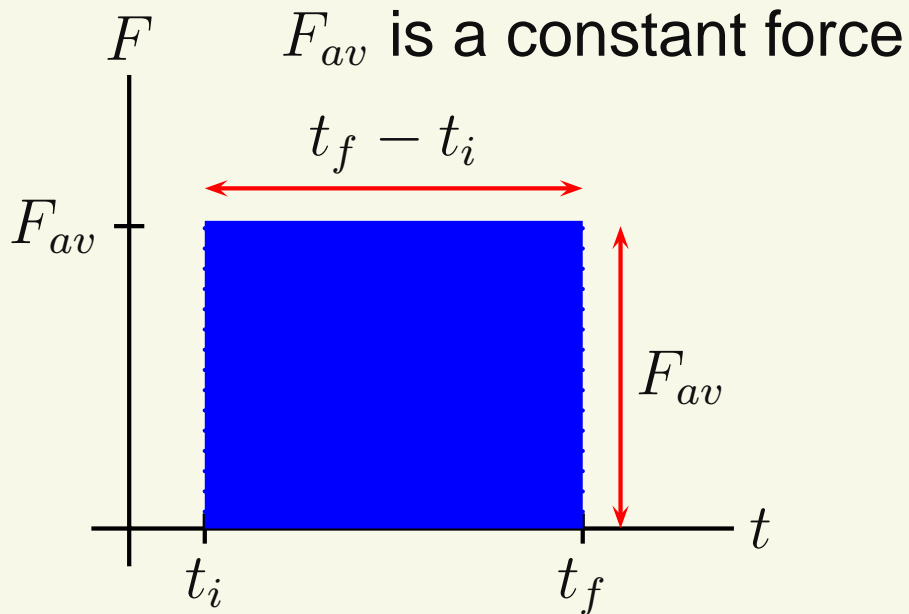
The Impulse-Momentum Theorem also holds for non-constant forces!



$$J = F_{av} \Delta t = F_{av} (t_f - t_i)$$

Impulse-Momentum Theorem - Variable Forces

The Impulse-Momentum Theorem also holds for non-constant forces!

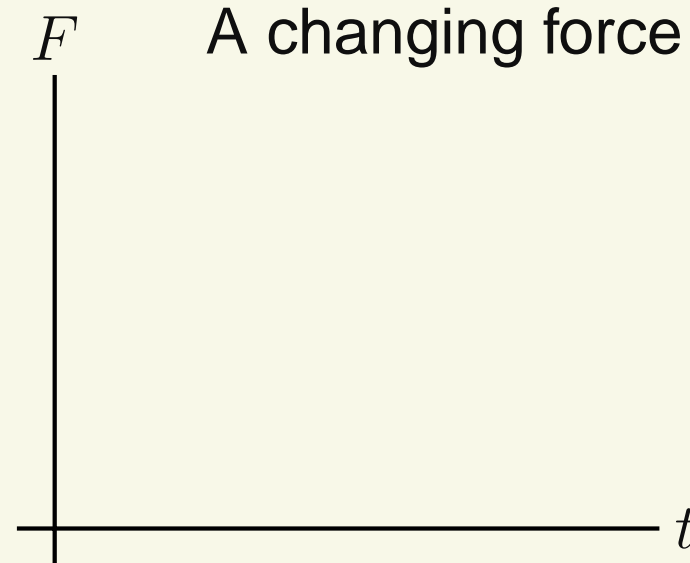
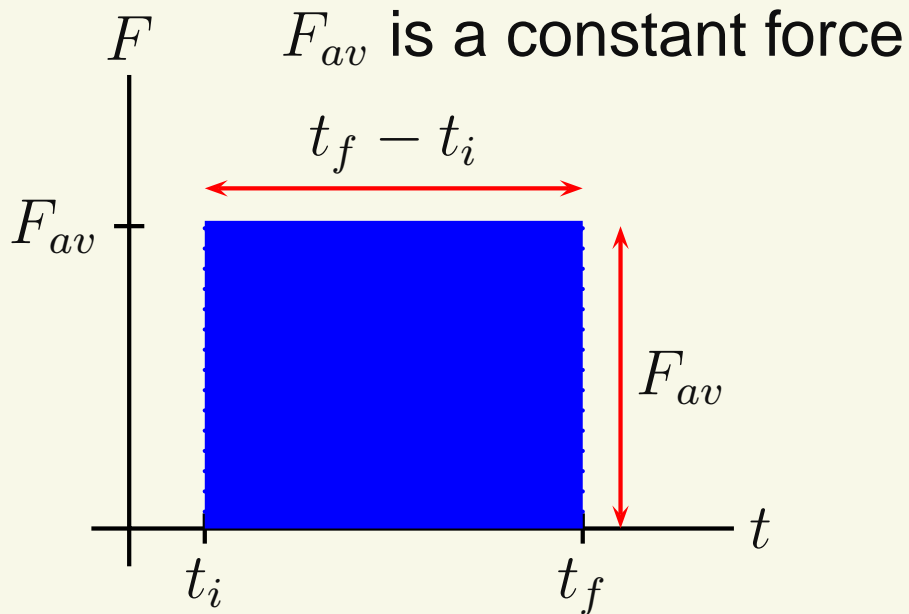


$$J = F_{av} \Delta t = F_{av} (t_f - t_i)$$

Impulse is the area
under the curve

Impulse-Momentum Theorem - Variable Forces

The Impulse-Momentum Theorem also holds for non-constant forces!

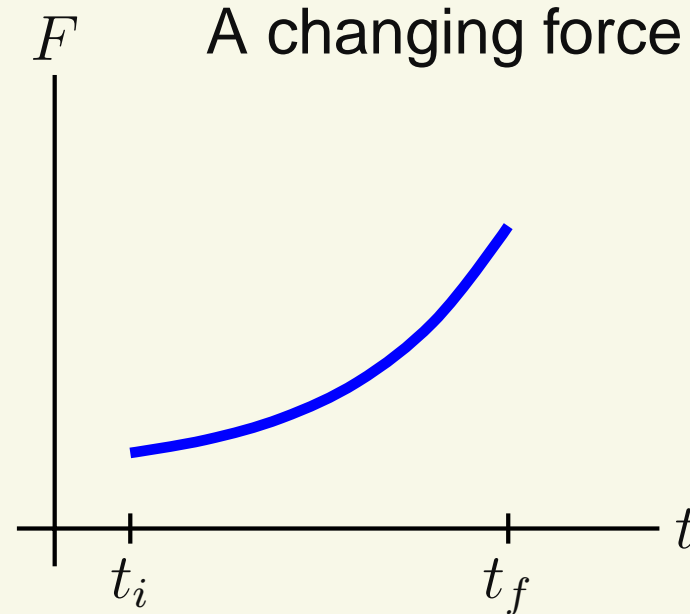
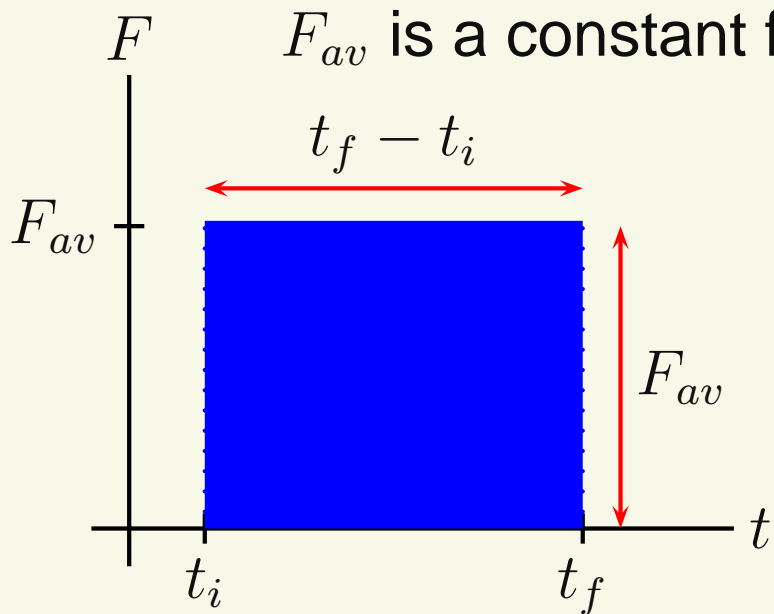


$$J = F_{av} \Delta t = F_{av} (t_f - t_i)$$

Impulse is the area
under the curve

Impulse-Momentum Theorem - Variable Forces

The Impulse-Momentum Theorem also holds for non-constant forces!

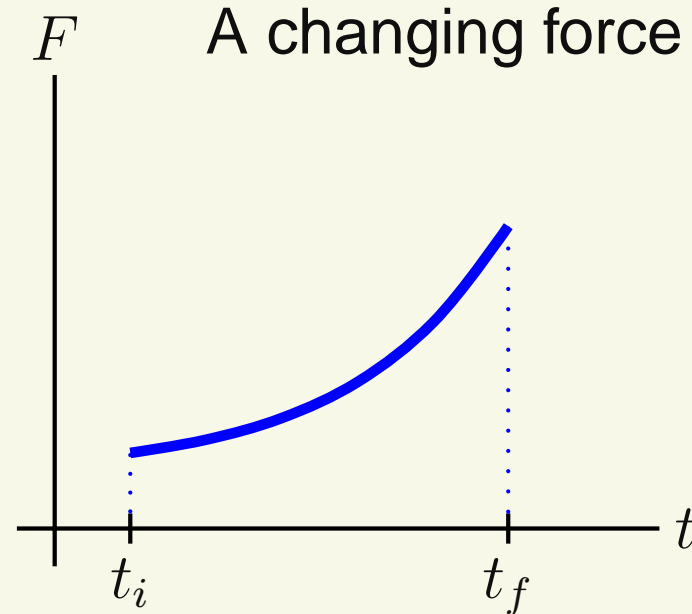
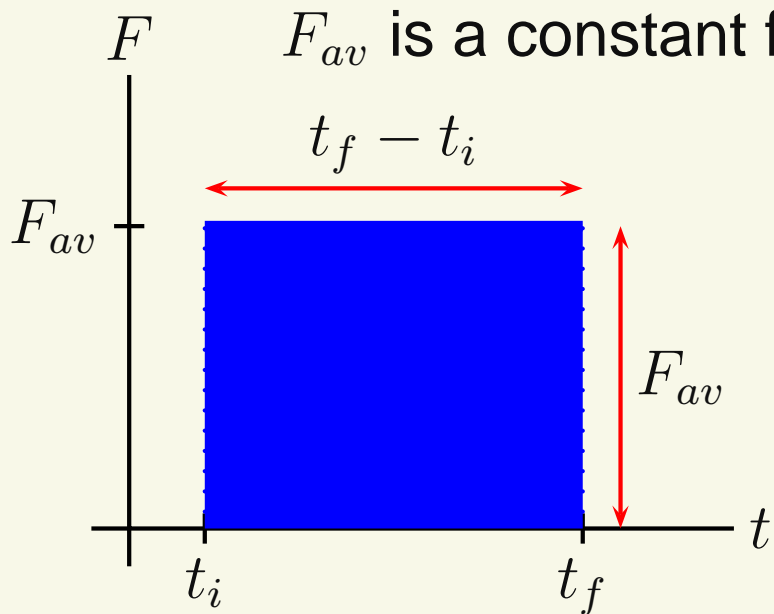


$$J = F_{av} \Delta t = F_{av} (t_f - t_i)$$

Impulse is the area
under the curve

Impulse-Momentum Theorem - Variable Forces

The Impulse-Momentum Theorem also holds for non-constant forces!

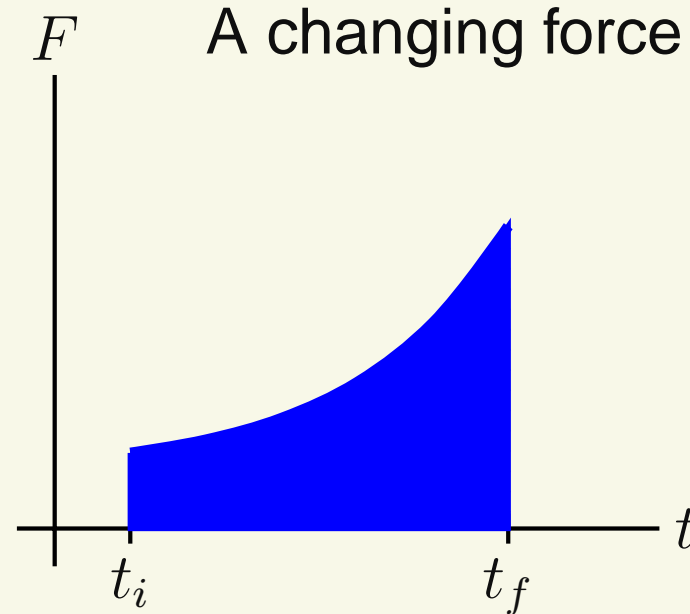
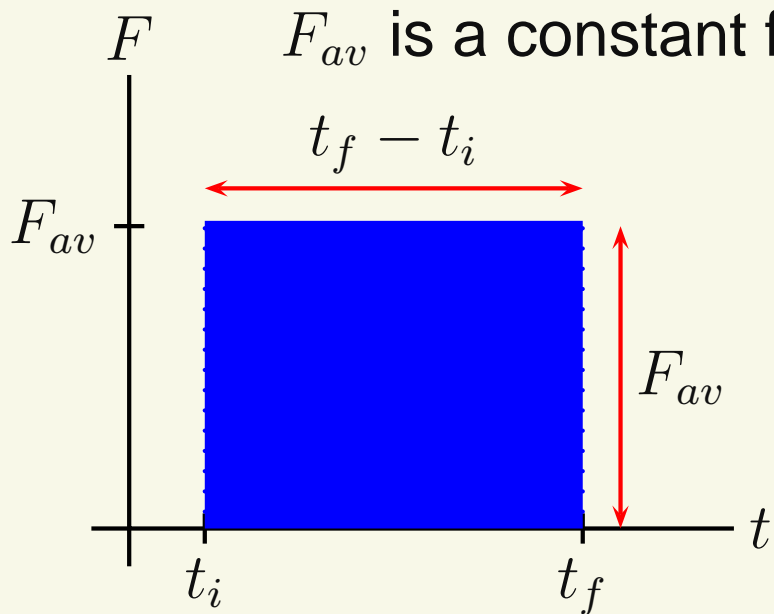


$$J = F_{av} \Delta t = F_{av} (t_f - t_i)$$

Impulse is the area
under the curve

Impulse-Momentum Theorem - Variable Forces

The Impulse-Momentum Theorem also holds for non-constant forces!

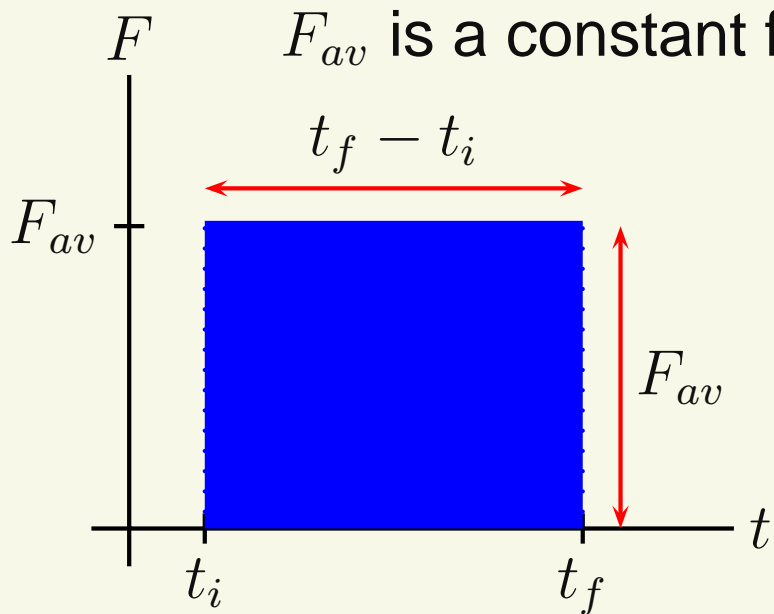


$$J = F_{av} \Delta t = F_{av} (t_f - t_i)$$

Impulse is the area
under the curve

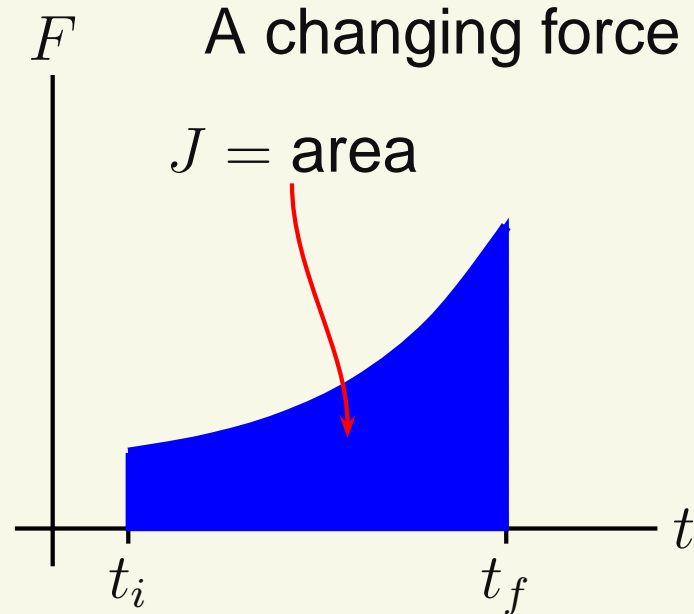
Impulse-Momentum Theorem - Variable Forces

The Impulse-Momentum Theorem also holds for non-constant forces!



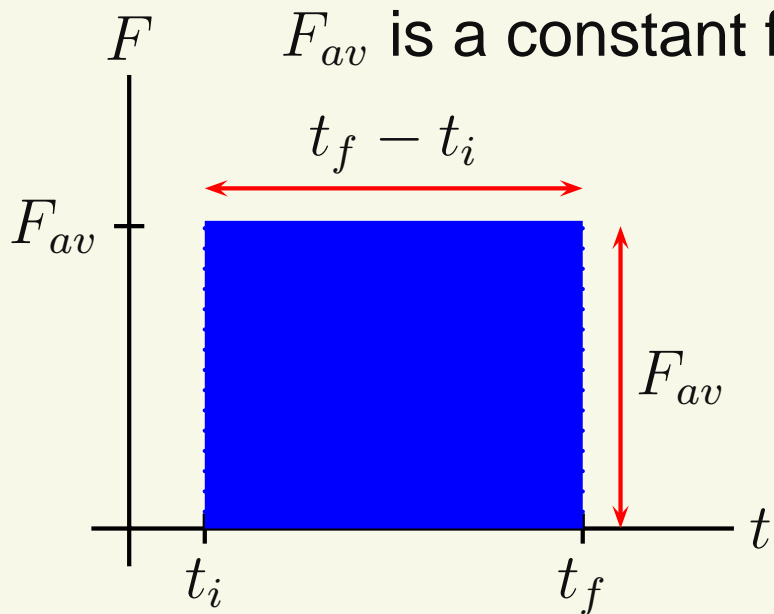
$$J = F_{av} \Delta t = F_{av} (t_f - t_i)$$

Impulse is the area
under the curve



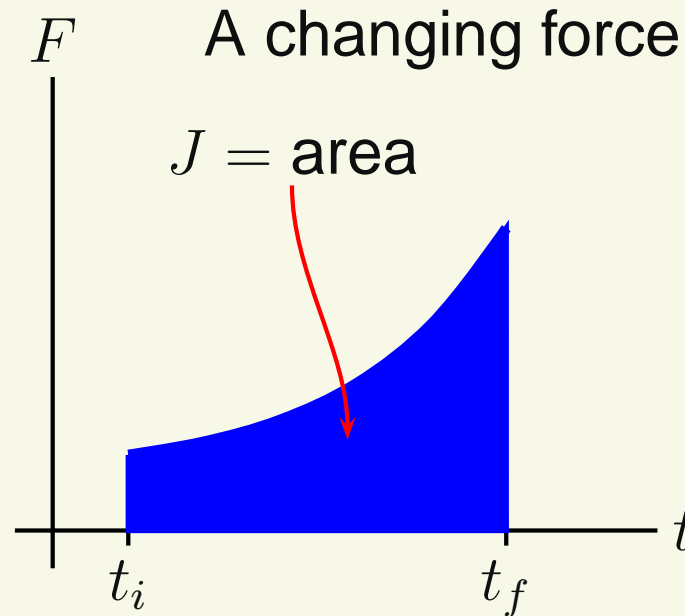
Impulse-Momentum Theorem - Variable Forces

The Impulse-Momentum Theorem also holds for non-constant forces!



$$J = F_{av} \Delta t = F_{av} (t_f - t_i)$$

Impulse is the area under the curve



It is beyond the scope of this course but $J = \Delta p$ still!