

April 10, Week 12

Today: Chapter 9, Rotational Kinetic Energy

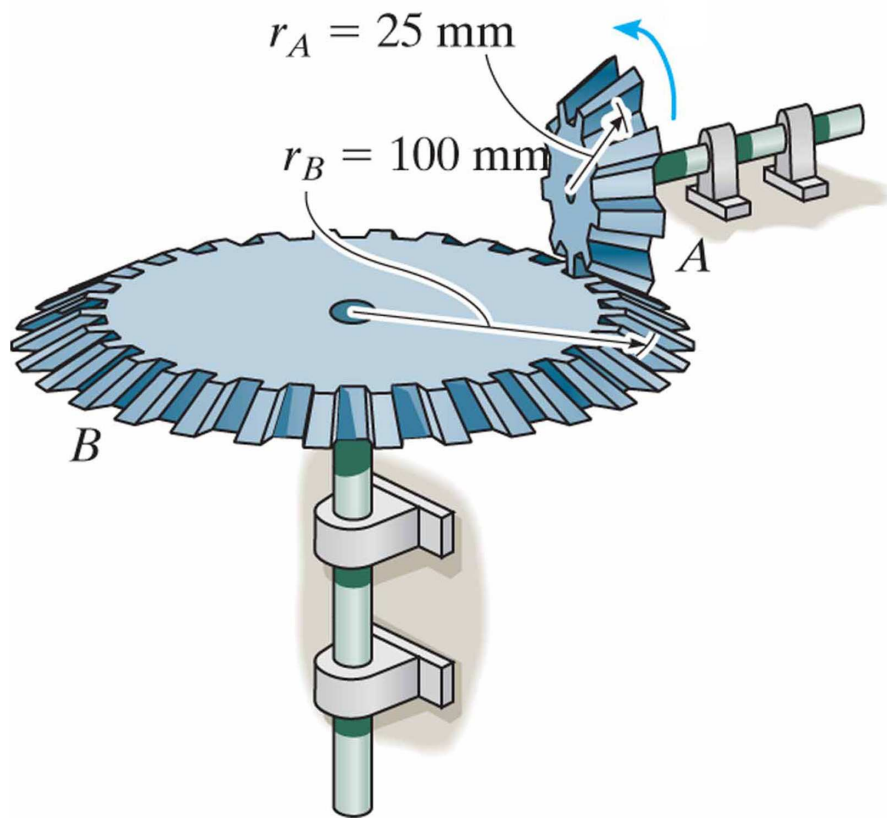
Homework Assignment #9 - Due Friday, April 12.

Mastering Physics: 7 problems from chapter 9

Written Question: 10.80

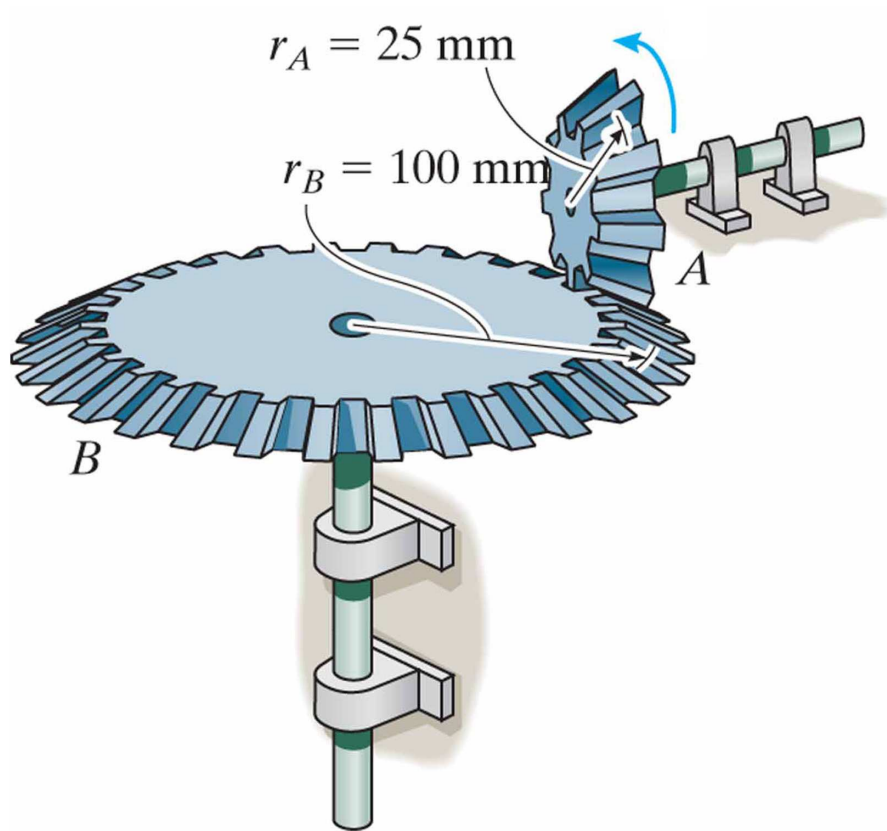
Connected Objects Example

With what angular velocity must gear A rotate if we wish gear B to rotate at 100 RPM ?



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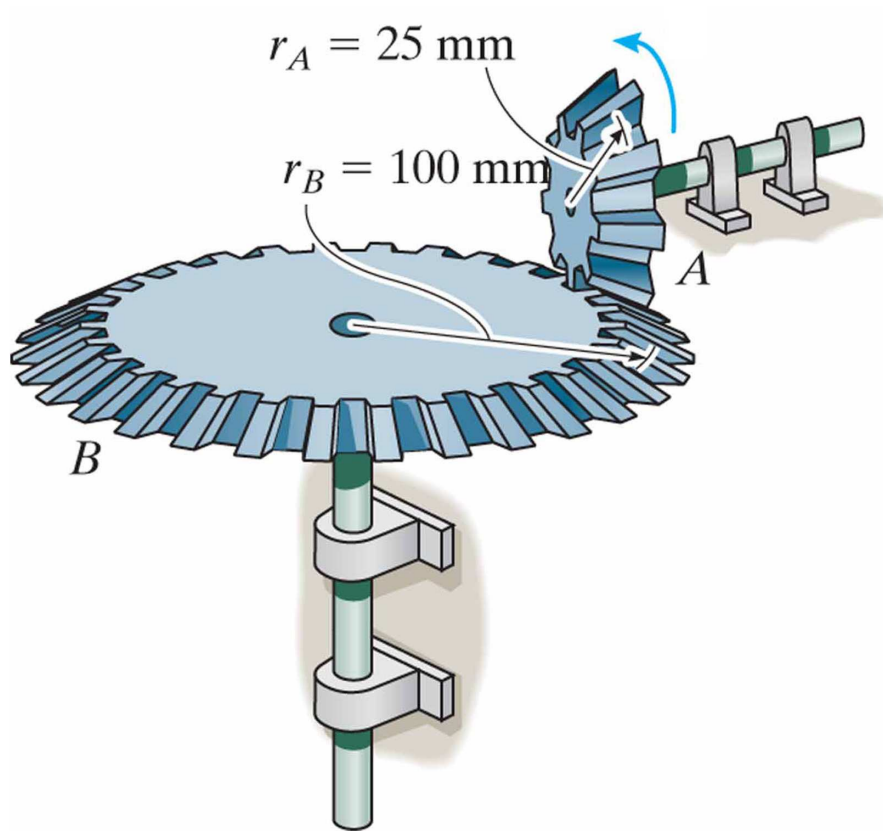
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(a) 25 RPM

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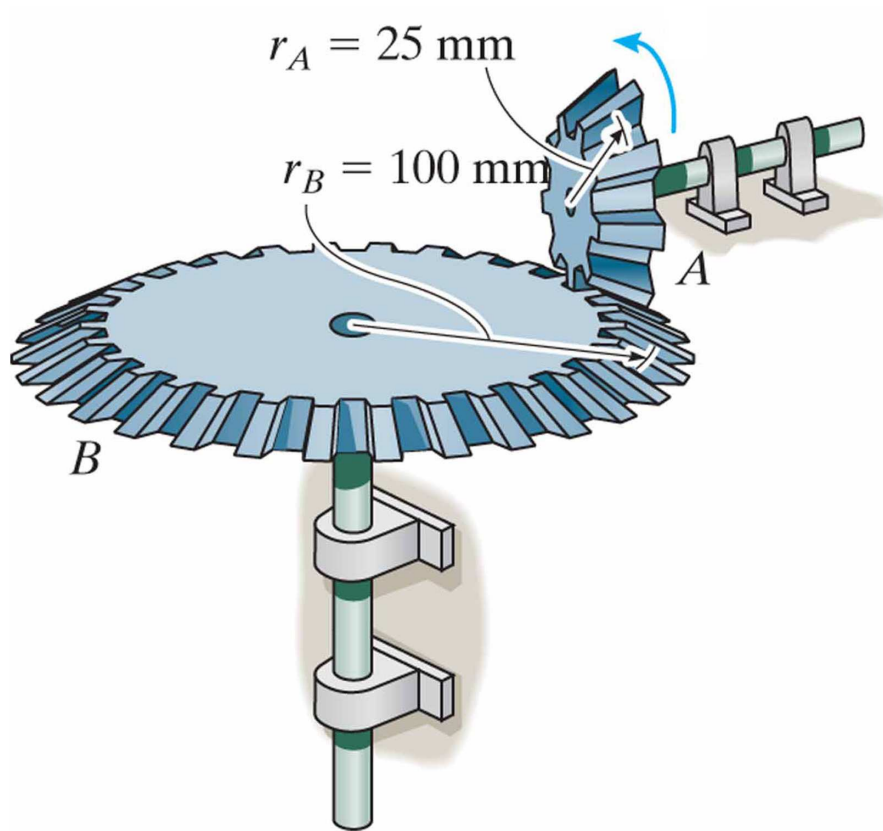


(a) 25 RPM

(b) 50 RPM

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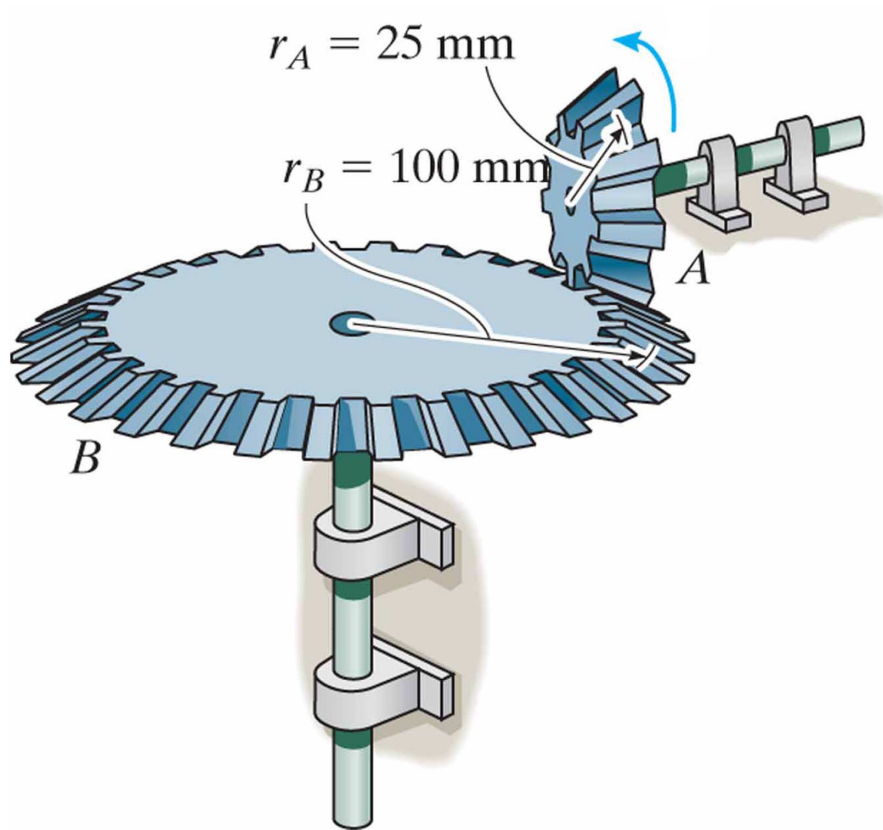
(a) 25 RPM

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(c) 100 RPM

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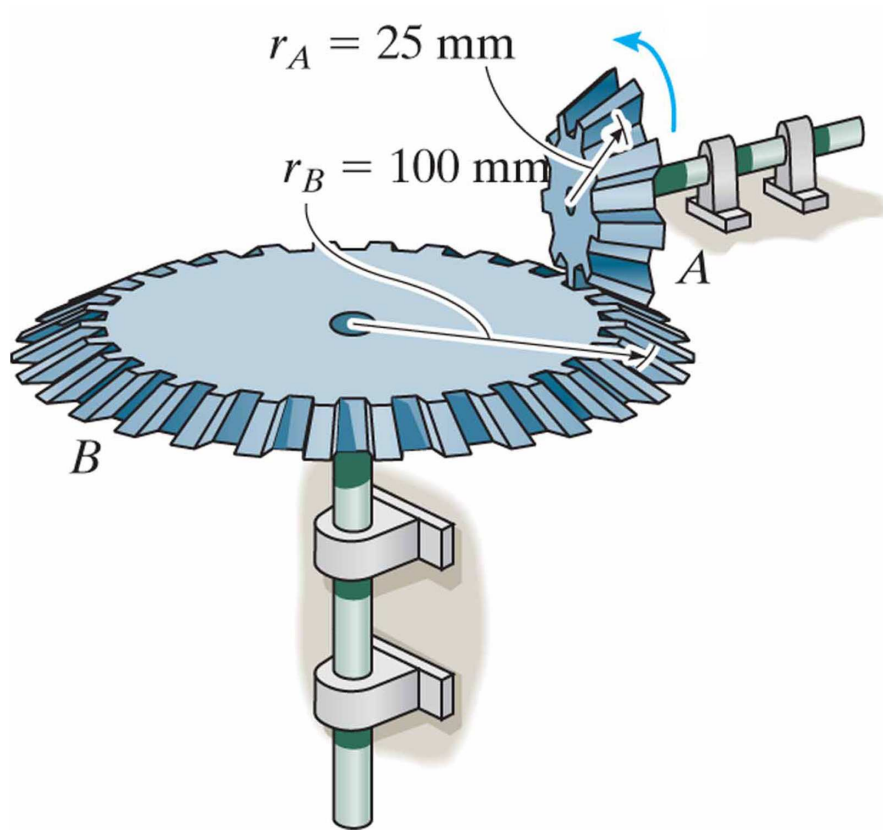
(b) 50 RPM

(c) 100 RPM

(d) 200 RPM

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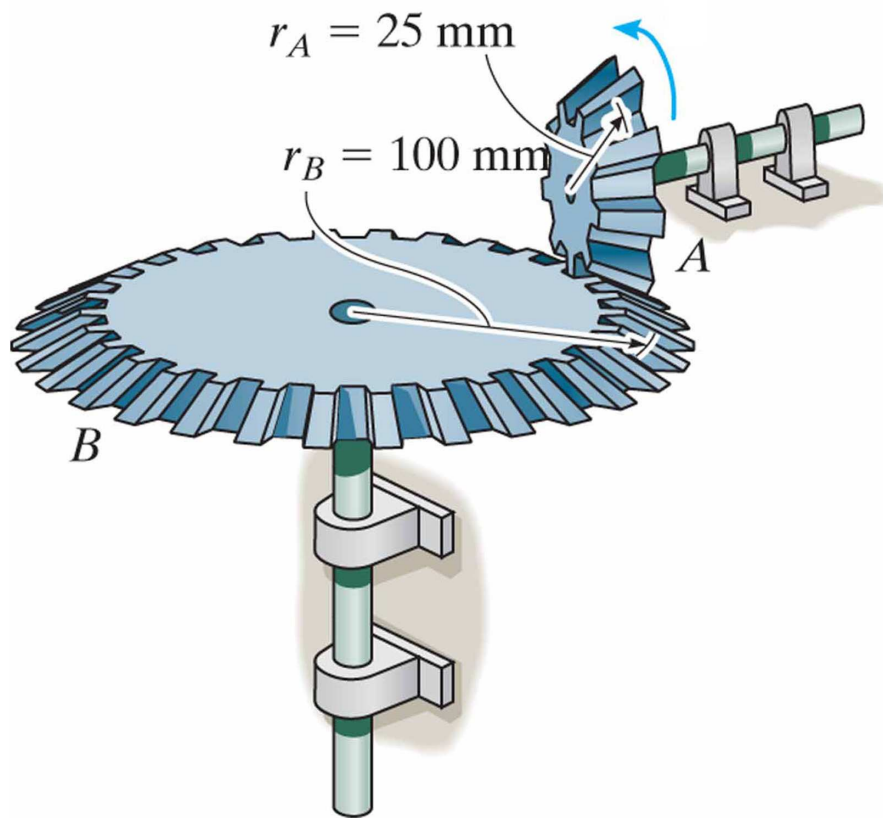
(c) 100 RPM

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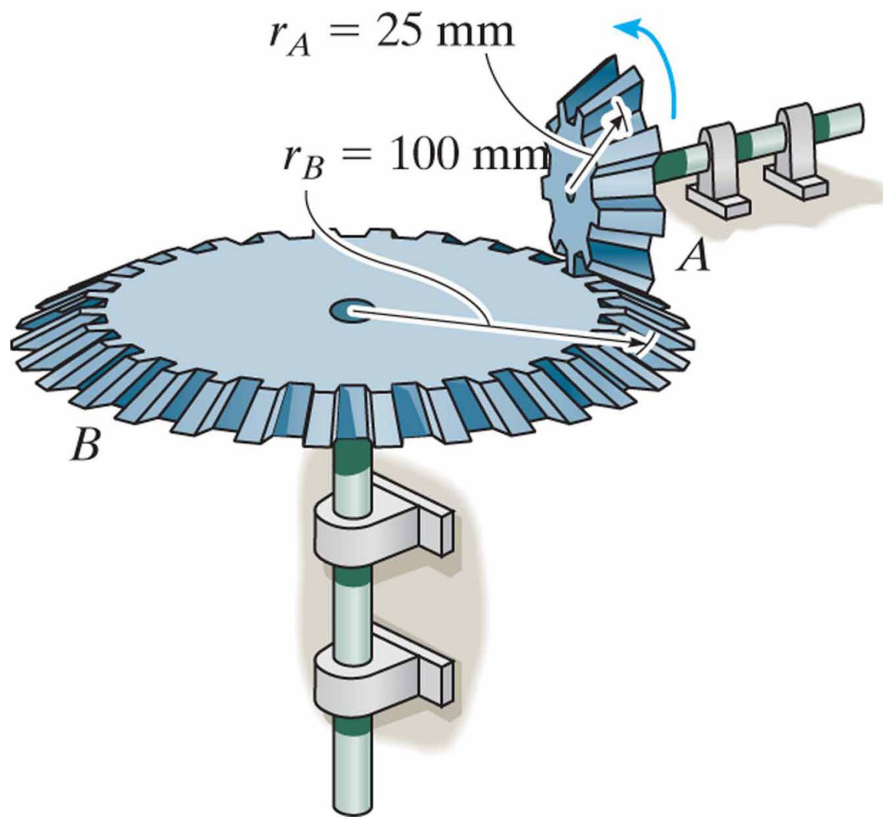
(c) 100 RPM

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We can use any units in this equation as long as they are the same

$$r_1\omega_1 = r_2\omega_2 \Rightarrow$$

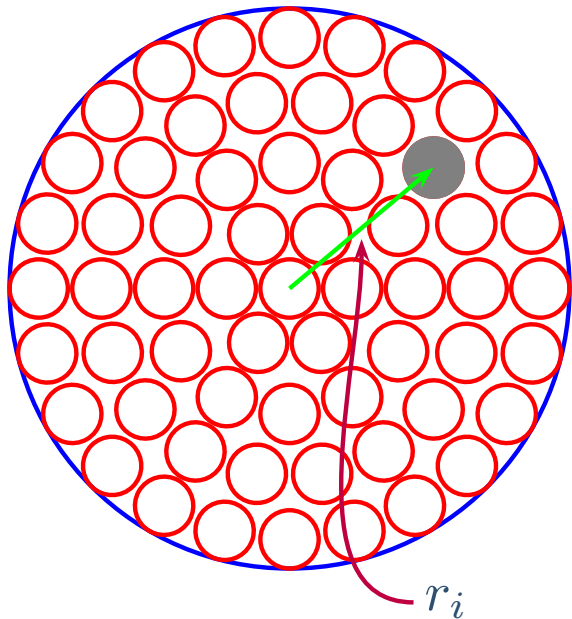
$$\omega_1 = \frac{(100 \text{ mm})(100 \text{ RPM})}{25 \text{ mm}}$$

(e) 400 RPM

Rotational Kinetic Energy II

Any rotating object has a kinetic energy due to its motion.

We have to imagine splitting the rotating object up into many small pieces.



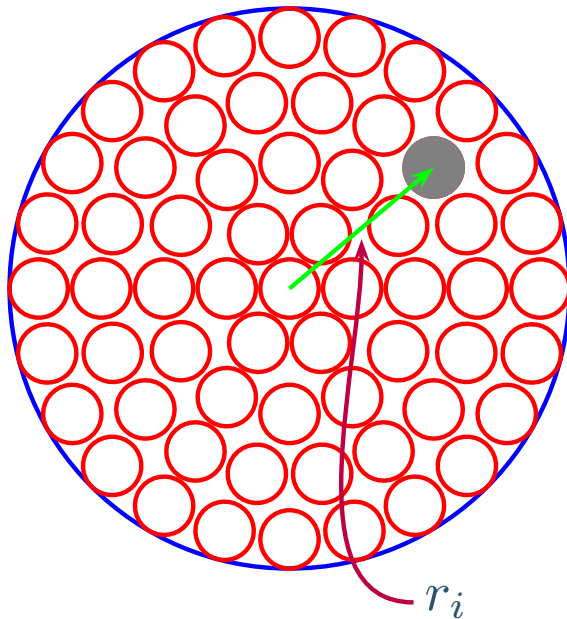
$$K \approx \frac{1}{2} \left(\sum_i M_i r_i^2 \right) \omega^2$$

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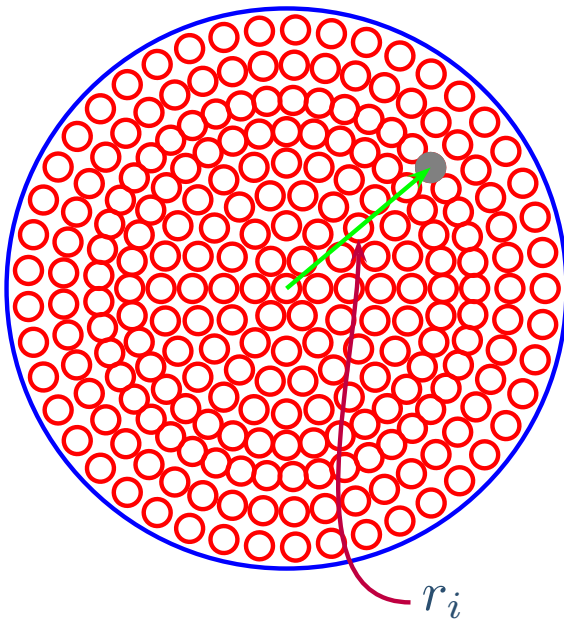
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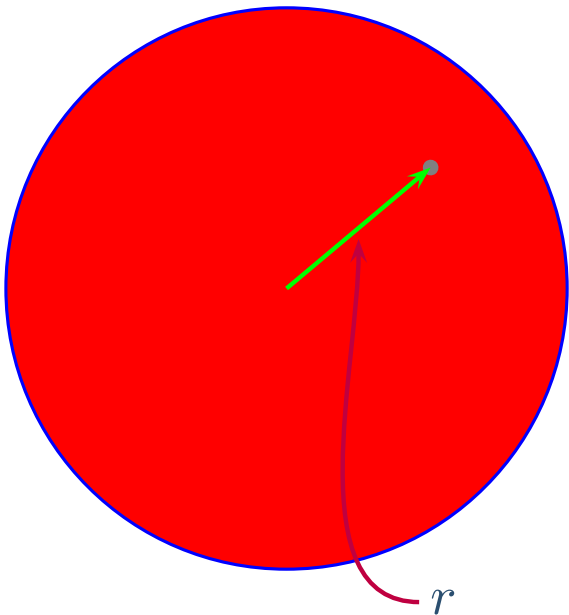
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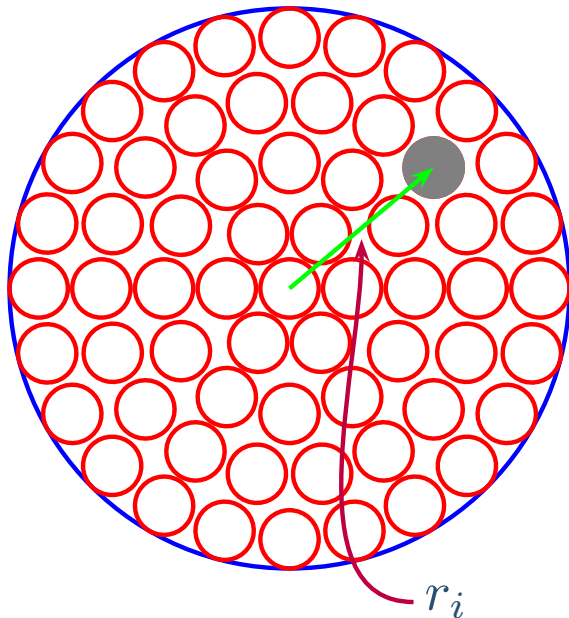
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Moment of Inertia

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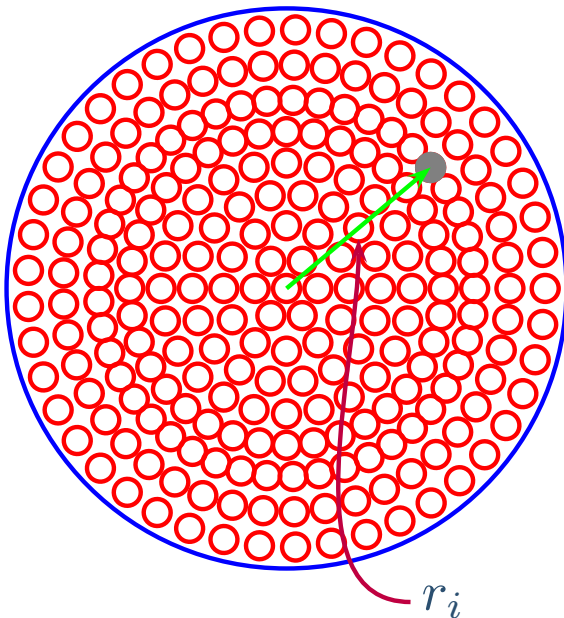


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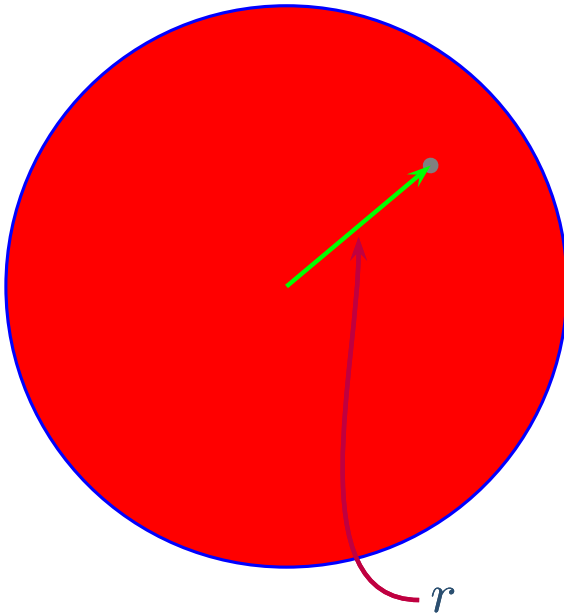
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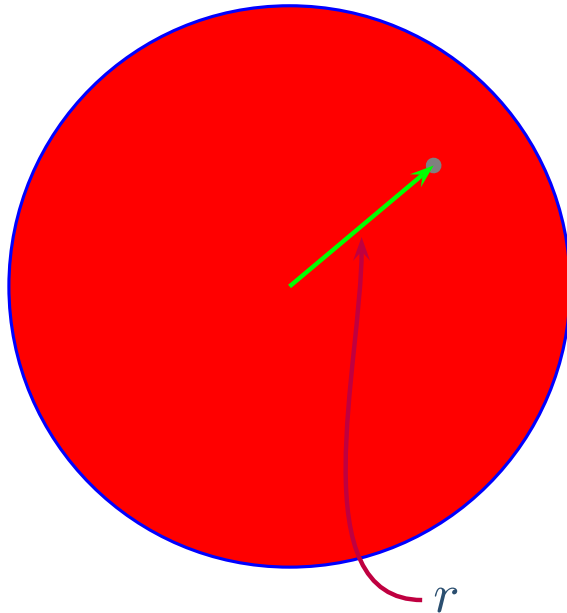
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$$I = \int r^2 dM = \int r^2 \rho dV$$

(ρ = density, V = volume)

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- (a) The object’s shape.

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The moment of inertia depends on:

- (a) The object’s shape.
- (b) The axis of rotation.
- (c) The total mass of the object.

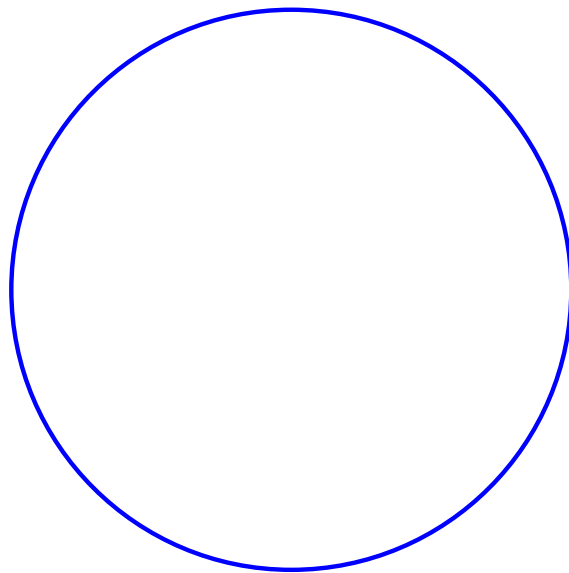
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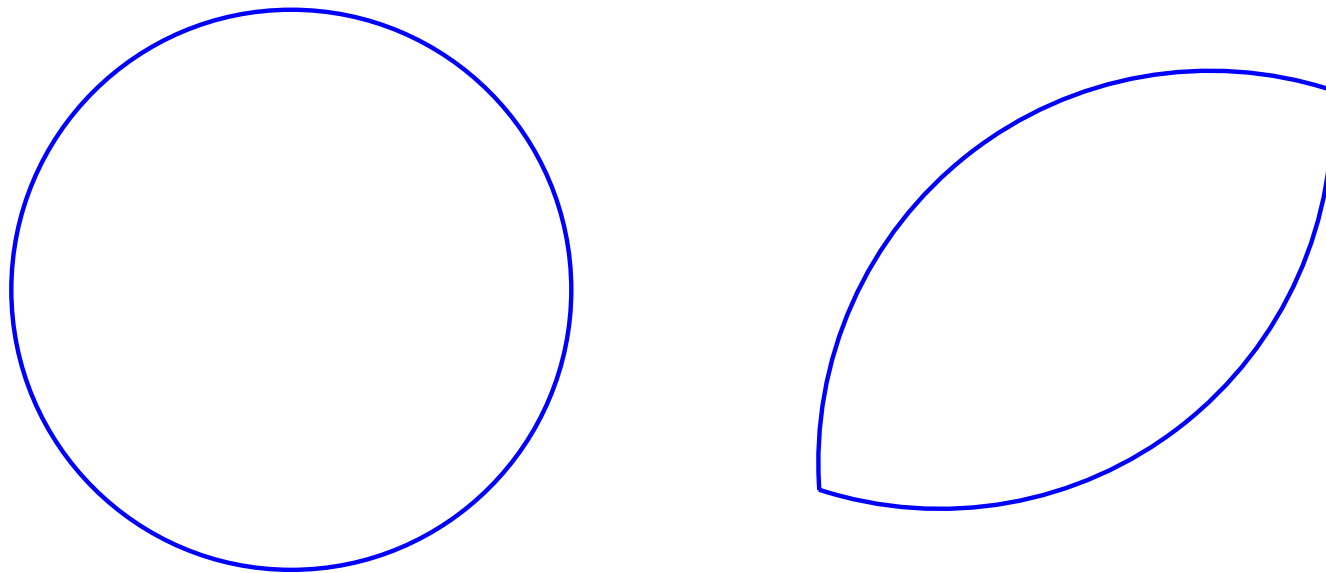
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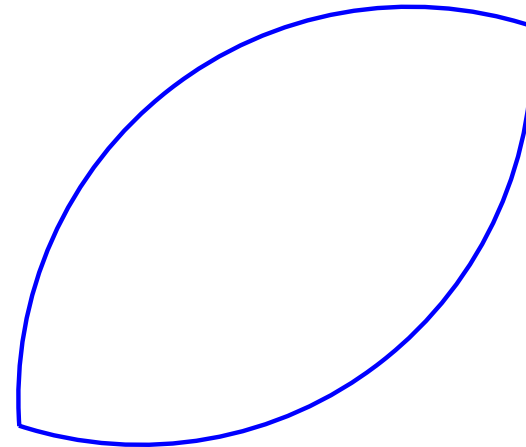
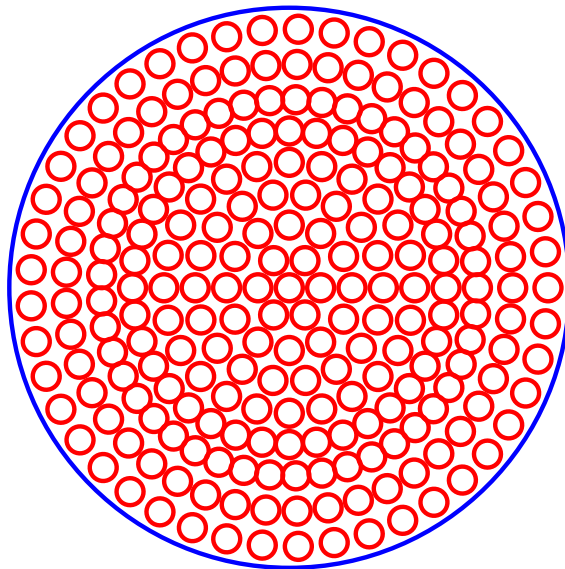
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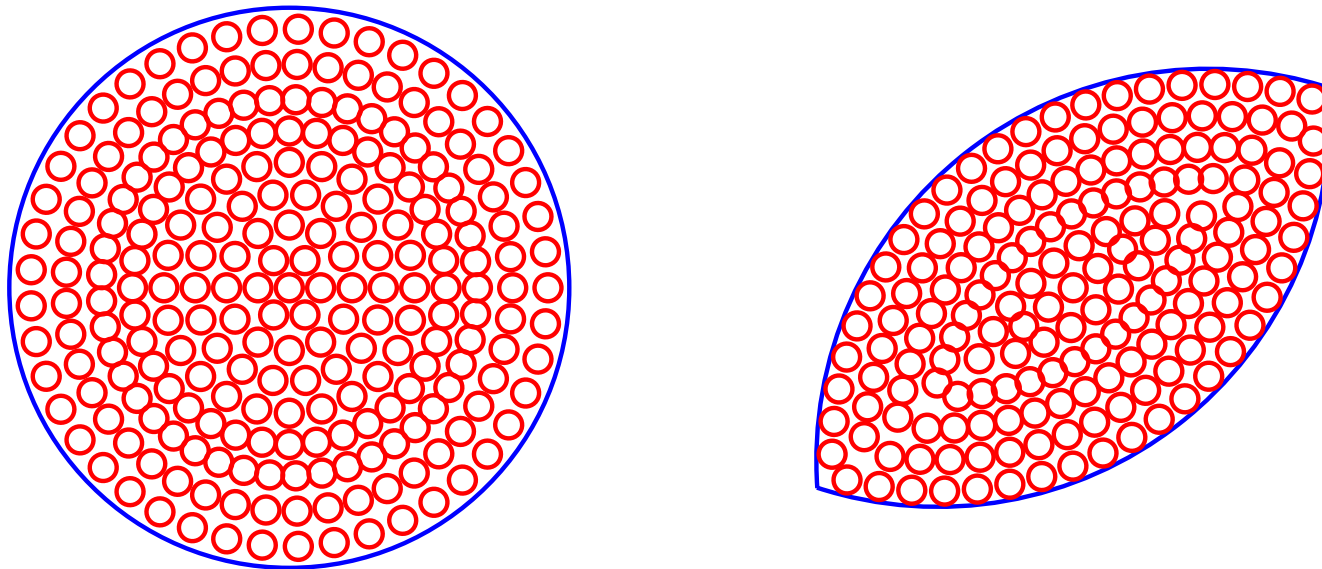
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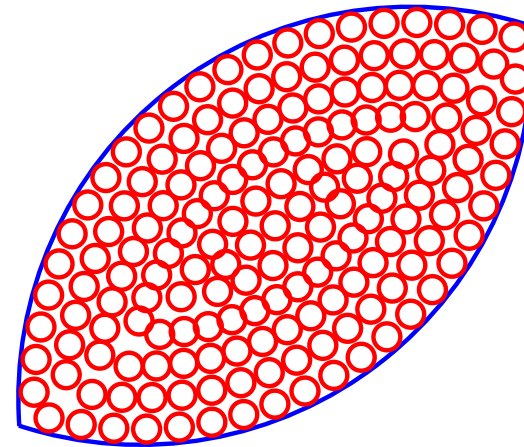
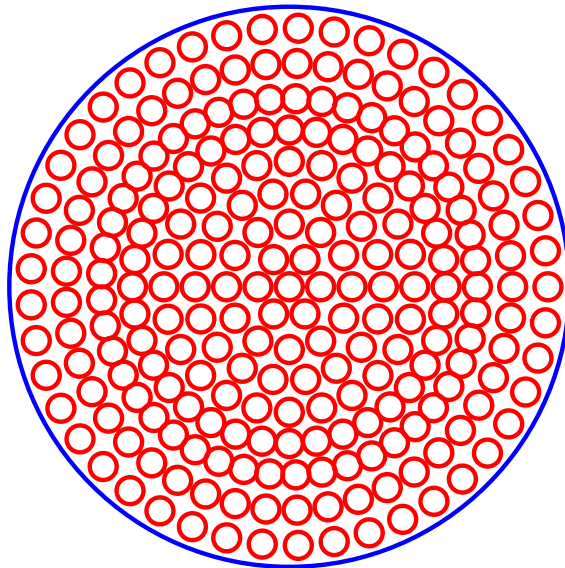


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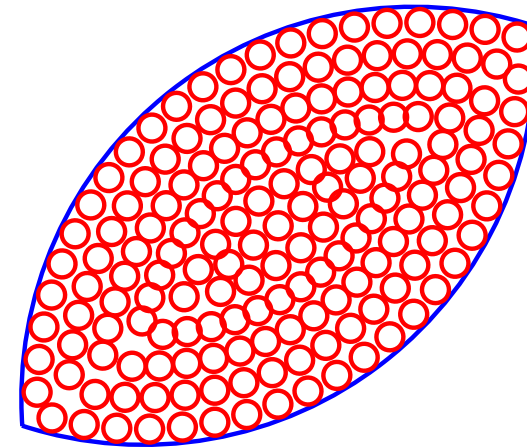
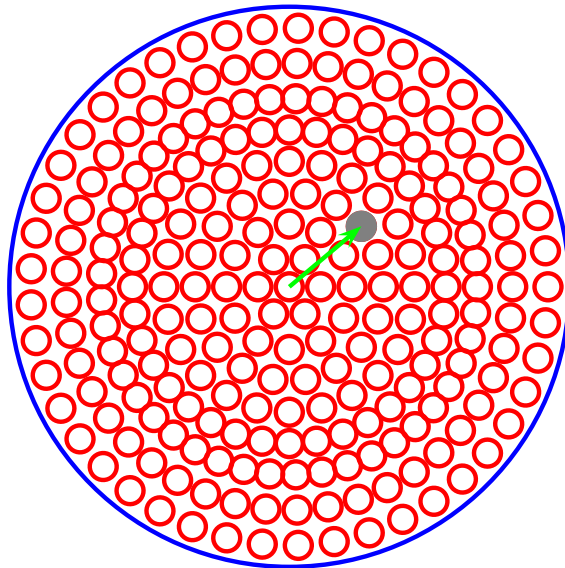
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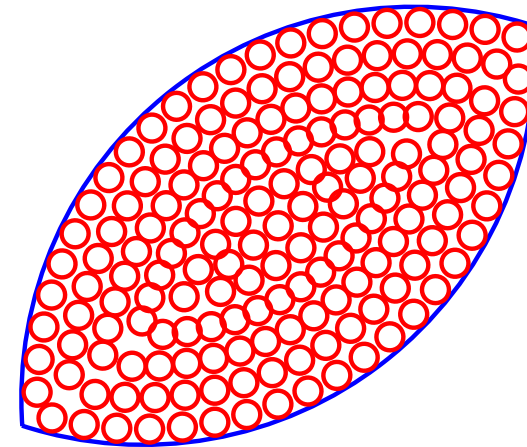
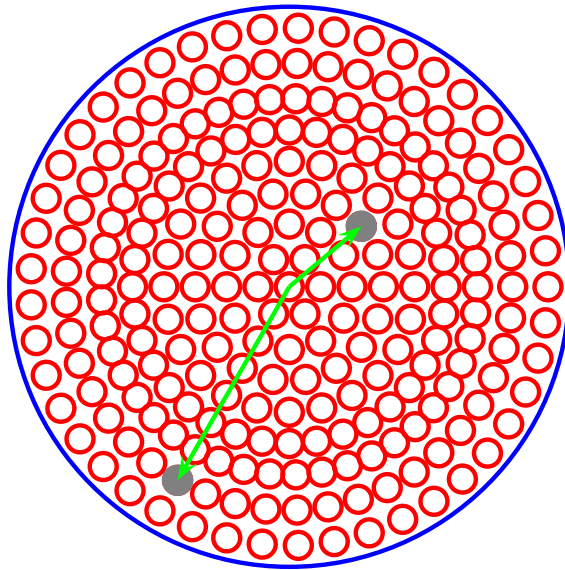
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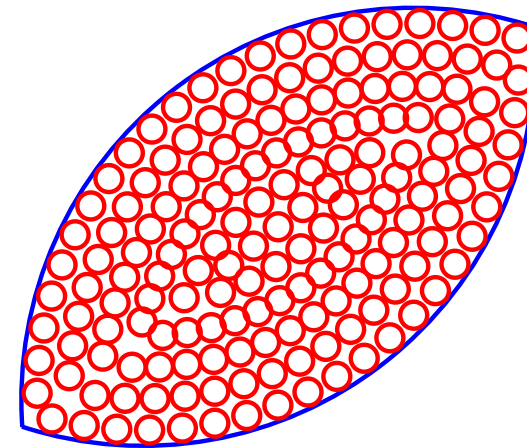
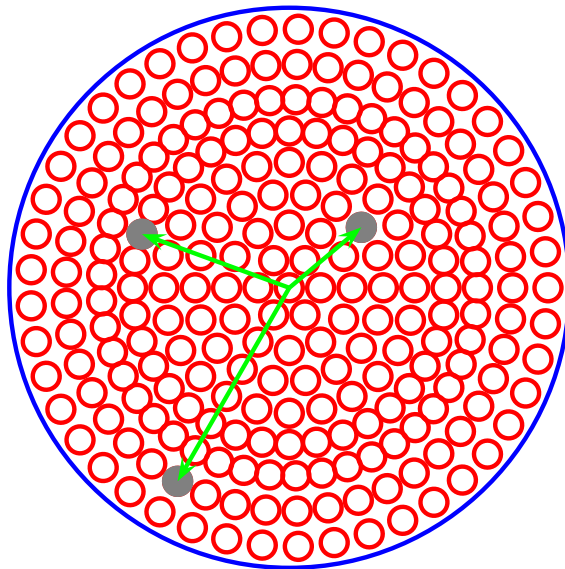
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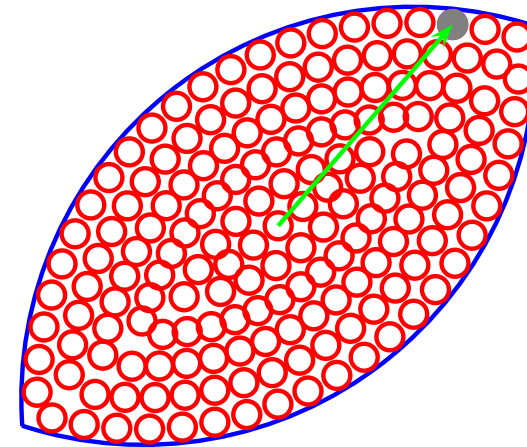
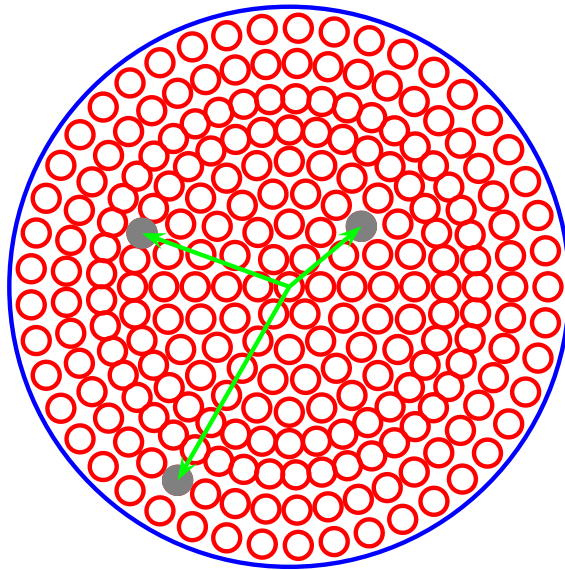
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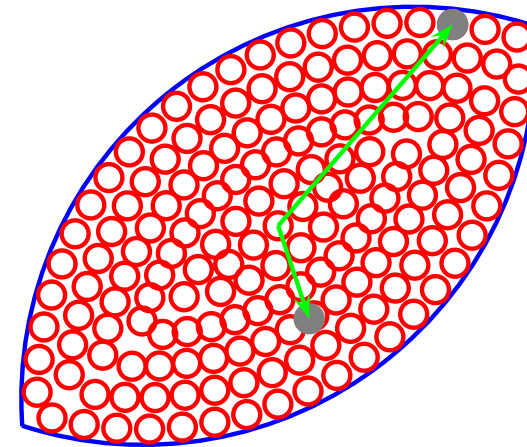
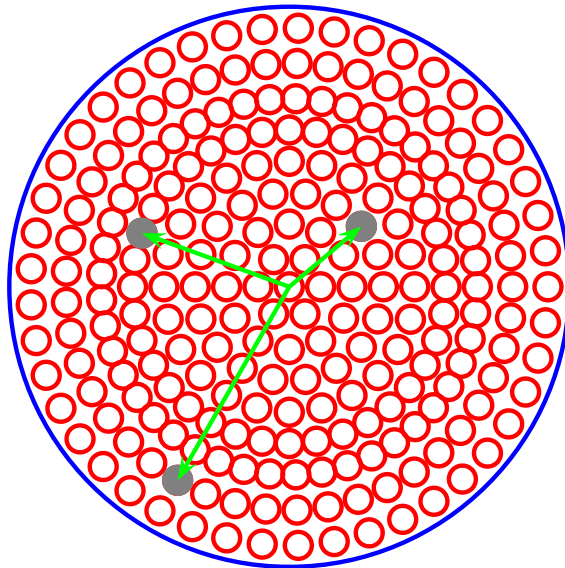
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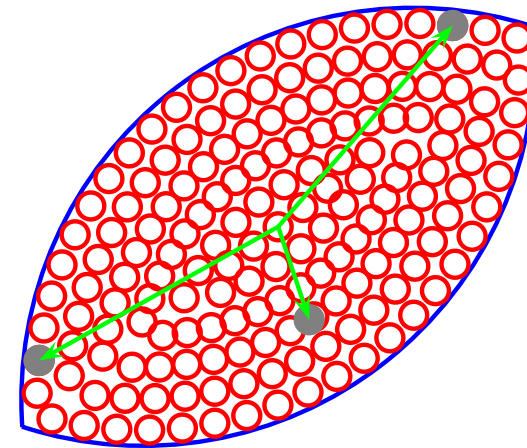
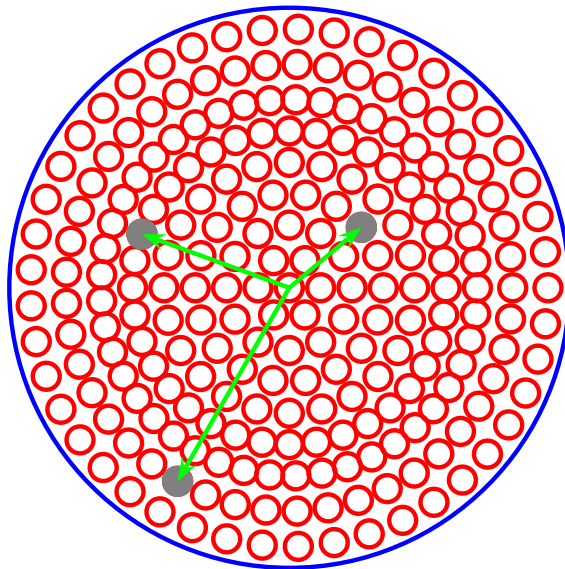
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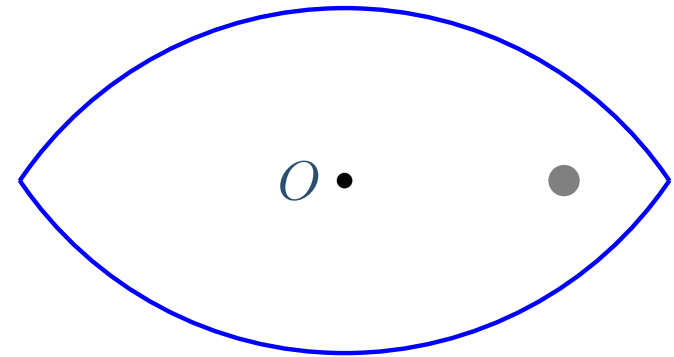
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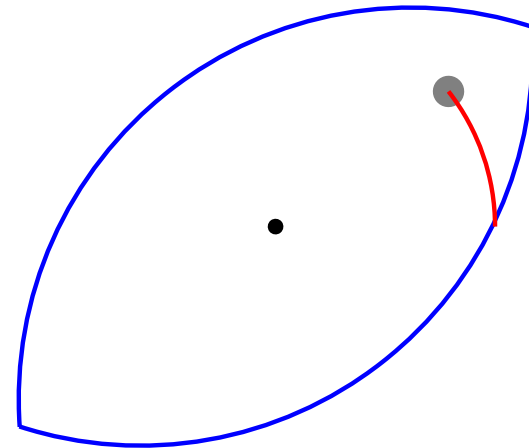
Rotation about the Center:



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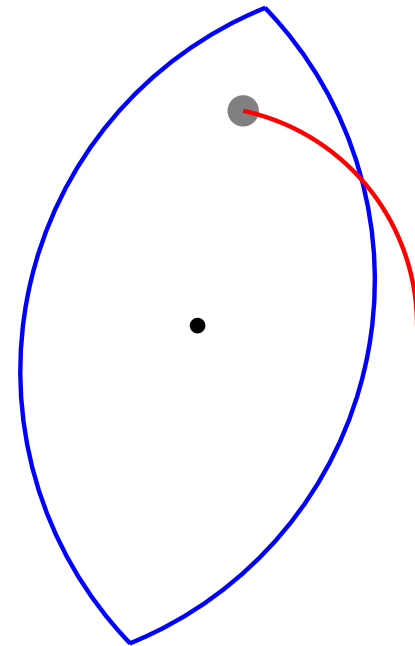
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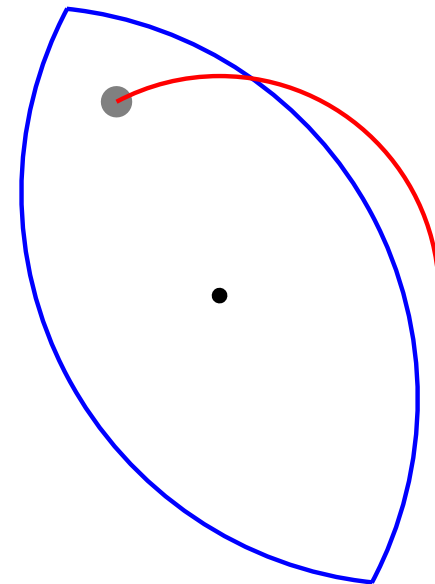
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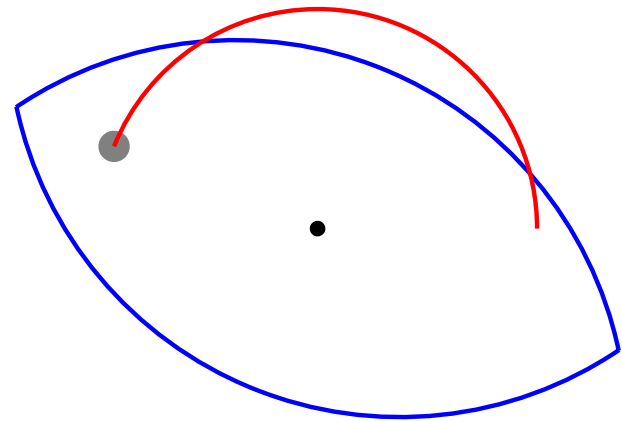
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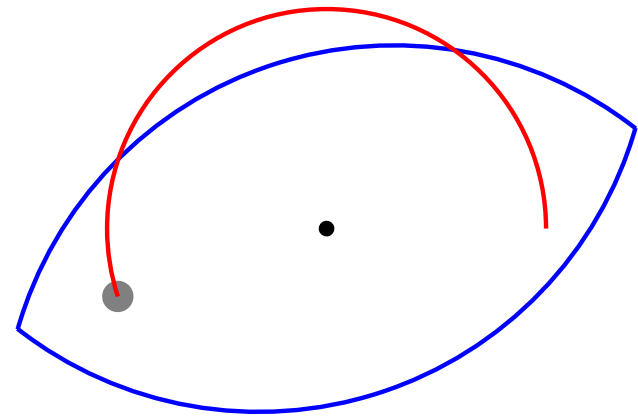
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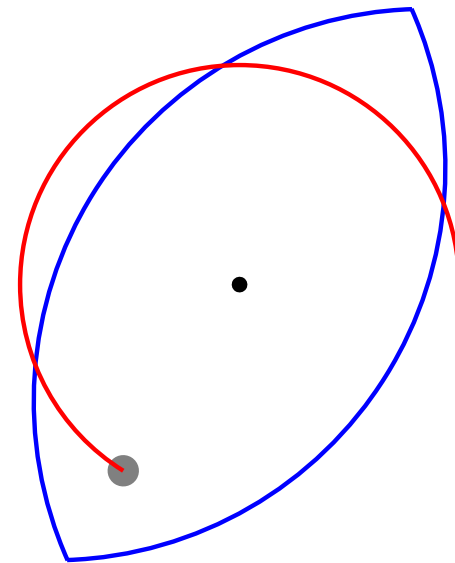
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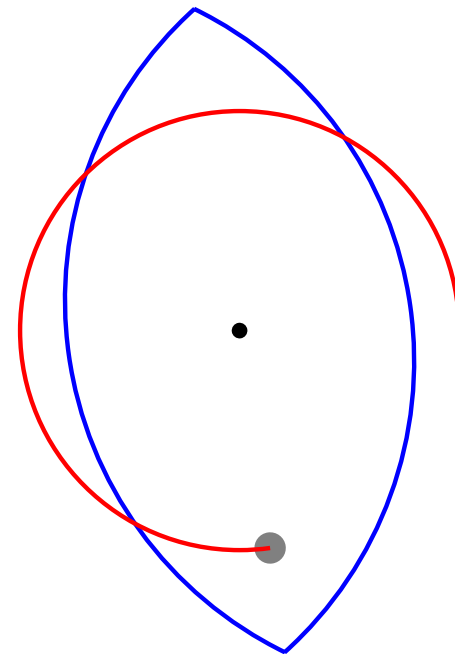
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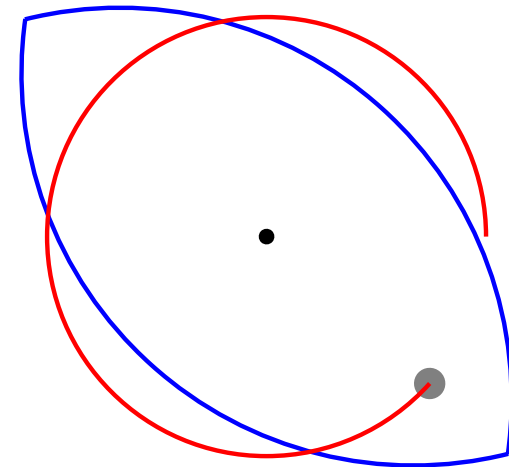
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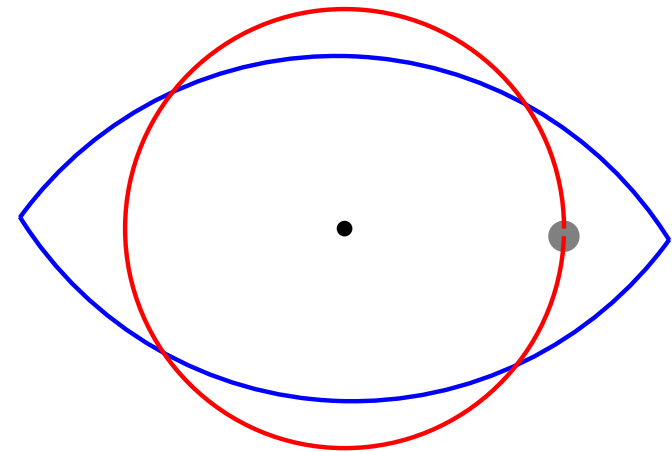
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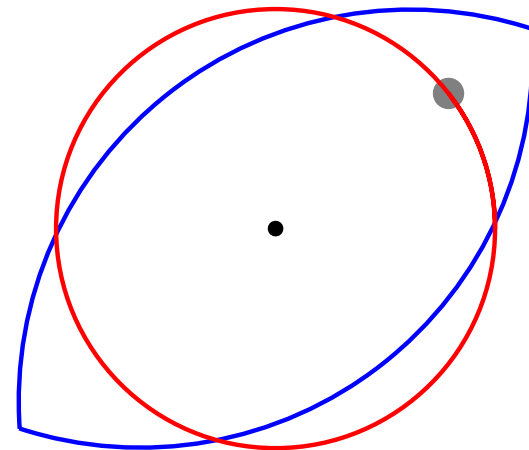
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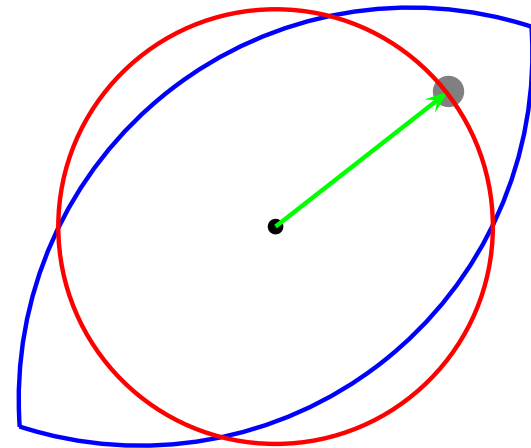
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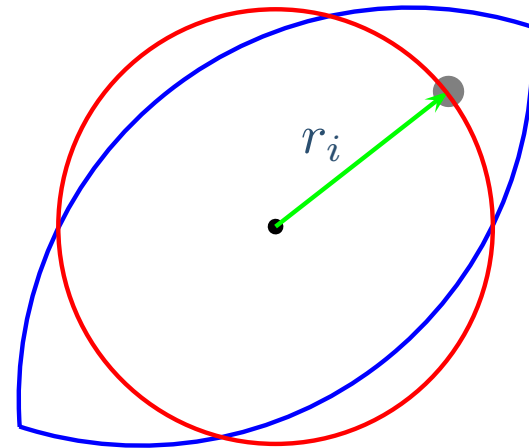


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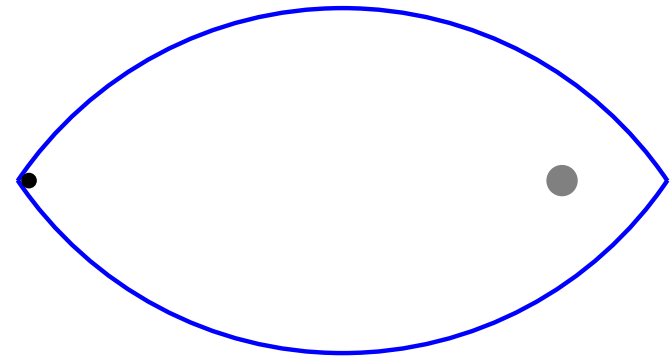


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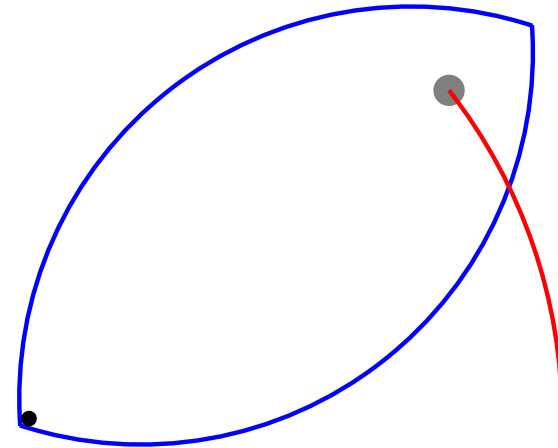


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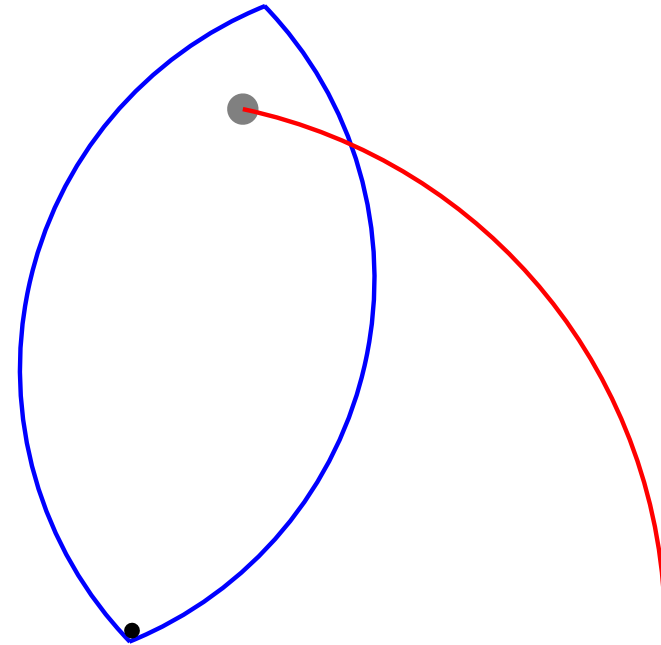


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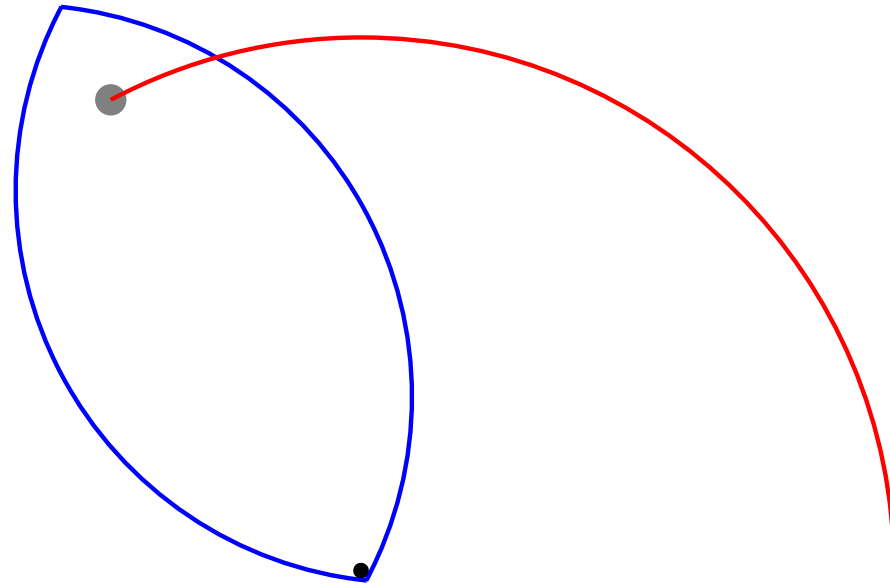


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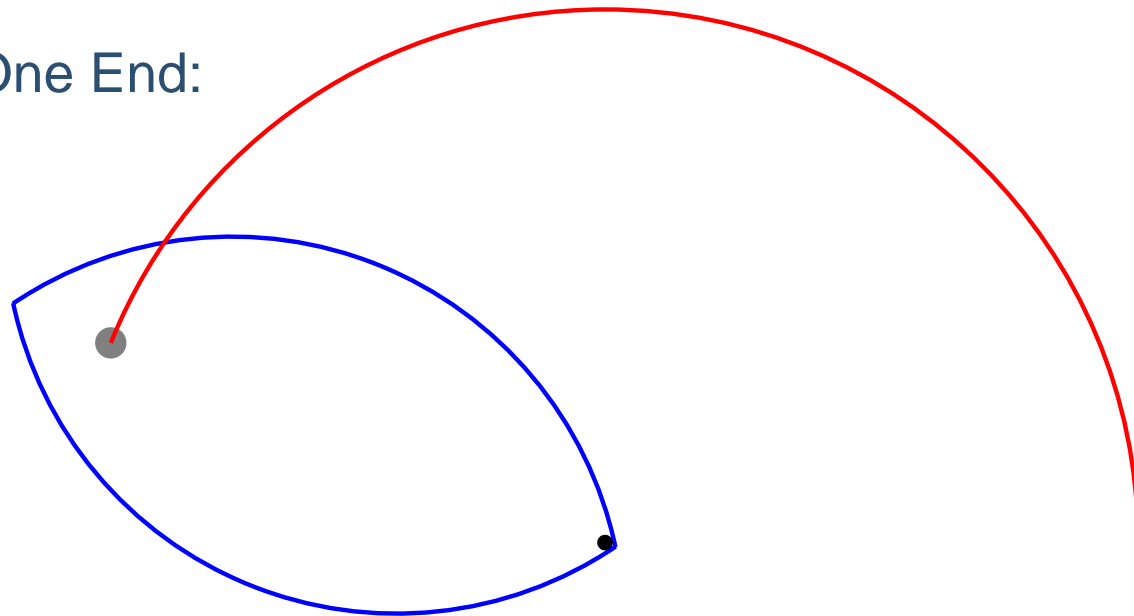


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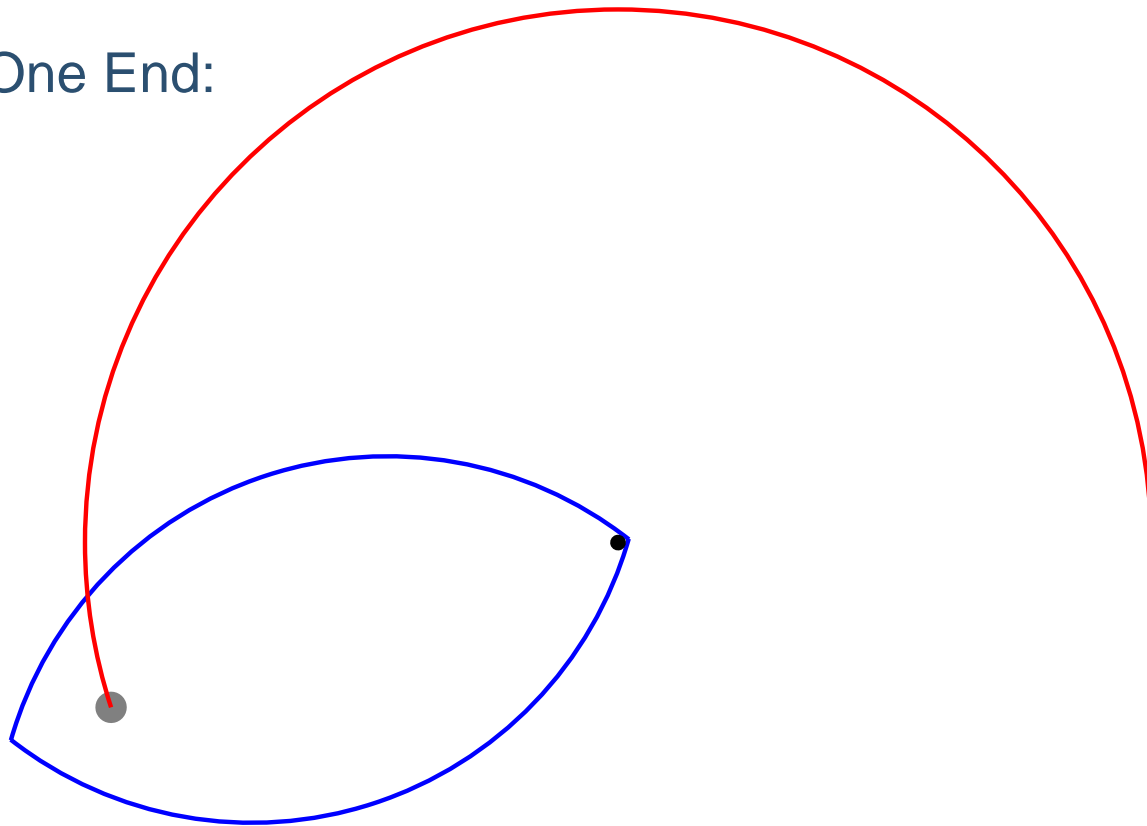


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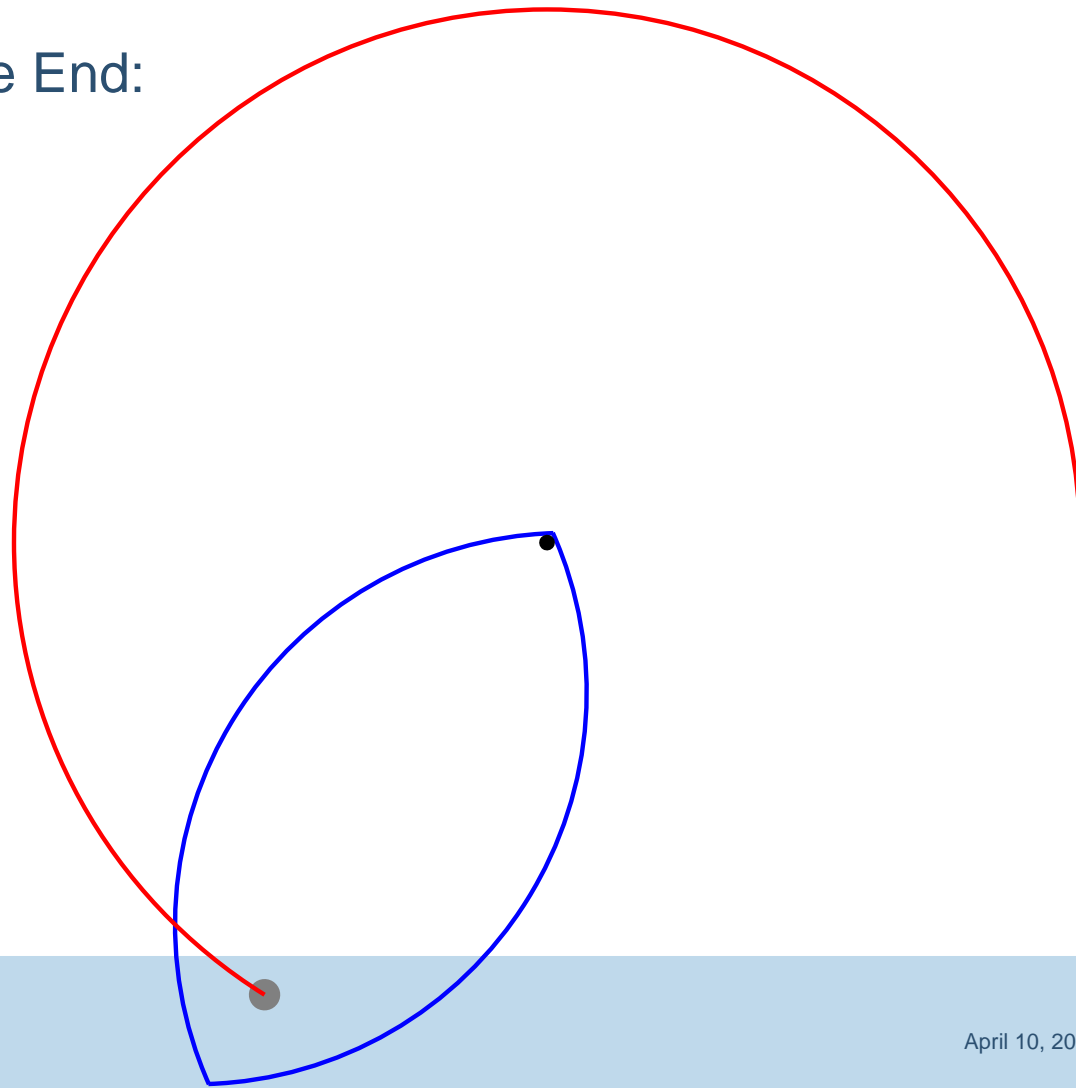


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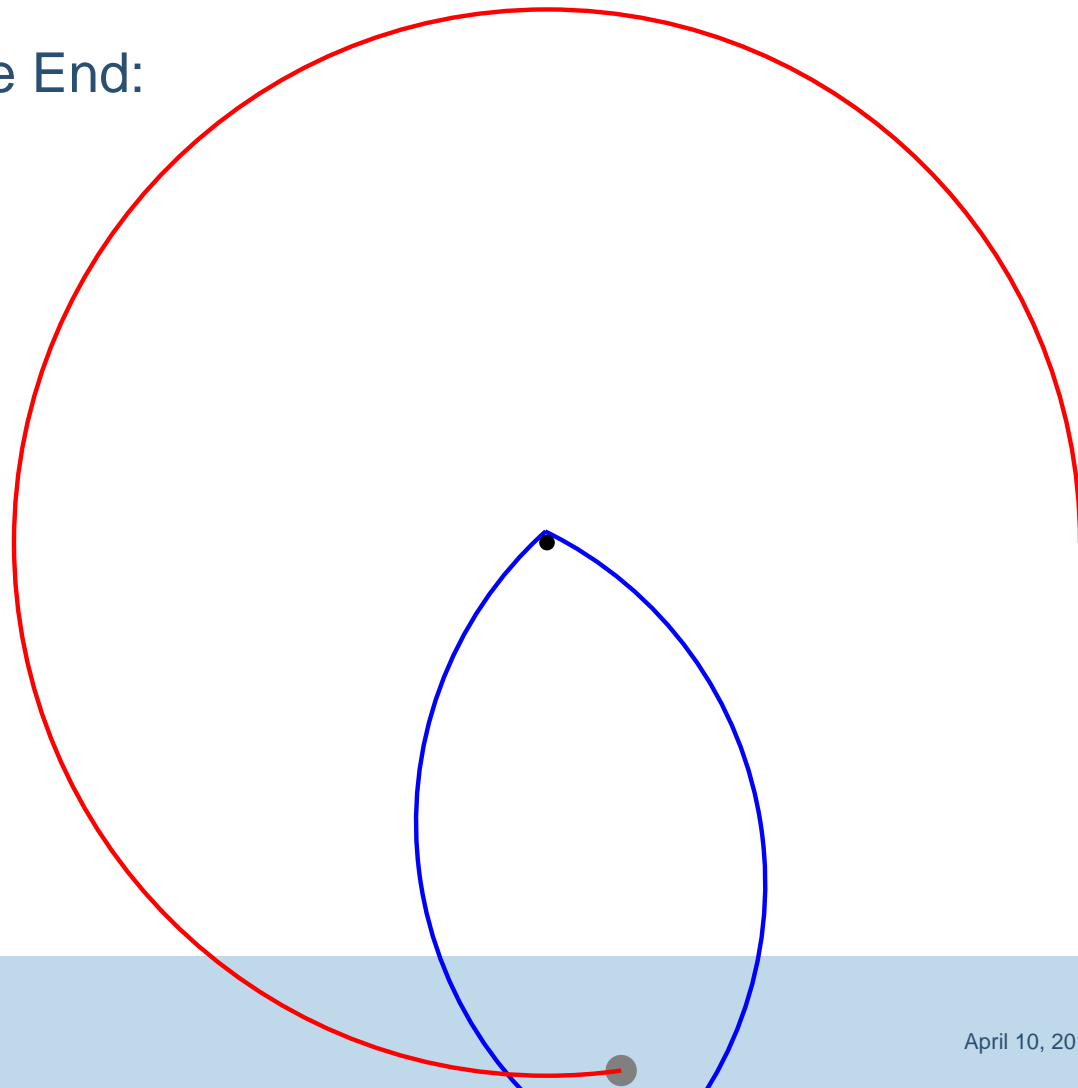


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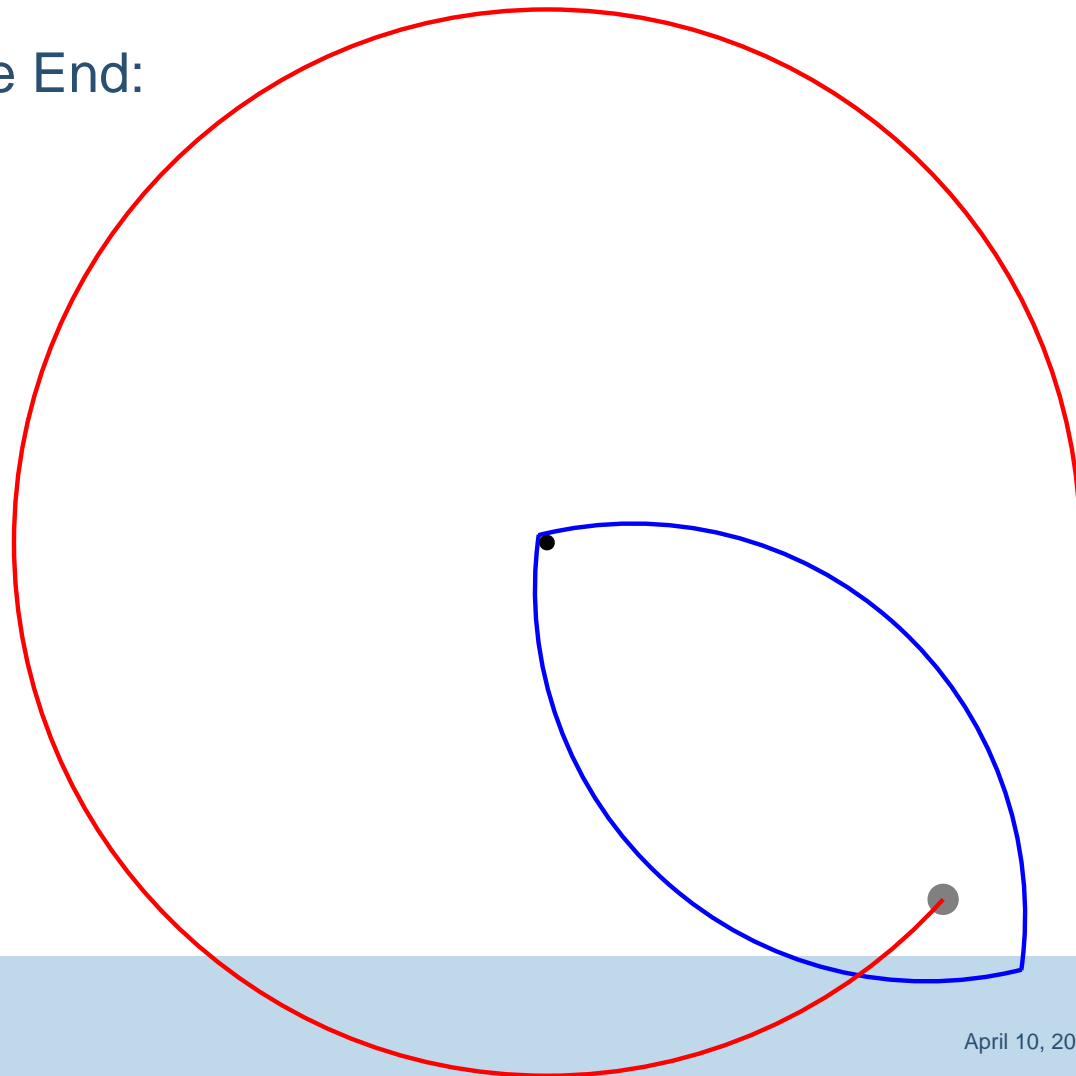


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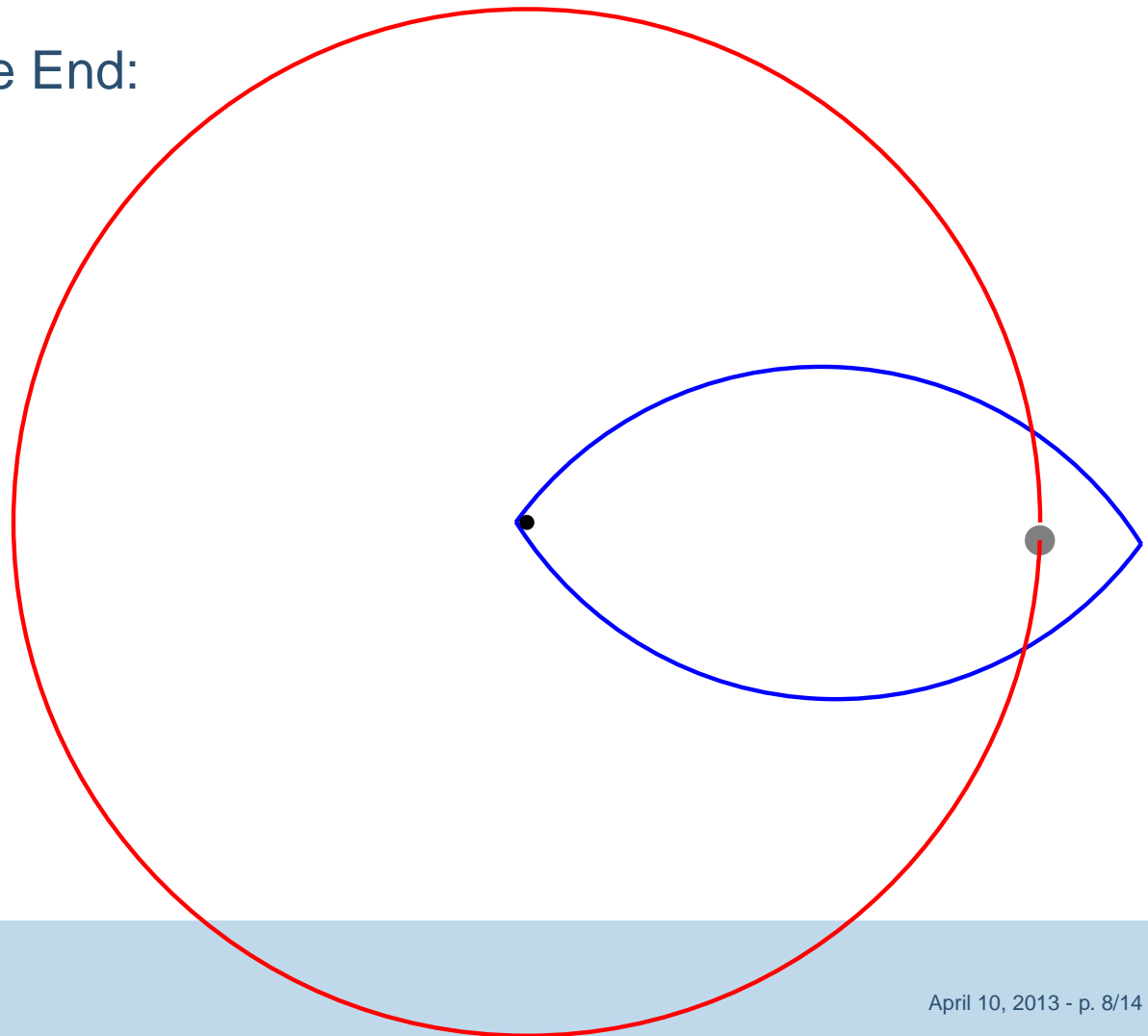


Axis of Rotation

A single object has many different moments of inertia.

Rotation about One End:

$$I = \sum_i m_i r_i^2$$

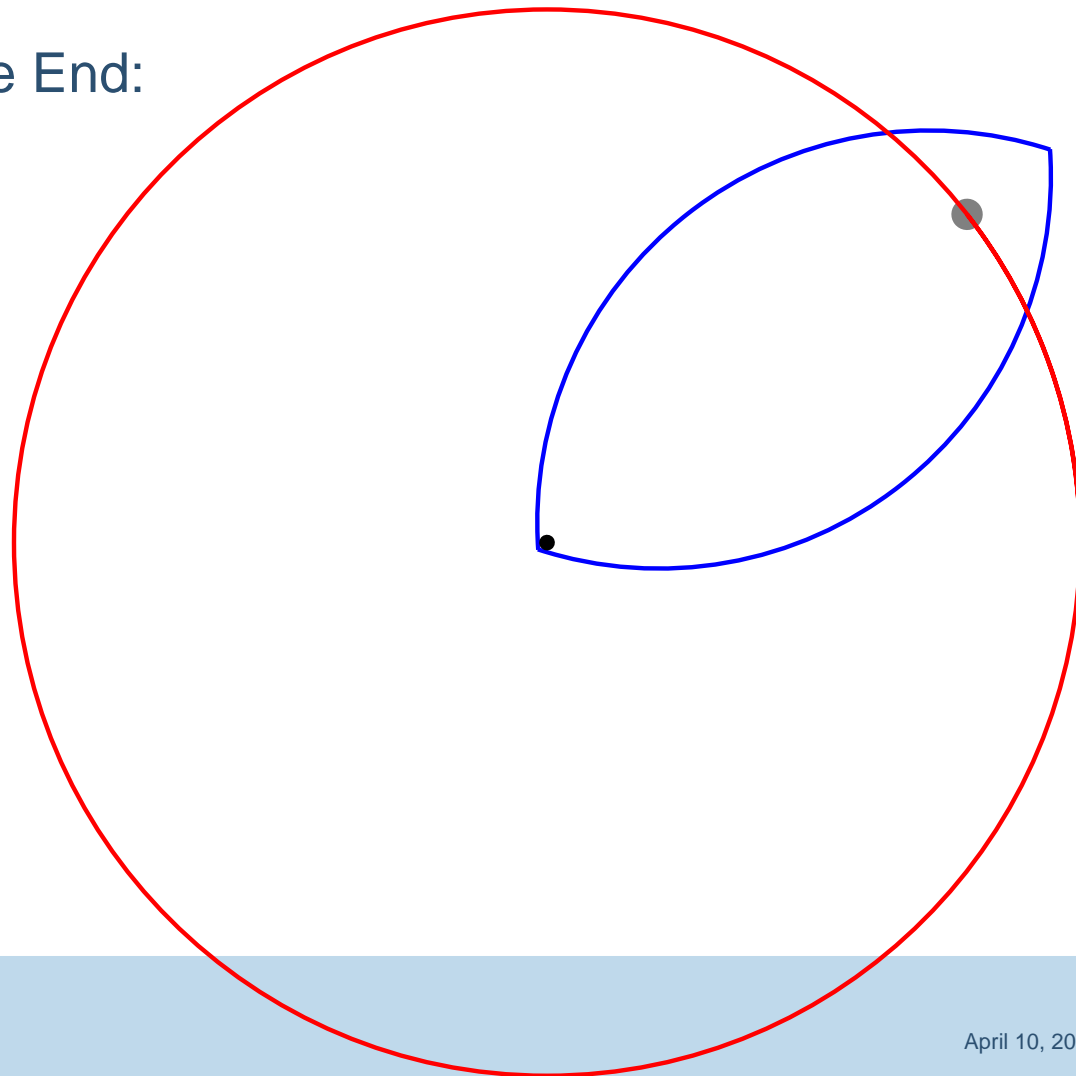


Axis of Rotation

A single object has many different moments of inertia.

Rotation about One End:

$$I = \sum_i m_i r_i^2$$

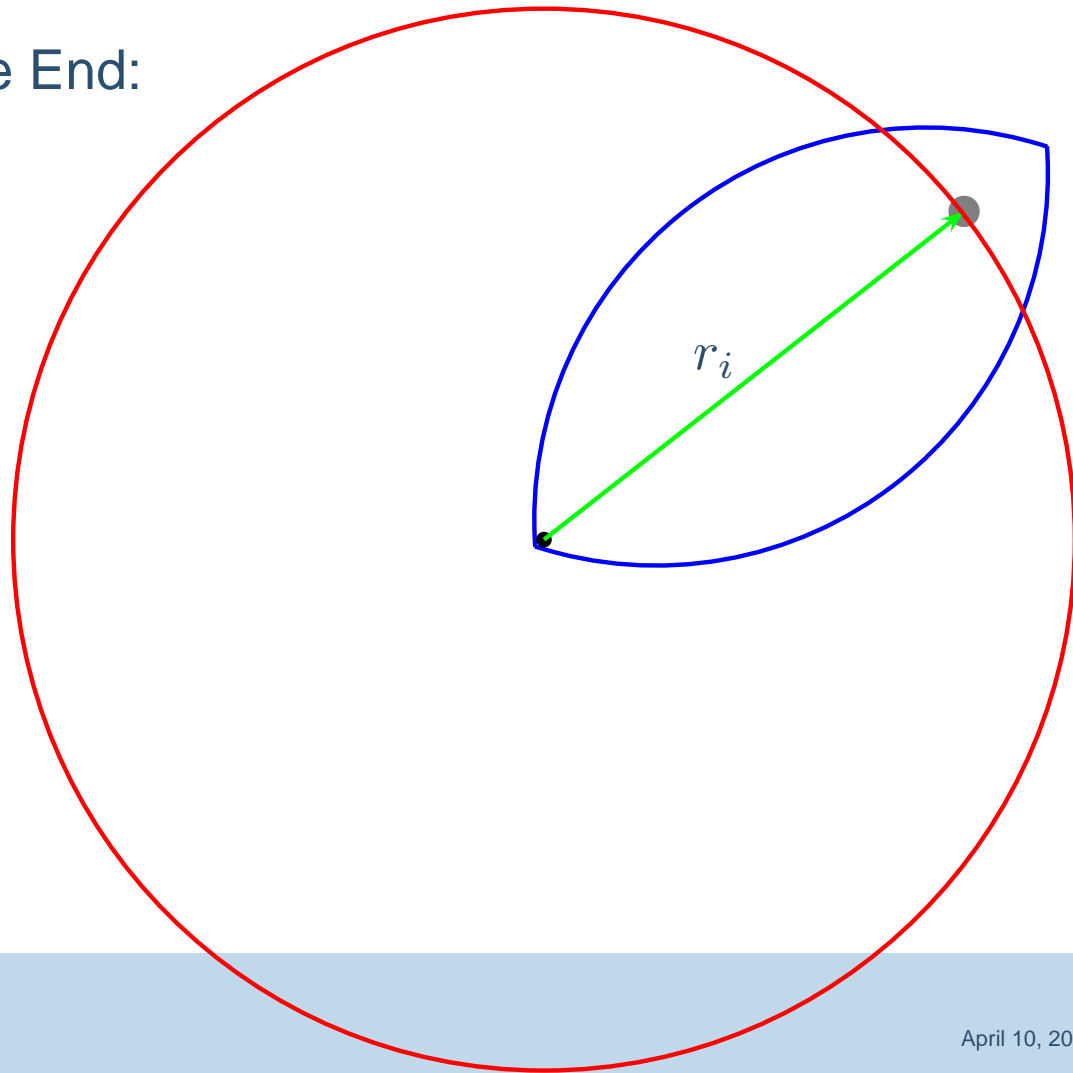


Axis of Rotation

A single object has many different moments of inertia.

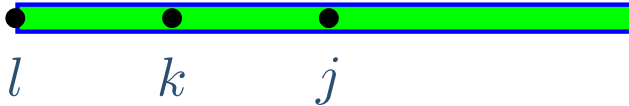
Rotation about One End:

$$I = \sum_i m_i r_i^2$$



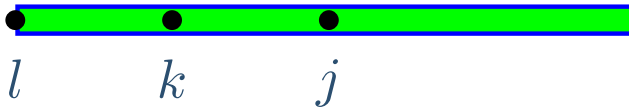
Moment of Inertia Exercise

For the rectangular stick shown, the moment of inertia for rotation about the center is I_j , the moment of inertia for rotation about the point $1/4$ of the length is I_k , and the moment of inertia for rotation about the end is I_l . Which of the following is the correct listing of moments of inertia from largest to smallest?



Moment of Inertia Exercise

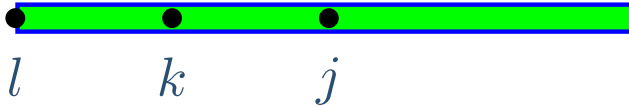
For the rectangular stick shown, the moment of inertia for rotation about the center is I_j , the moment of inertia for rotation about the point $1/4$ of the length is I_k , and the moment of inertia for rotation about the end is I_l . Which of the following is the correct listing of moments of inertia from largest to smallest?



(a) I_j, I_k, I_l

Moment of Inertia Exercise

For the rectangular stick shown, the moment of inertia for rotation about the center is I_j , the moment of inertia for rotation about the point $1/4$ of the length is I_k , and the moment of inertia for rotation about the end is I_l . Which of the following is the correct listing of moments of inertia from largest to smallest?

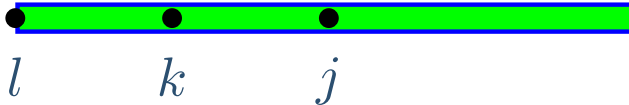


(a) I_j, I_k, I_l

(b) I_j, I_l, I_k

Moment of Inertia Exercise

For the rectangular stick shown, the moment of inertia for rotation about the center is I_j , the moment of inertia for rotation about the point $1/4$ of the length is I_k , and the moment of inertia for rotation about the end is I_l . Which of the following is the correct listing of moments of inertia from largest to smallest?



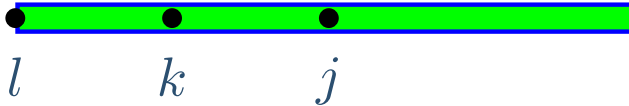
(a) I_j, I_k, I_l

(b) I_j, I_l, I_k

(c) I_l, I_j, I_k

Moment of Inertia Exercise

For the rectangular stick shown, the moment of inertia for rotation about the center is I_j , the moment of inertia for rotation about the point $1/4$ of the length is I_k , and the moment of inertia for rotation about the end is I_l . Which of the following is the correct listing of moments of inertia from largest to smallest?



(a) I_j, I_k, I_l

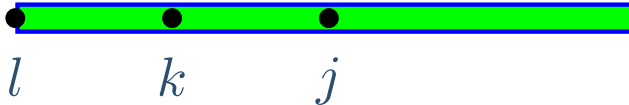
(b) I_j, I_l, I_k

(c) I_l, I_j, I_k

(d) I_l, I_k, I_j

Moment of Inertia Exercise

For the rectangular stick shown, the moment of inertia for rotation about the center is I_j , the moment of inertia for rotation about the point $1/4$ of the length is I_k , and the moment of inertia for rotation about the end is I_l . Which of the following is the correct listing of moments of inertia from largest to smallest?



(a) I_j, I_k, I_l

(b) I_j, I_l, I_k

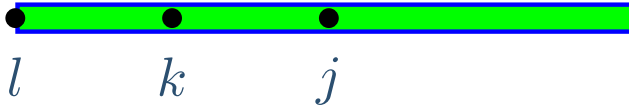
(c) I_l, I_j, I_k

(d) I_l, I_k, I_j

(e) $I_j = I_k = I_l$

Moment of Inertia Exercise

For the rectangular stick shown, the moment of inertia for rotation about the center is I_j , the moment of inertia for rotation about the point $1/4$ of the length is I_k , and the moment of inertia for rotation about the end is I_l . Which of the following is the correct listing of moments of inertia from largest to smallest?



(a) I_j, I_k, I_l

(b) I_j, I_l, I_k

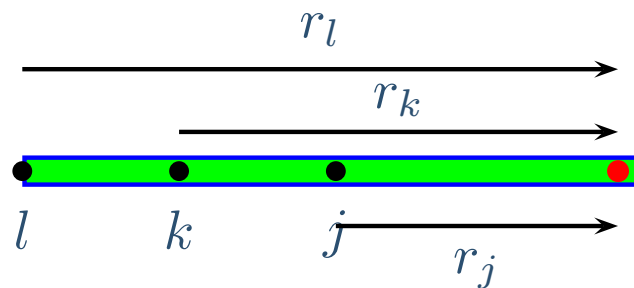
(c) I_l, I_j, I_k

(d) I_l, I_k, I_j

(e) $I_j = I_k = I_l$

Moment of Inertia Exercise

For the rectangular stick shown, the moment of inertia for rotation about the center is I_j , the moment of inertia for rotation about the point $1/4$ of the length is I_k , and the moment of inertia for rotation about the end is I_l . Which of the following is the correct listing of moments of inertia from largest to smallest?



(d) I_l, I_k, I_j

Standard Shapes

For standard shapes and axes, equations for moments of inertia have already been calculated.

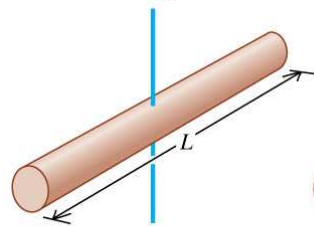
Standard Shapes

For standard shapes and axes, equations for moments of inertia have already been calculated.

Table 9.2 Moments of Inertia of Various Bodies

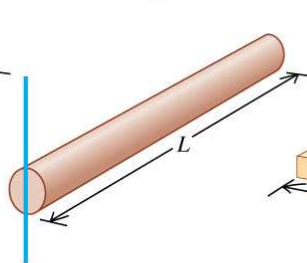
(a) Slender rod,
axis through center

$$I = \frac{1}{12}ML^2$$



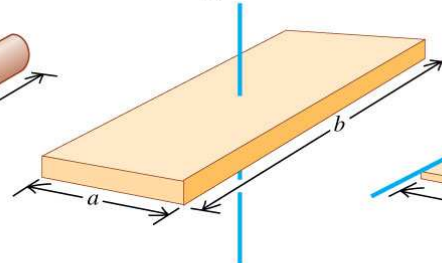
(b) Slender rod,
axis through one end

$$I = \frac{1}{3}ML^2$$



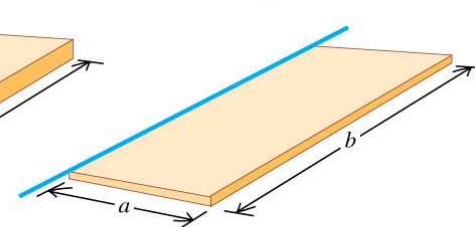
(c) Rectangular plate,
axis through center

$$I = \frac{1}{12}M(a^2 + b^2)$$



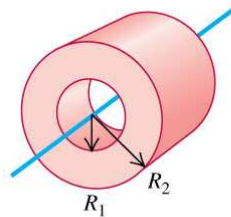
(d) Thin rectangular plate,
axis along edge

$$I = \frac{1}{3}Ma^2$$



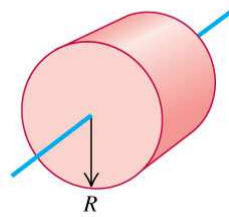
(e) Hollow cylinder

$$I = \frac{1}{2}M(R_1^2 + R_2^2)$$



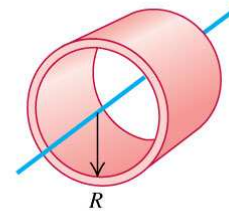
(f) Solid cylinder

$$I = \frac{1}{2}MR^2$$



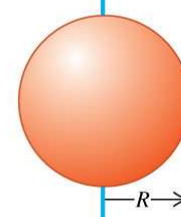
(g) Thin-walled hollow
cylinder

$$I = MR^2$$



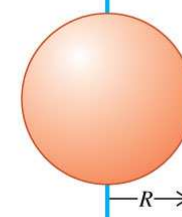
(h) Solid sphere

$$I = \frac{2}{5}MR^2$$



(i) Thin-walled hollow
sphere

$$I = \frac{2}{3}MR^2$$



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Gravitational Potential Energy

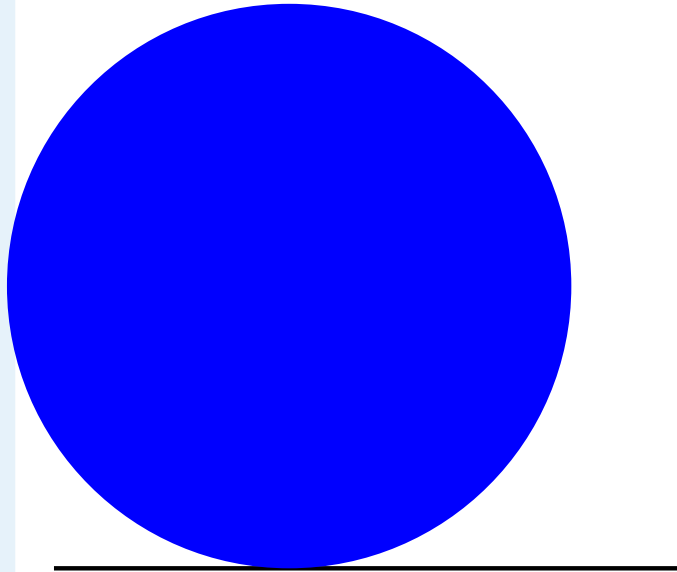
To find the gravitational potential energy of a rigid body, we use the center of gravity.

Center of Gravity - Position on an rigid body where the entirety of the weight seems to reside \Rightarrow the place we draw the weight.

Gravitational Potential Energy

To find the gravitational potential energy of a rigid body, we use the center of gravity.

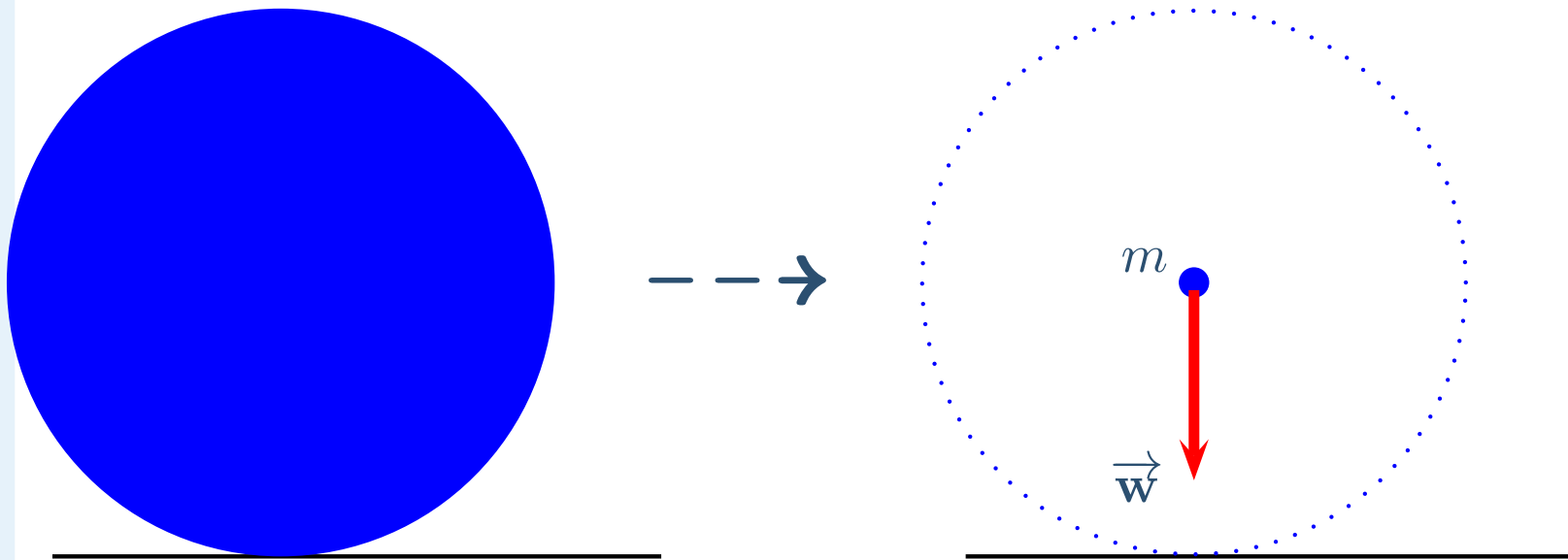
Center of Gravity - Position on an rigid body where the entirety of the weight seems to reside \Rightarrow the place we draw the weight.



Gravitational Potential Energy

To find the gravitational potential energy of a rigid body, we use the center of gravity.

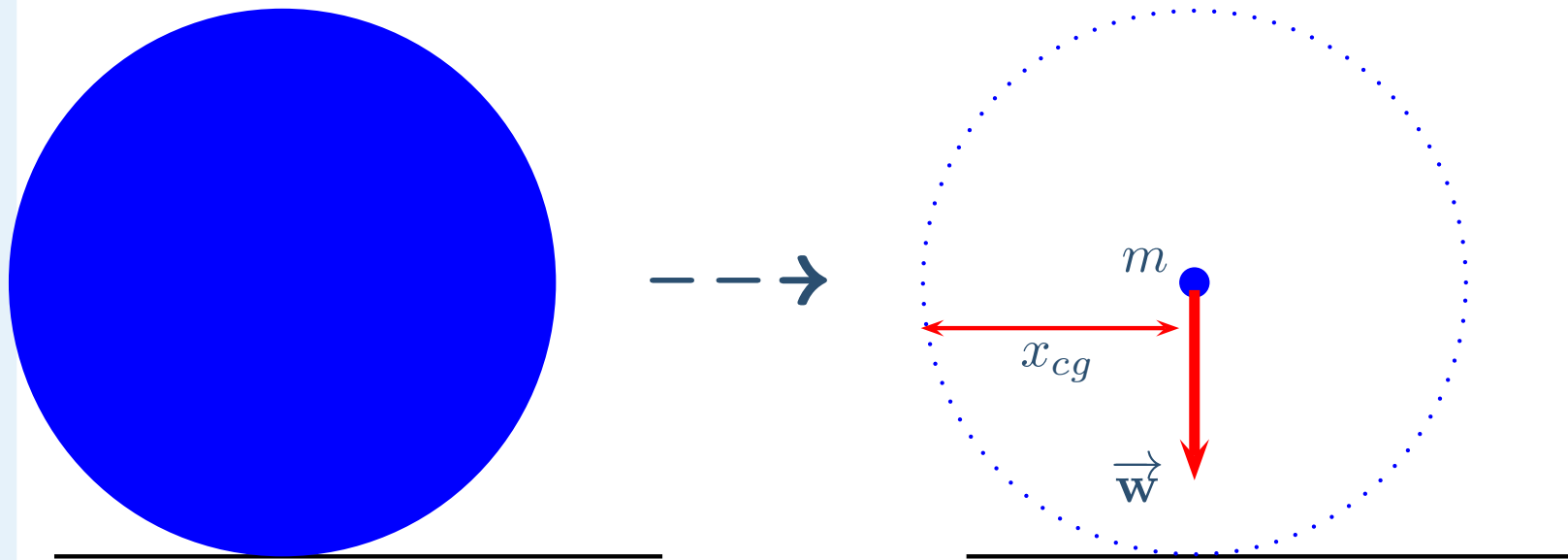
Center of Gravity - Position on an rigid body where the entirety of the weight seems to reside \Rightarrow the place we draw the weight.



Gravitational Potential Energy

To find the gravitational potential energy of a rigid body, we use the center of gravity.

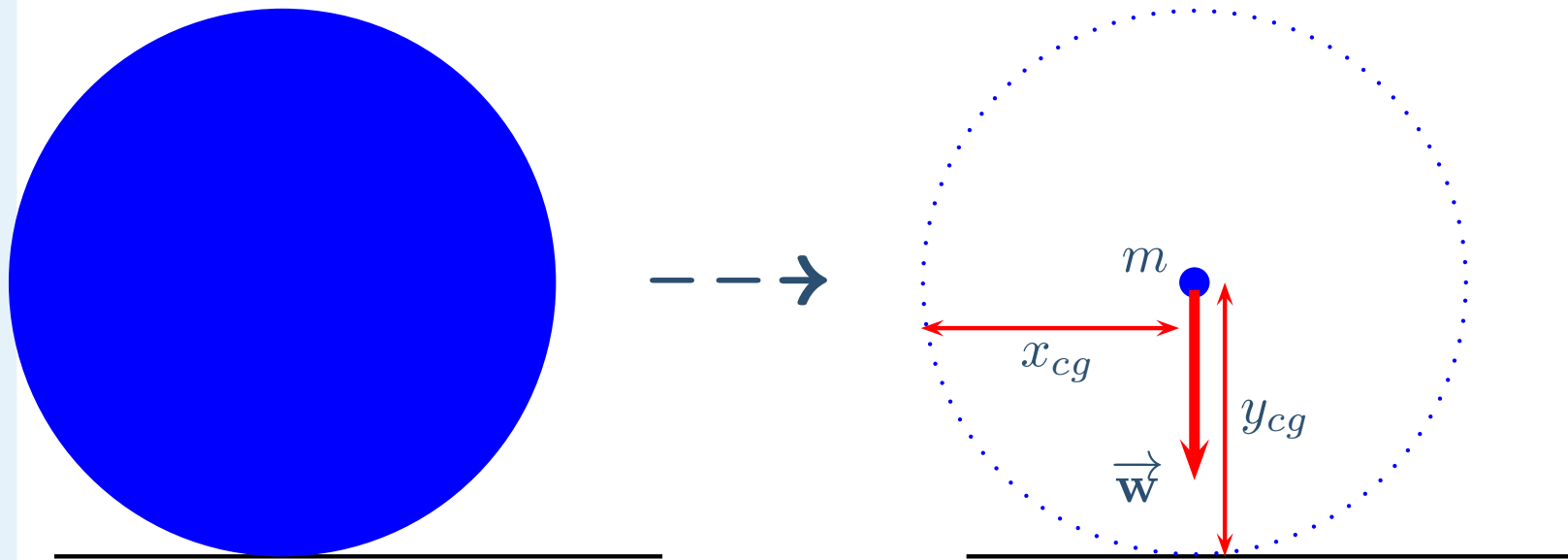
Center of Gravity - Position on an rigid body where the entirety of the weight seems to reside \Rightarrow the place we draw the weight.



Gravitational Potential Energy

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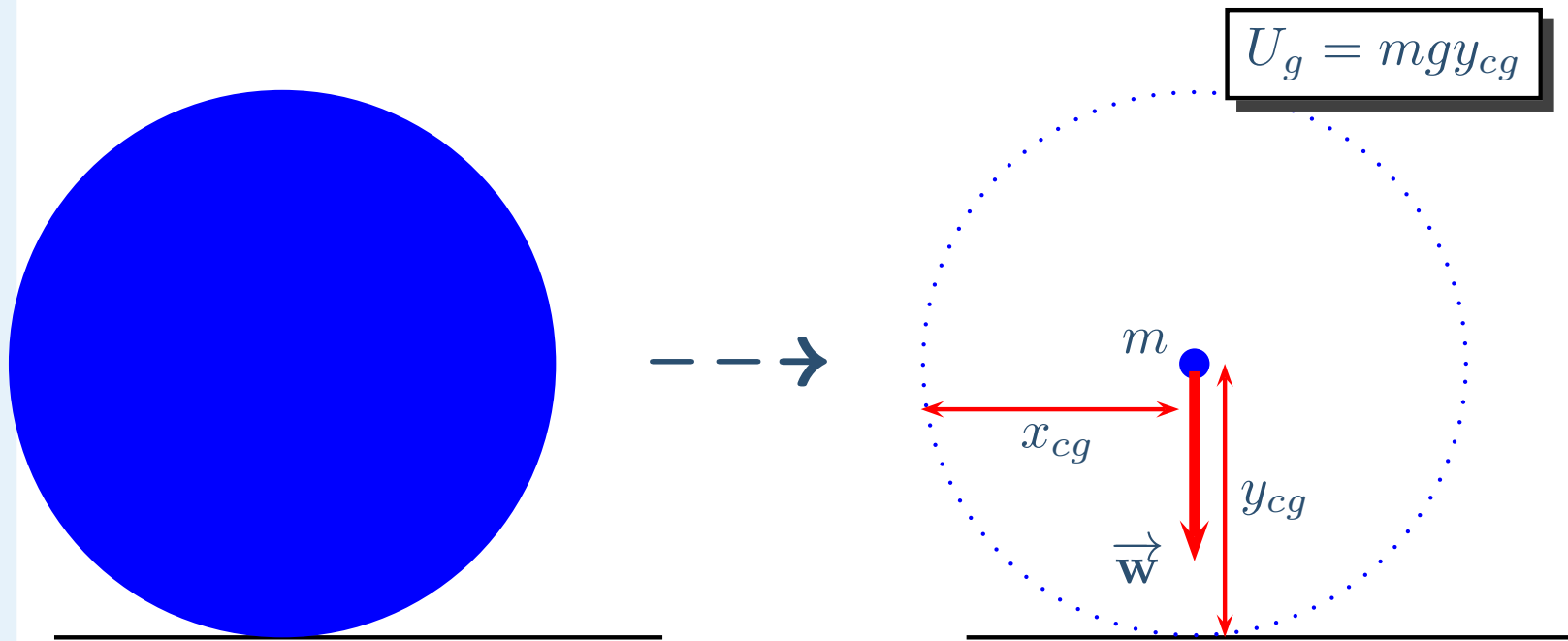
Center of Gravity - Position on an rigid body where the entirety of the weight seems to reside \Rightarrow the place we draw the weight.



Gravitational Potential Energy

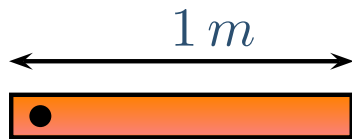
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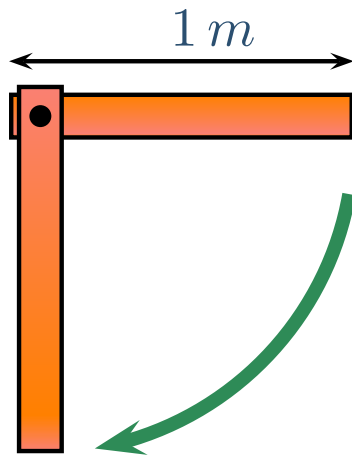
Potential Energy exercise

A 0.15-kg uniform meter stick is held 1 m above the ground by one end. What is the change in its gravitational potential energy, ΔU_g , when it swings through the vertical?



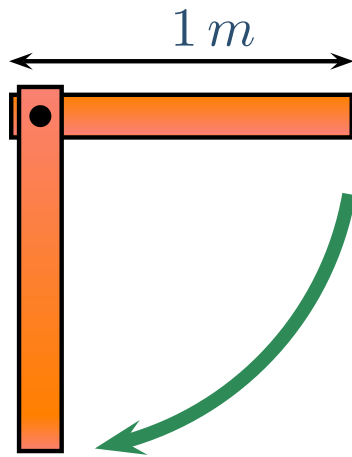
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Potential Energy exercise

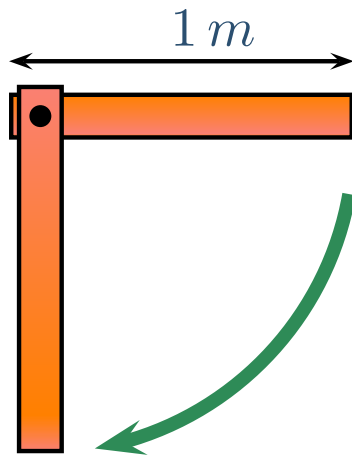
A 0.15-kg uniform meter stick is held 1 m above the ground by one end. What is the change in its gravitational potential energy, ΔU_g , when it swings through the vertical?



$$\begin{aligned} \text{(a)} \quad & (0.15\text{ kg})(9.8\text{ m/s}^2)(1\text{ m}) \\ & = 1.47\text{ J} \end{aligned}$$

Potential Energy exercise

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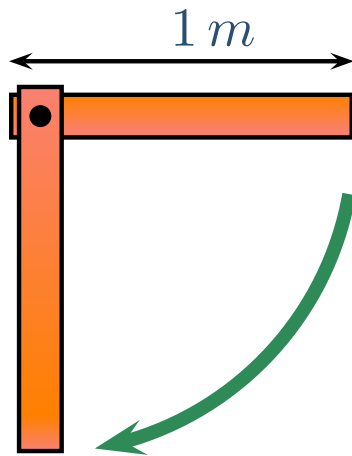


(a) $(0.15\text{ kg})(9.8\text{ m/s}^2)(1\text{ m})$
 $= 1.47\text{ J}$

(b) $(0.15\text{ kg})(9.8\text{ m/s}^2)(-1\text{ m})$
 $= -1.47\text{ J}$

Potential Energy exercise

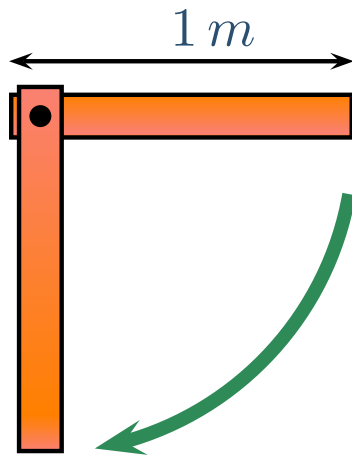
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 $= 1.47\text{ J}$
- (b) $(0.15\text{ kg})(9.8\text{ m/s}^2)(-1\text{ m})$
 $= -1.47\text{ J}$
- (c) $(0.15\text{ kg})(9.8\text{ m/s}^2)(0.5\text{ m})$
 $= 0.735\text{ J}$

Potential Energy exercise

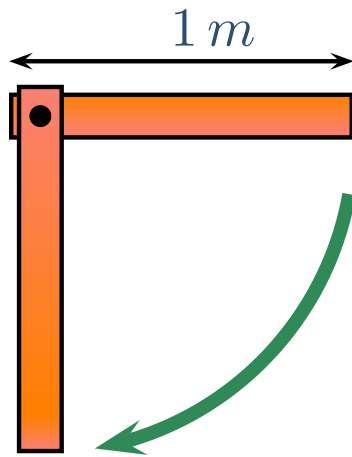
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- (a) $(0.15\text{ kg})(9.8\text{ m/s}^2)(1\text{ m})$
 $= 1.47\text{ J}$
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 $= -1.47\text{ J}$
- (c) $(0.15\text{ kg})(9.8\text{ m/s}^2)(0.5\text{ m})$
 $= 0.735\text{ J}$
- (d) $(0.15\text{ kg})(9.8\text{ m/s}^2)(-0.5\text{ m})$
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Potential Energy exercise

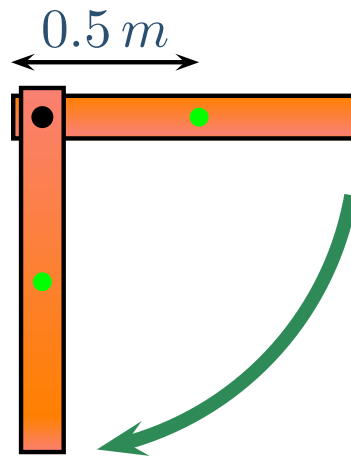
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 $= -1.47\text{ J}$
- (c) $(0.15\text{ kg})(9.8\text{ m/s}^2)(0.5\text{ m})$
 $= 0.735\text{ J}$
- (d) $(0.15\text{ kg})(9.8\text{ m/s}^2)(-0.5\text{ m})$
 $= -0.735\text{ J}$
- (e) $(0.15\text{ kg})(9.8\text{ m/s}^2)(0\text{ m})$
 $= 0\text{ J}$

Potential Energy exercise

A 0.15-kg uniform meter stick is held 1 m above the ground by one end. What is the change in its gravitational potential energy, ΔU_g , when it swings through the vertical?

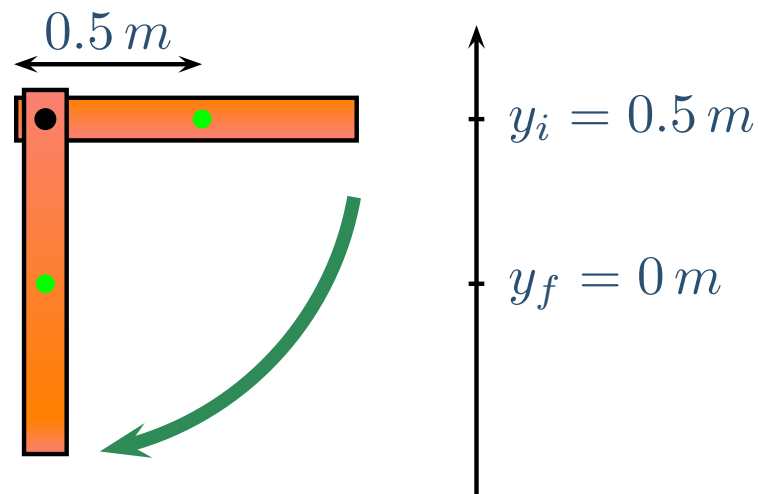


● = Center of Gravity

- (a) $(0.15\text{ kg})(9.8\text{ m/s}^2)(1\text{ m})$
 $= 1.47\text{ J}$
- (b) $(0.15\text{ kg})(9.8\text{ m/s}^2)(-1\text{ m})$
 $= -1.47\text{ J}$
- (c) $(0.15\text{ kg})(9.8\text{ m/s}^2)(0.5\text{ m})$
 $= 0.735\text{ J}$
- (d) $(0.15\text{ kg})(9.8\text{ m/s}^2)(-0.5\text{ m})$
 $= -0.735\text{ J}$
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 $= 0\text{ J}$

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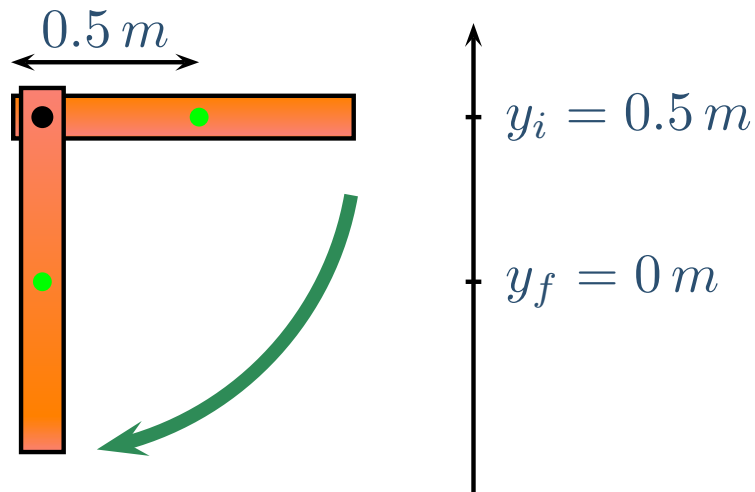


● = Center of Gravity

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Potential Energy exercise

A 0.15-kg uniform meter stick is held 1 m above the ground by one end. What is the change in its gravitational potential energy, ΔU_g , when it swings through the vertical?



● = Center of Gravity

$$\begin{aligned}\Delta U_g &= mgy_{cg,f} - mgy_{cg,i} \\ &= 0 - mgy_{cg,i}\end{aligned}$$

- (a) $(0.15\text{ kg})(9.8\text{ m/s}^2)(1\text{ m})$
 $= 1.47\text{ J}$
- (b) $(0.15\text{ kg})(9.8\text{ m/s}^2)(-1\text{ m})$
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 $= 0.735\text{ J}$
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 $= -0.735\text{ J}$
- (e) $(0.15\text{ kg})(9.8\text{ m/s}^2)(0\text{ m})$
 $= 0\text{ J}$

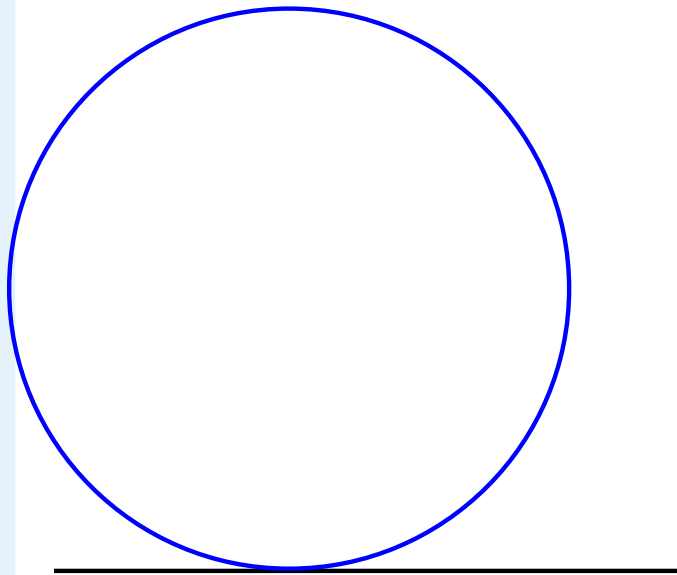
Conservation of Rotational energy

If gravity is the only force doing work on a rigid body:

$$\frac{1}{2}I\omega_i^2 + mgy_{cg,i} = \frac{1}{2}I\omega_f^2 + mgy_{cg,f}$$

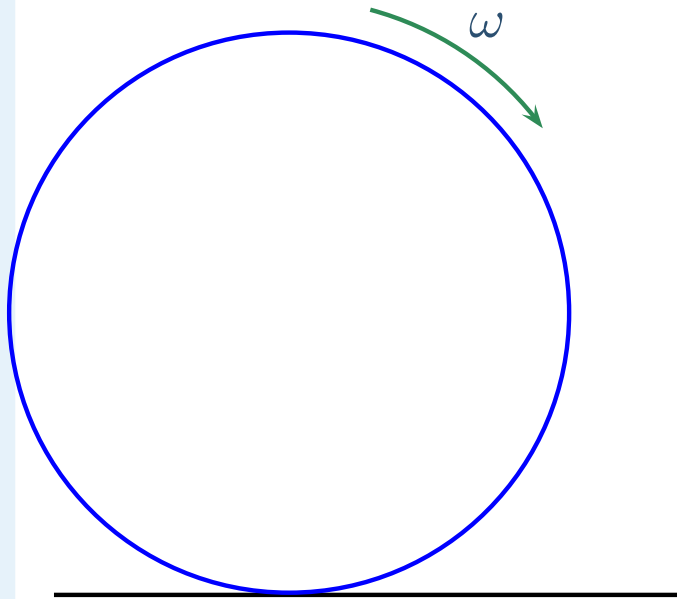
Rolling

When an object rolls, it rotates and its center moves.



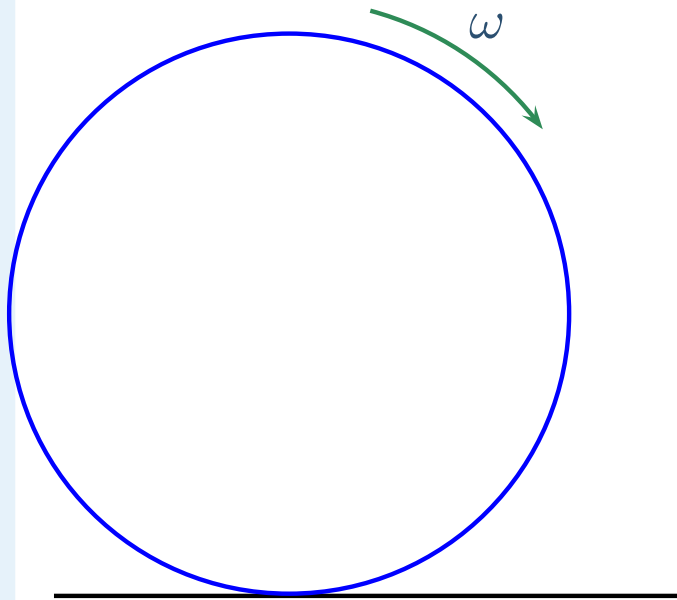
Rolling

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Rolling

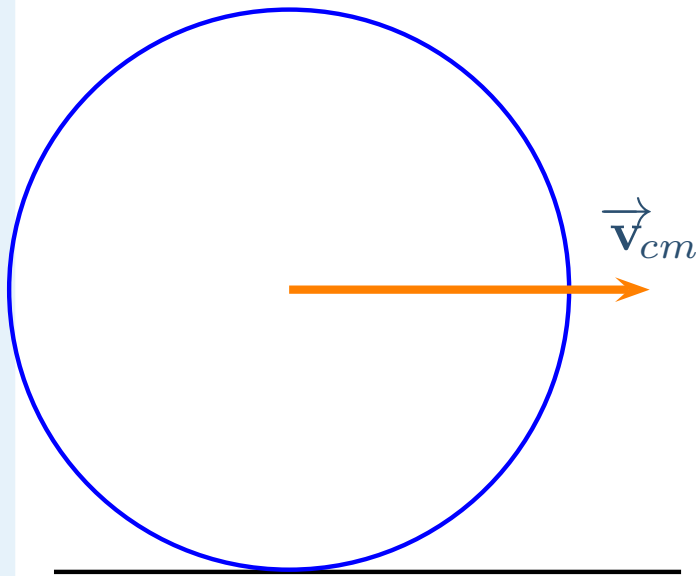
When an object rolls, it rotates and its center moves.



$$\text{Rotational: } K_r = \frac{1}{2}I\omega^2$$

Rolling

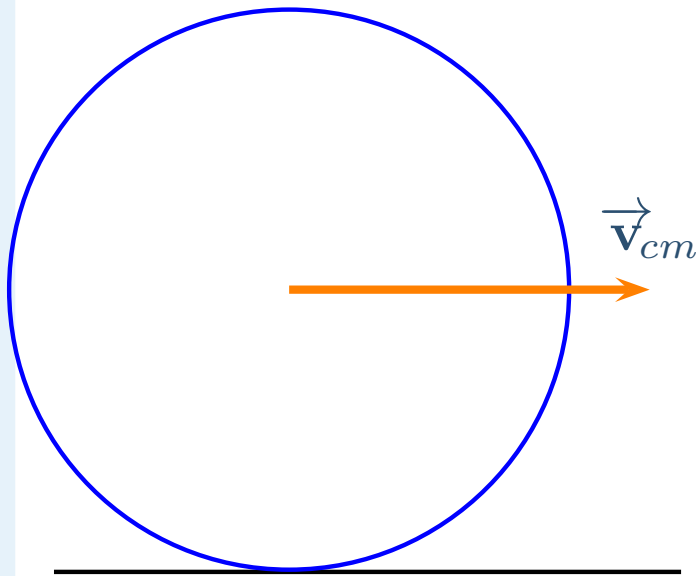
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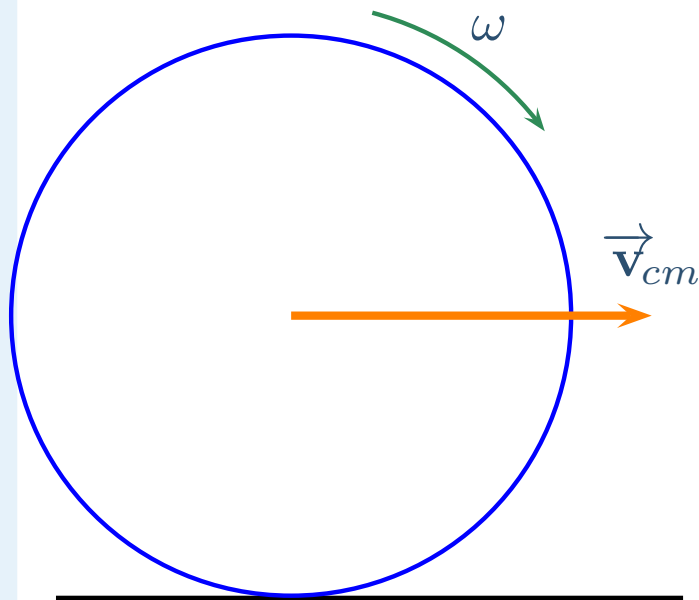


$$\text{Translational: } K_t = \frac{1}{2}mv_{cm}^2$$

$$\text{Rotational: } K_r = \frac{1}{2}I\omega^2$$

Rolling

When an object rolls, it rotates and its center moves.

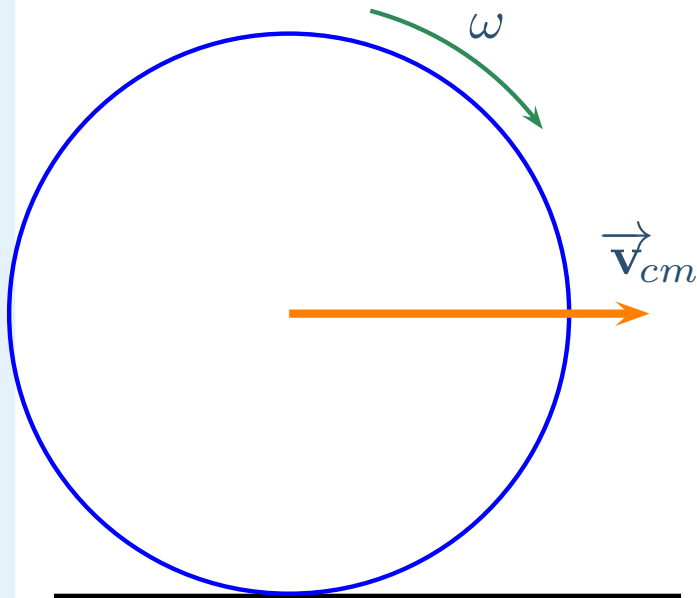


Translational: $K_t = \frac{1}{2}mv_{cm}^2$

Rotational: $K_r = \frac{1}{2}I\omega^2$

Rolling

When an object rolls, it rotates and its center moves.



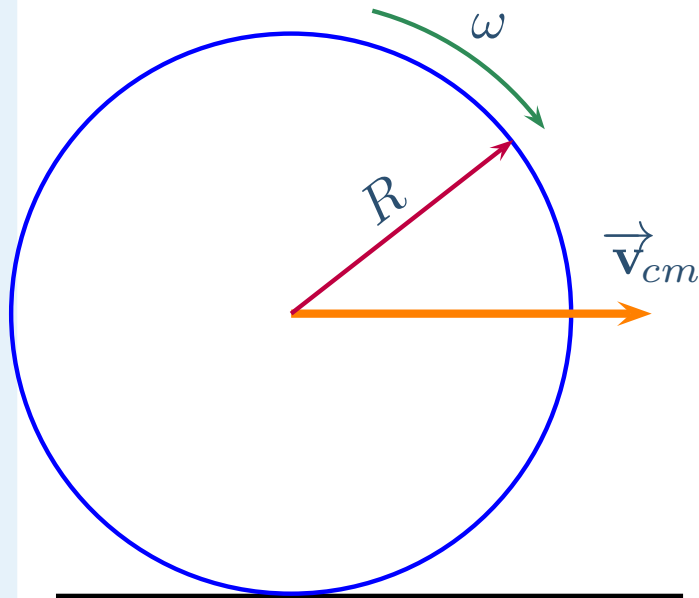
Translational: $K_t = \frac{1}{2}mv_{cm}^2$

Rotational: $K_r = \frac{1}{2}I\omega^2$

Total: $K = K_t + K_r = \frac{1}{2}mv_{cm}^2 + \frac{1}{2}I\omega^2$

Rolling

When an object rolls, it rotates and its center moves.



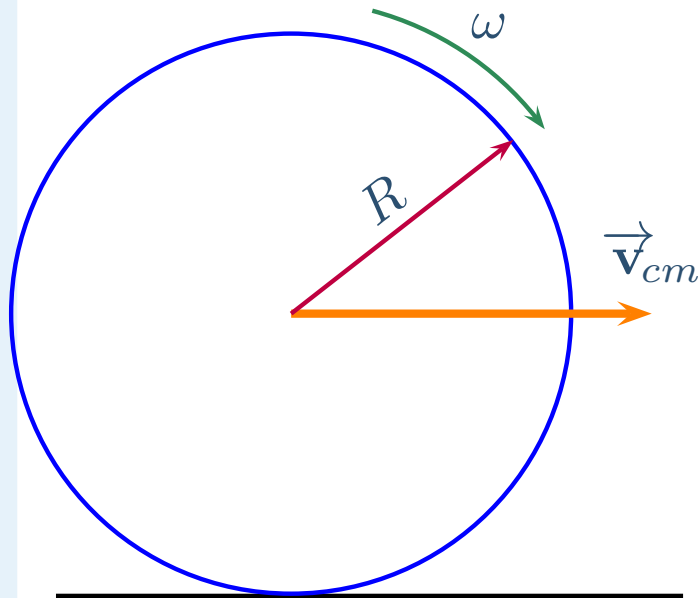
$$\text{Translational: } K_t = \frac{1}{2}mv_{cm}^2$$

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$$\text{Total: } K = K_t + K_r = \frac{1}{2}mv_{cm}^2 + \frac{1}{2}I\omega^2$$

Rolling

When an object rolls, it rotates and its center moves.



Translational: $K_t = \frac{1}{2}mv_{cm}^2$

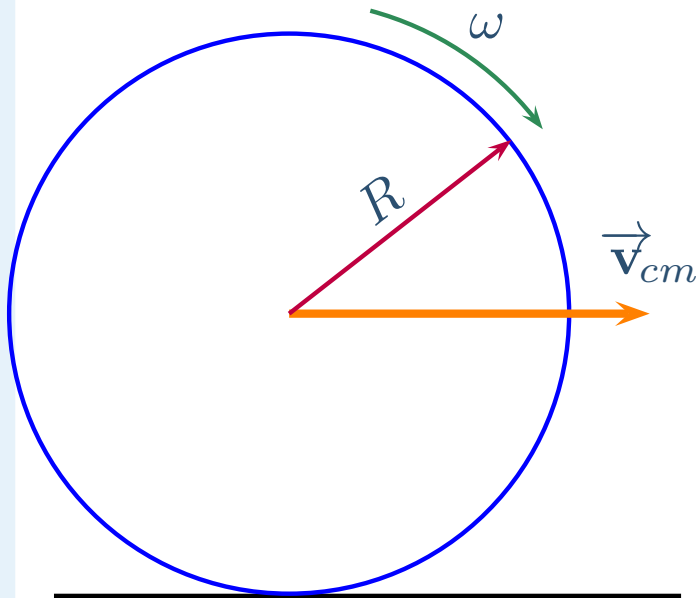
Rotational: $K_r = \frac{1}{2}I\omega^2$

Total: $K = K_t + K_r = \frac{1}{2}mv_{cm}^2 + \frac{1}{2}I\omega^2$

Rolling without slipping: $v_{cm} = \omega R$

Rolling

When an object rolls, it rotates and its center moves.



Translational: $K_t = \frac{1}{2}mv_{cm}^2$

Rotational: $K_r = \frac{1}{2}I\omega^2$

Total: $K = K_t + K_r = \frac{1}{2}mv_{cm}^2 + \frac{1}{2}I\omega^2$

Rolling without slipping: $v_{cm} = \omega R$

$$K = \frac{1}{2}mv_{cm}^2 \left(1 + \frac{I}{mR^2}\right)$$