

March 22, Week 9

Today: Chapter 7, Elastic Potential Energy

Homework Assignment #6 - Due Today

Mastering Physics: 9 problems from chapters 5 and 6

Written Questions: 6.73

Homework Assignment #7 - Due March 29

Mastering Physics: 6 problems from chapter 7

Written Questions: 7.60

Help sessions with Jonathan:

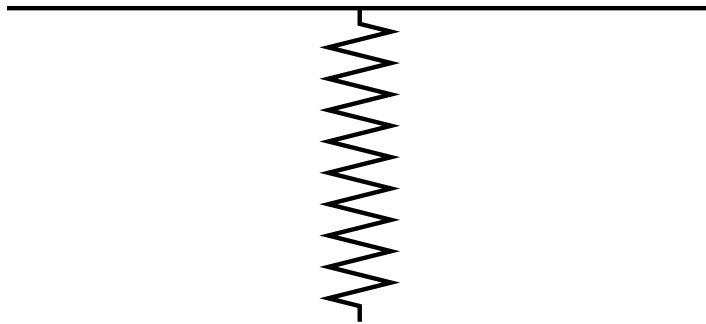
M: 1000-1100, RH 111

T: 1000-1100, RH 114

Th: 0900-1000, RH 114

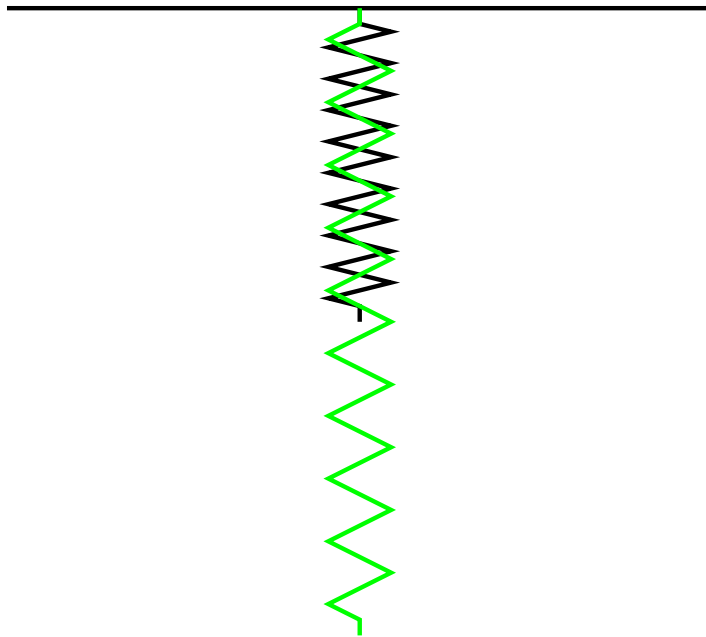
Hooke's Law

A simple example of a variable force is the force needed to stretch a spring.



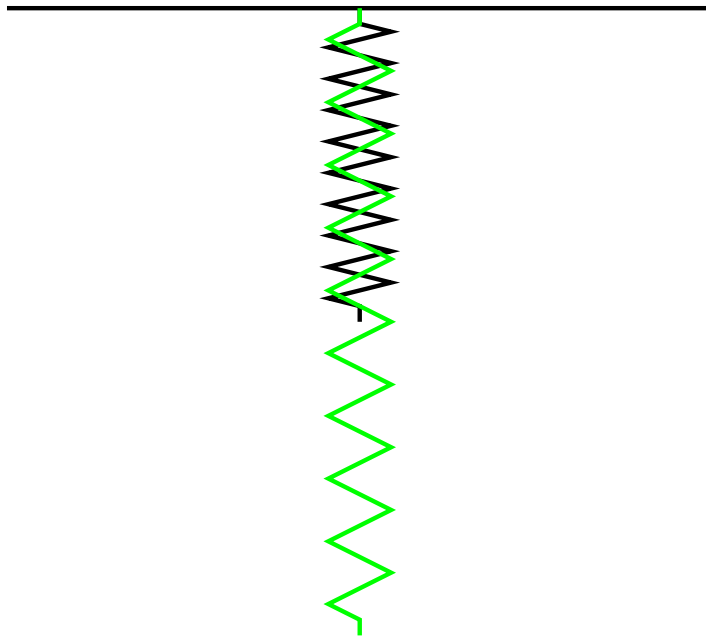
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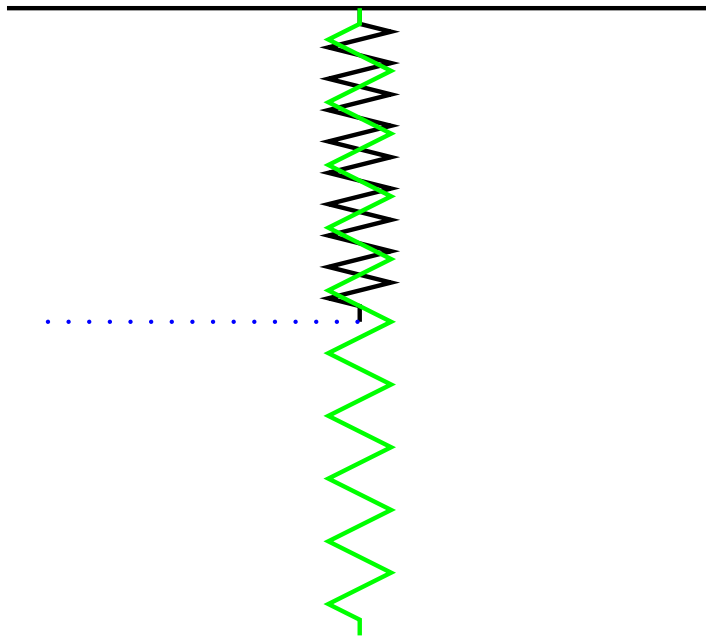
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Hooke's Law - The force needed to stretch or compress a spring increases linearly with stretching distance

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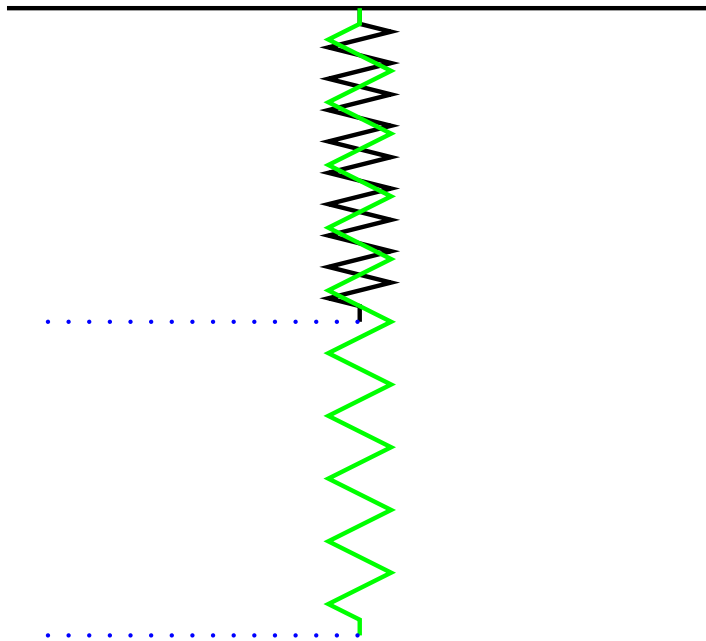
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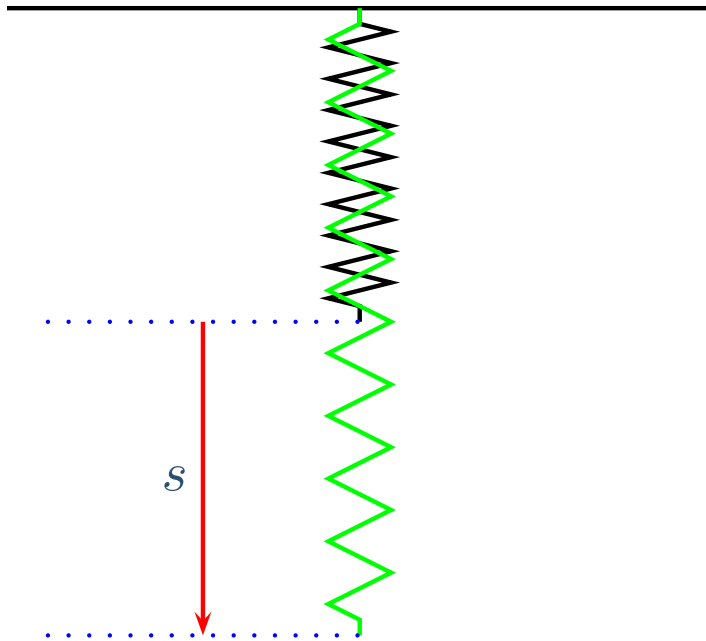
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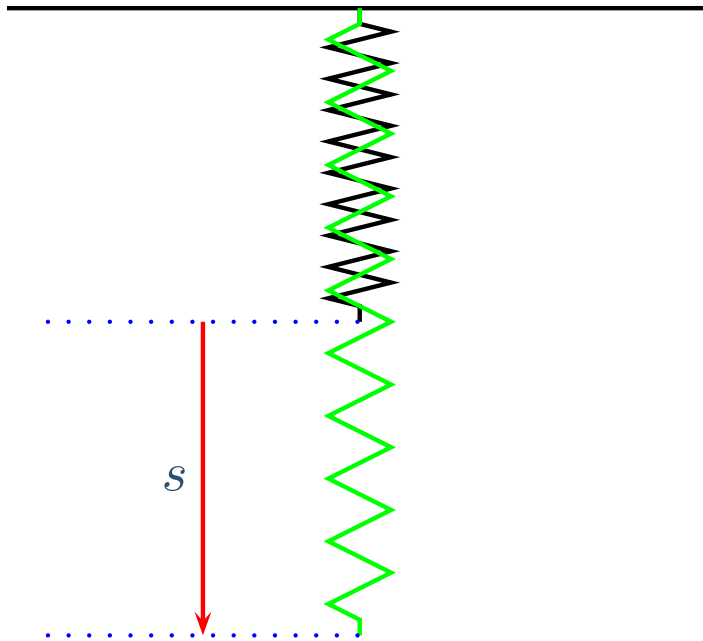
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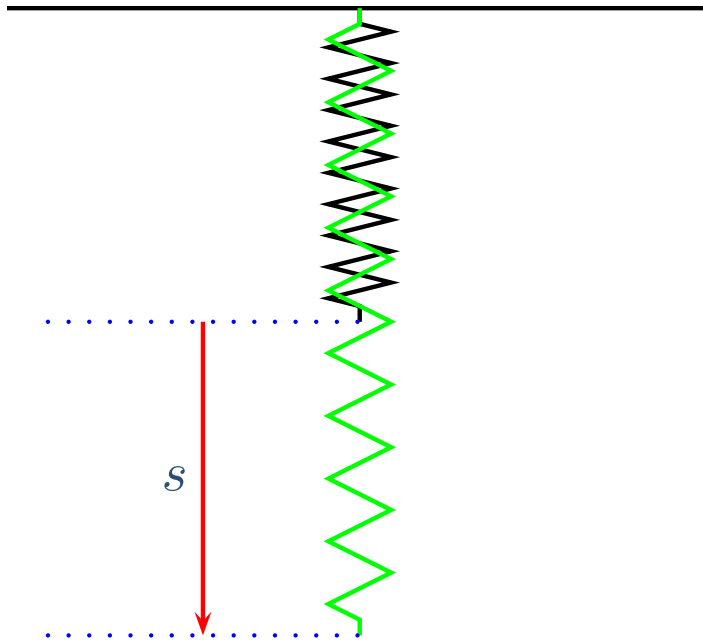


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$$F_{sp} = ks$$

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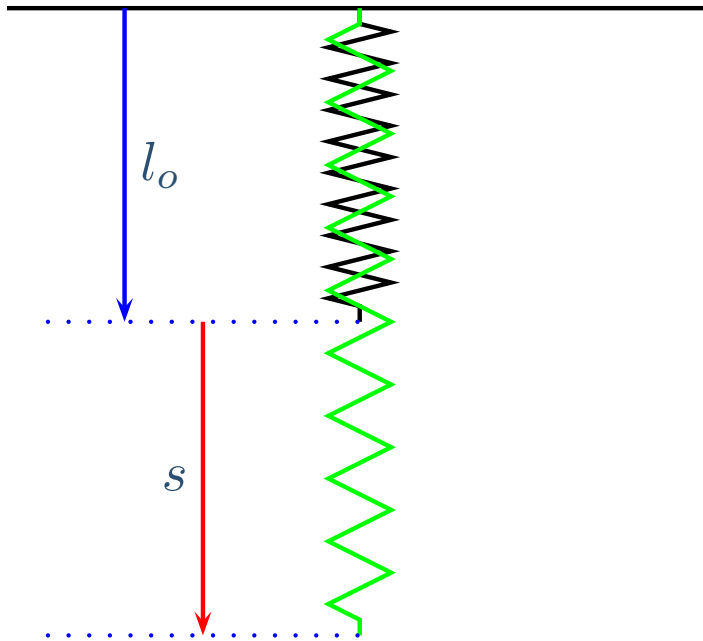
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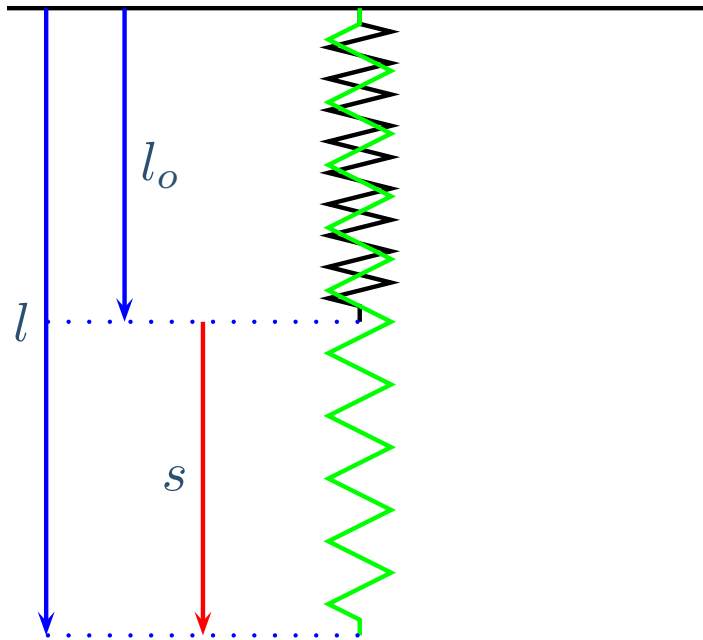
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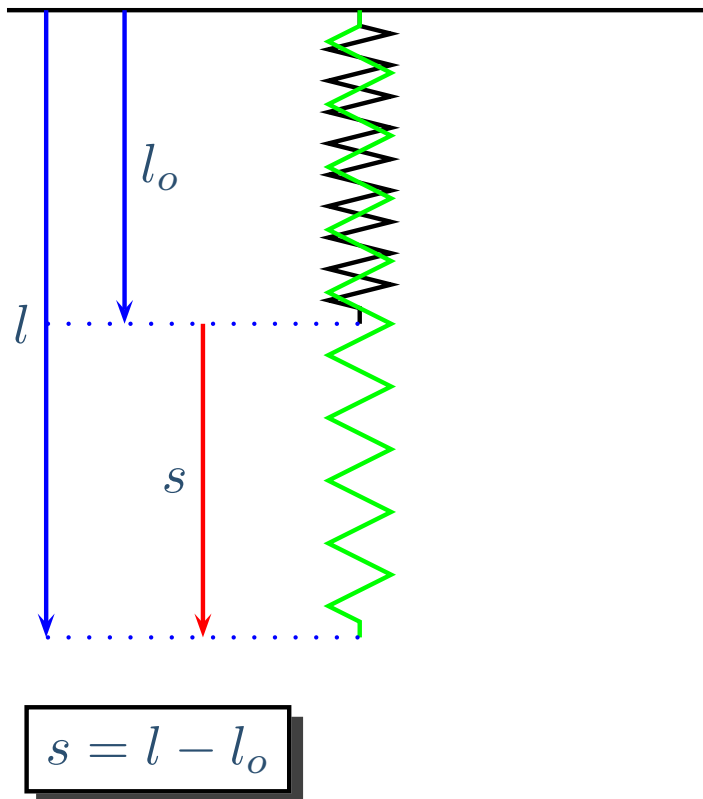
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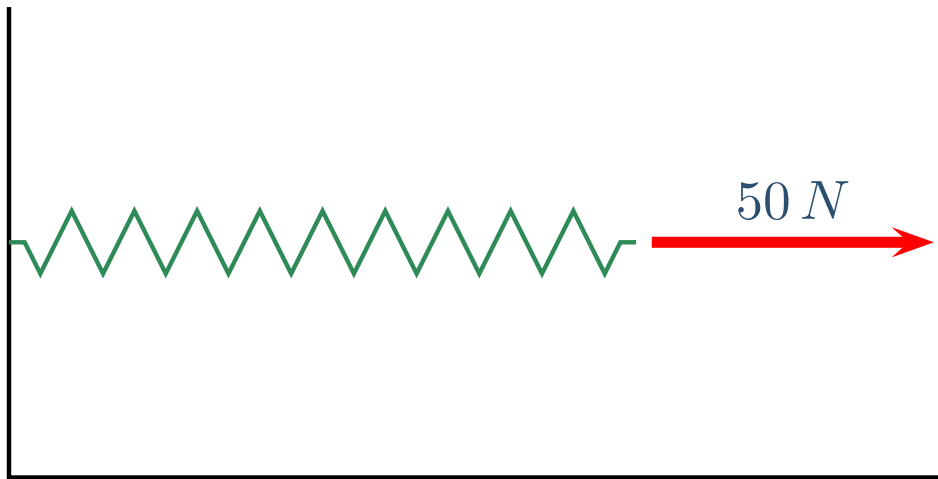
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Spring Exercise

$$F_{sp} = ks$$

A horizontal 50 N force is applied to a 100 N/m spring whose unstretched length is 0.5 m . What is the spring's length after the force has been applied?

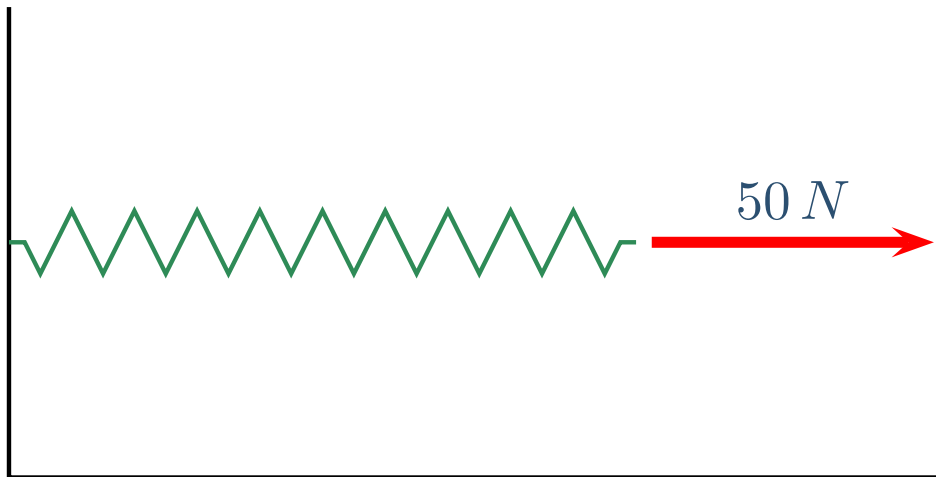


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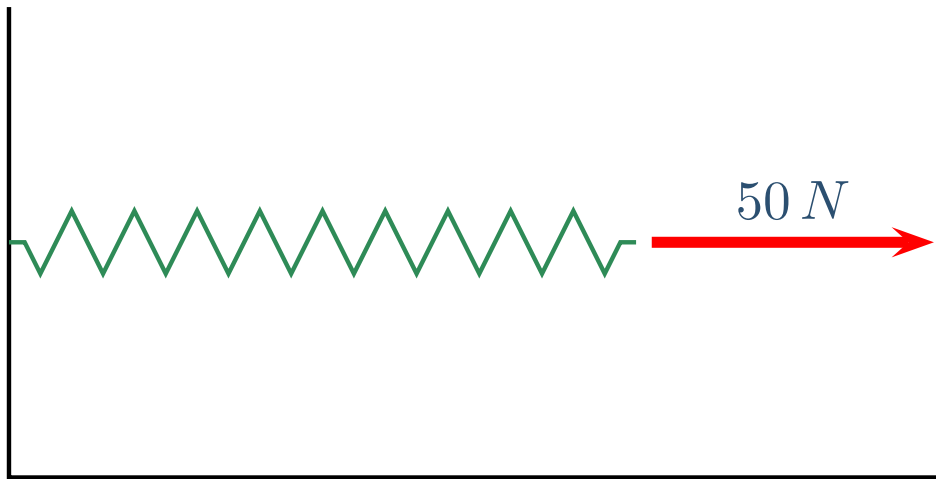
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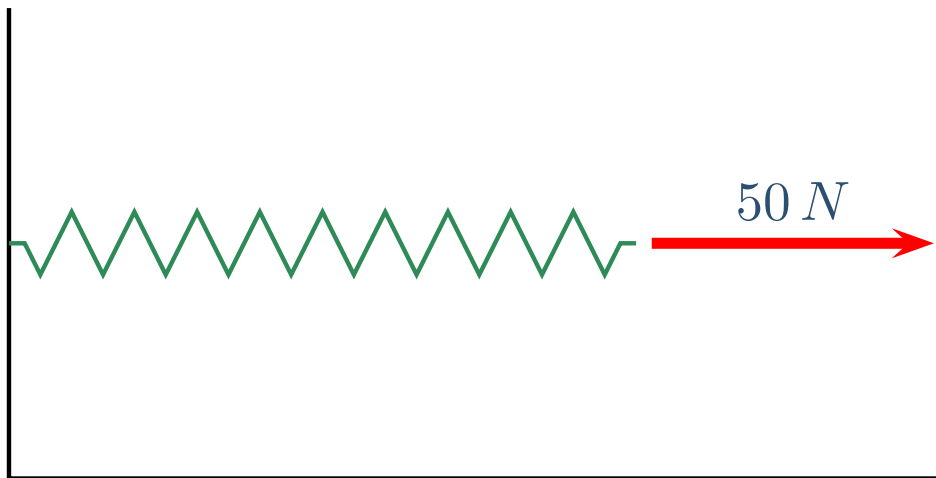
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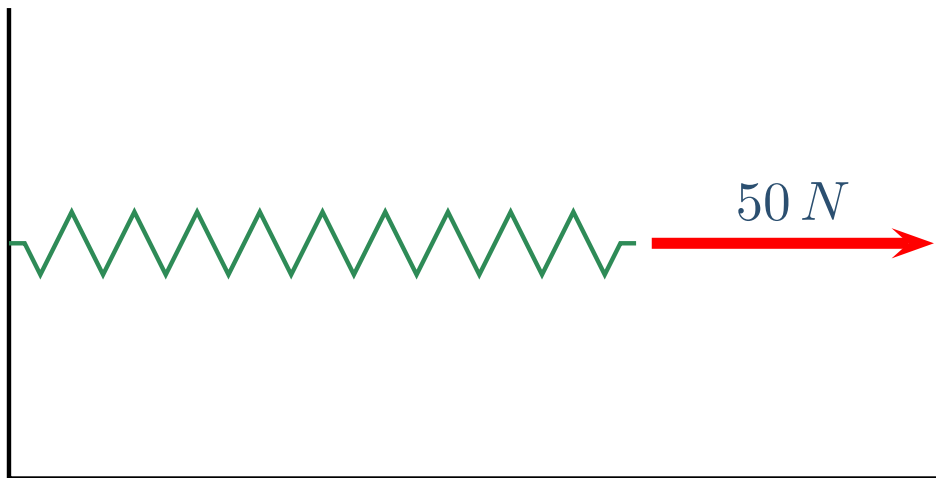
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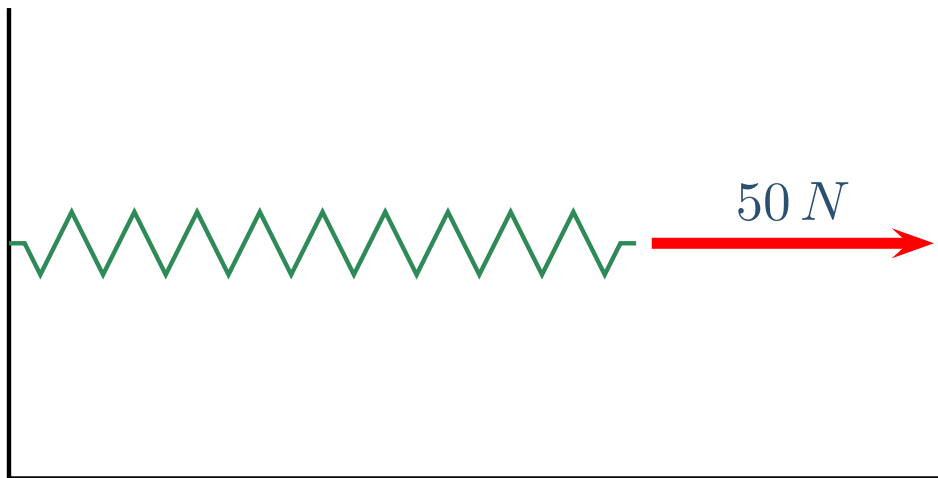
(a) 0 m

(b) 0.5 m

(c) 1 m

(d) 1.5 m

(e) 2 m



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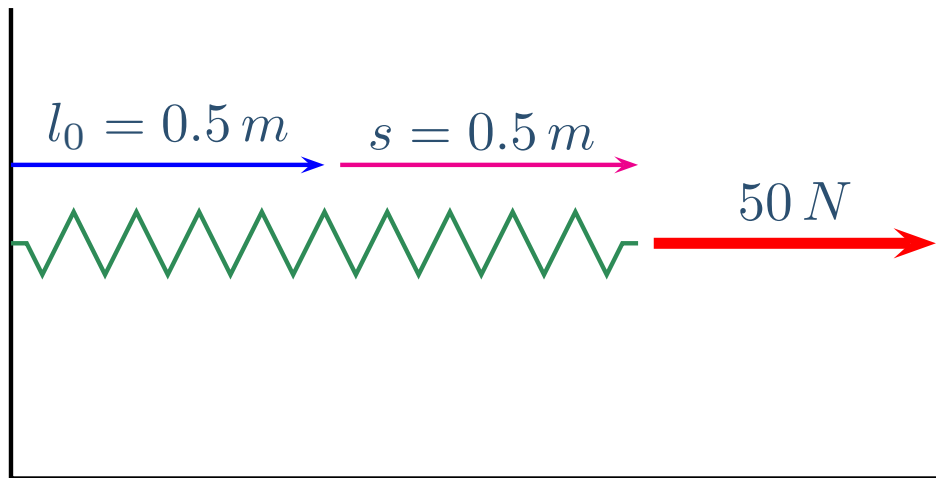
(a) 0 m

(b) 0.5 m

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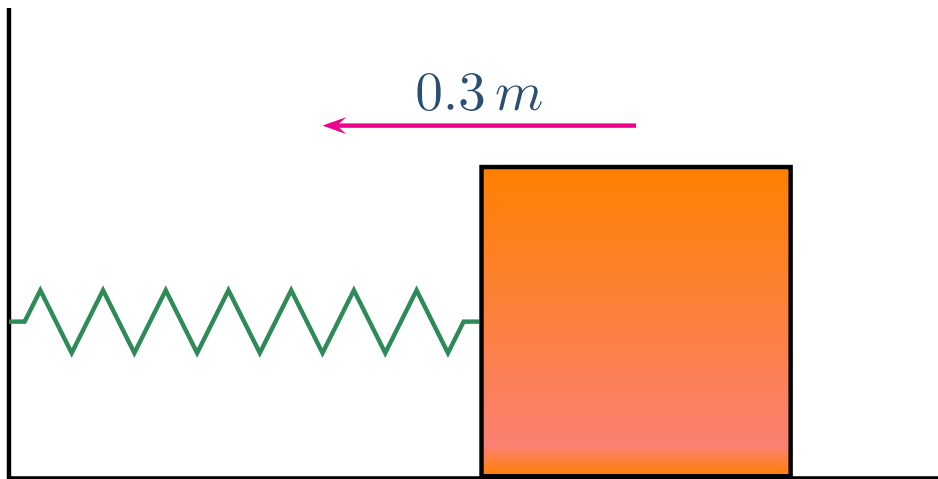
(e) 2 m



Spring Exercise II

$$F_{sp} = ks$$

A 5-kg mass is attached, as shown, to a 100 N/m spring whose unstretched length is 0.5 m . If the mass is pushed 0.3 m to the left, what is the magnitude and direction of the force exerted by the spring on the mass?

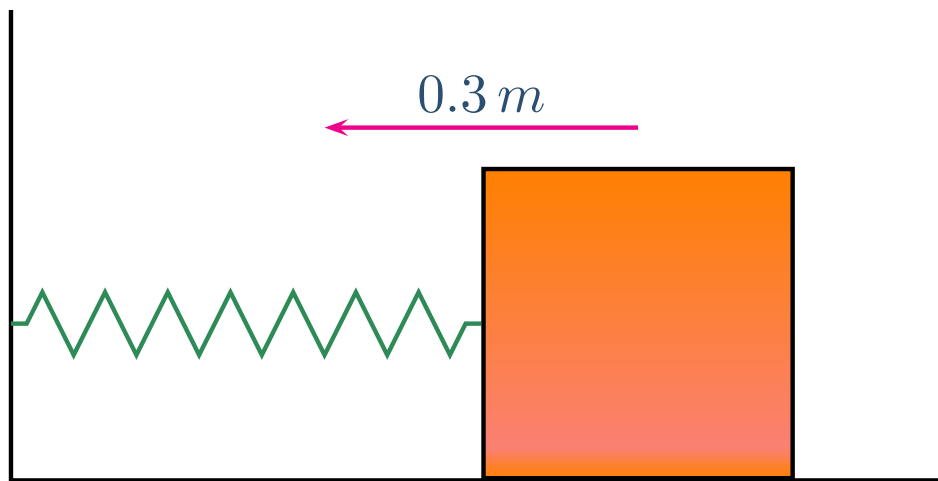


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(a) 30 N , Left



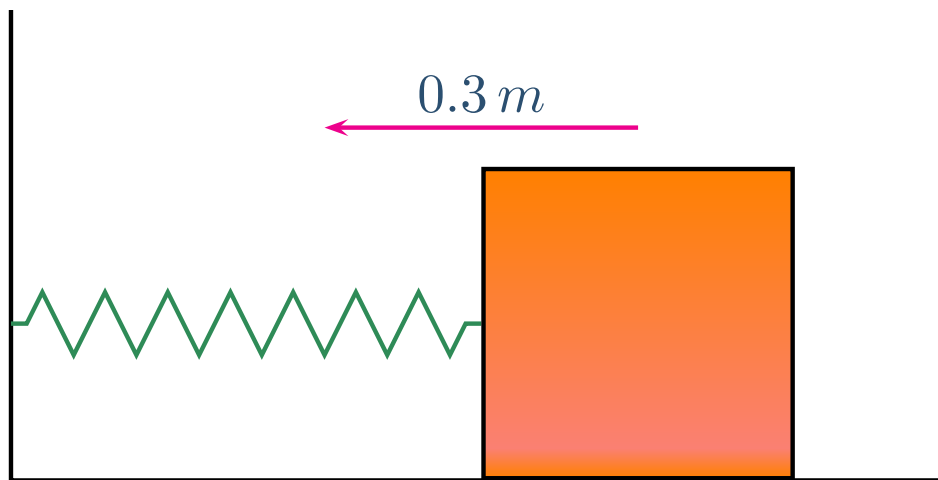
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Spring Exercise II

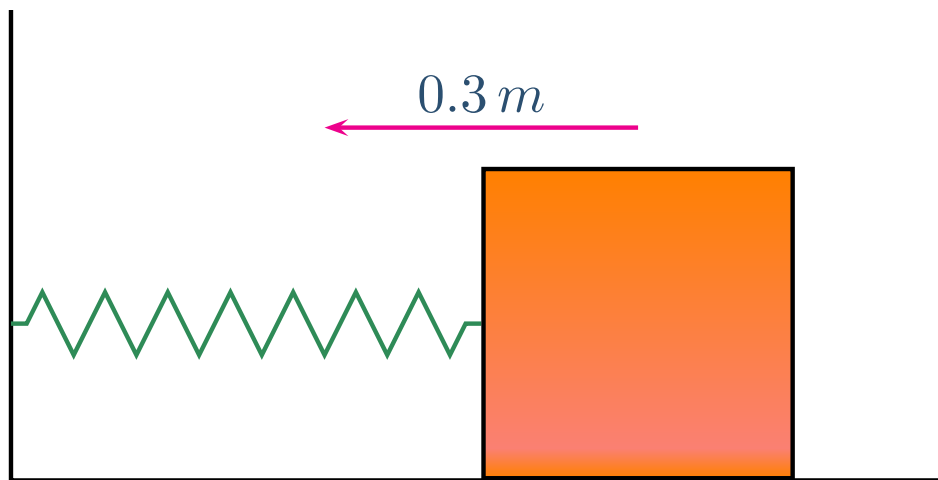
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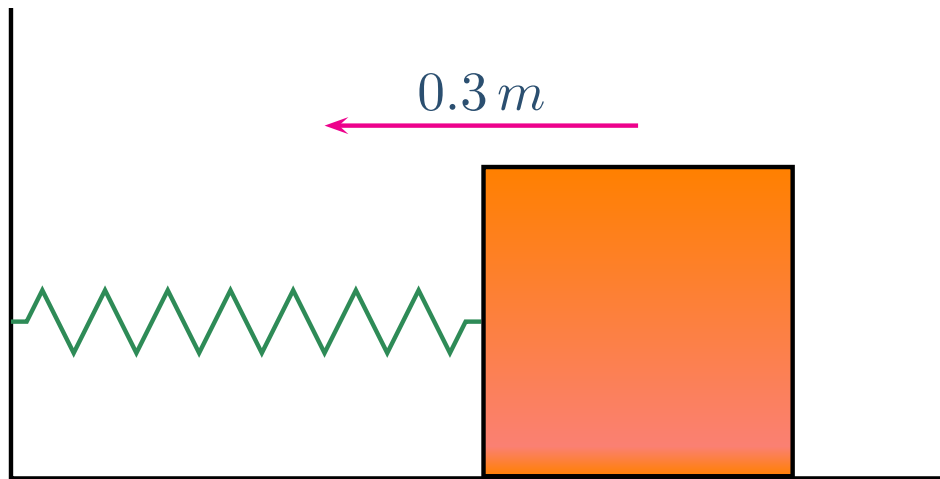
(c) 20 N , Left



Spring Exercise II

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(b) 30 N , Right

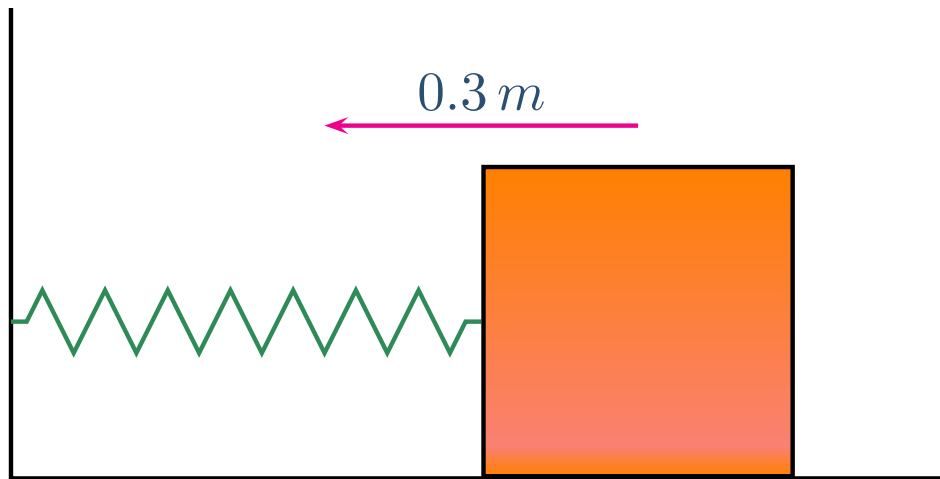
(c) 20 N , Left

(d) 20 N , Right

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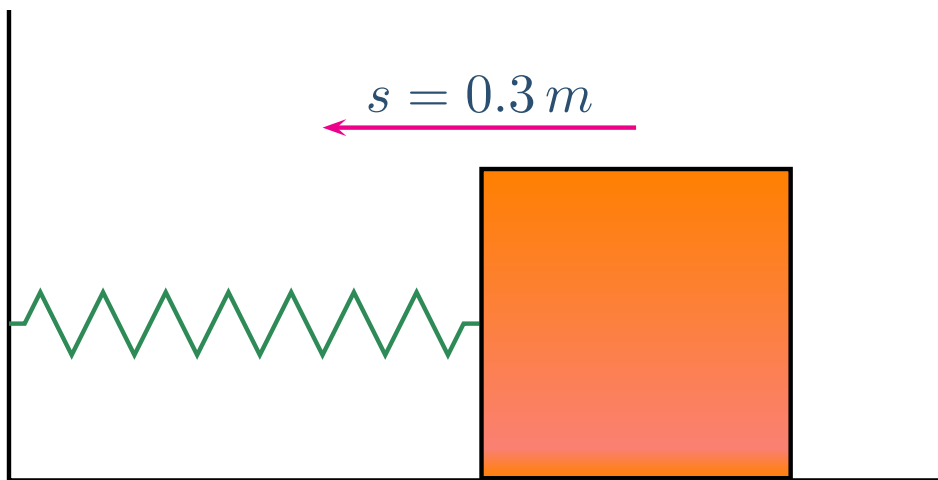
- (a) 30 N , Left
- (b) 30 N , Right
- (c) 20 N , Left
- (d) 20 N , Right
- (e) 50 N , Right

Spring Exercise II

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Springs can push or pull



(a) 30 N , Left

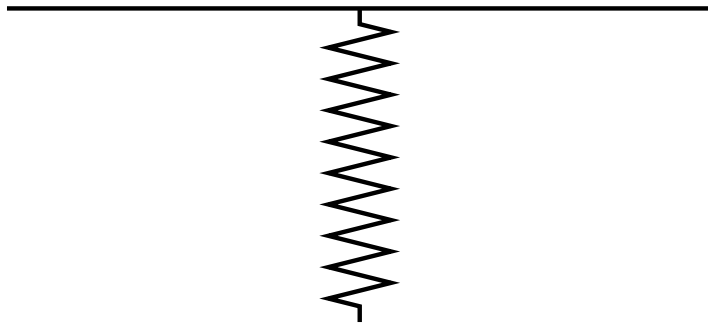
(b) 30 N , Right

(c) 20 N , Left

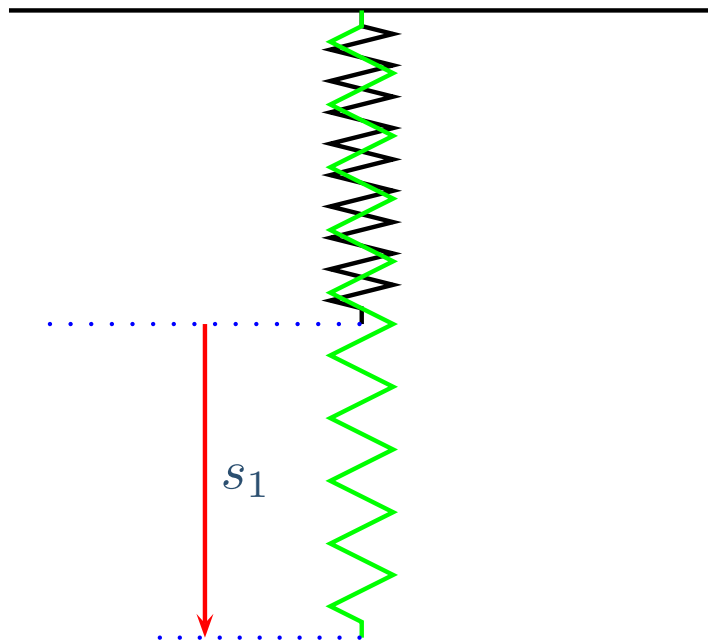
(d) 20 N , Right

(e) 50 N , Right

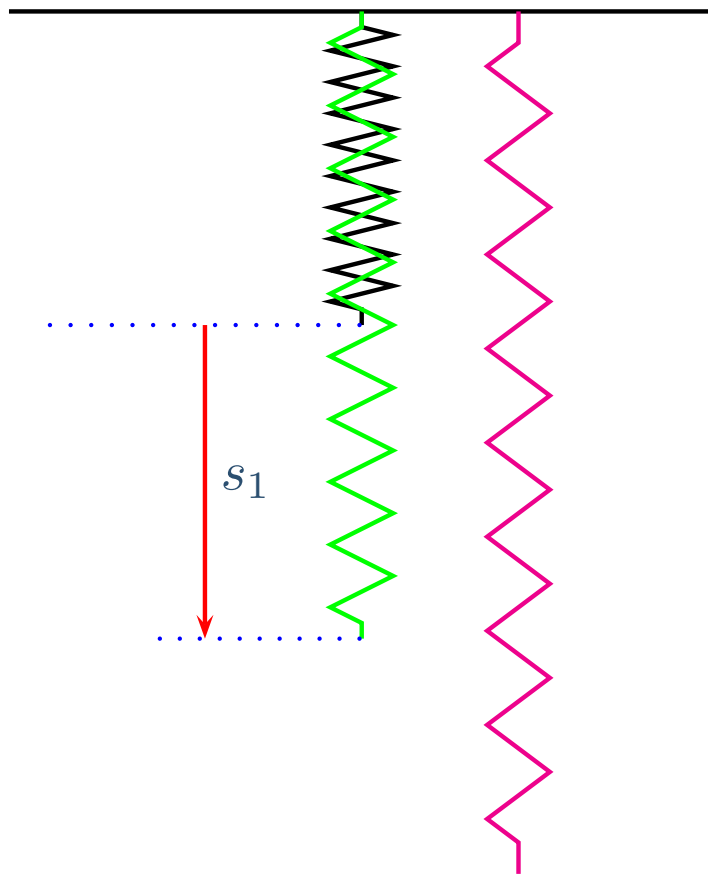
Work to Stretch a Spring



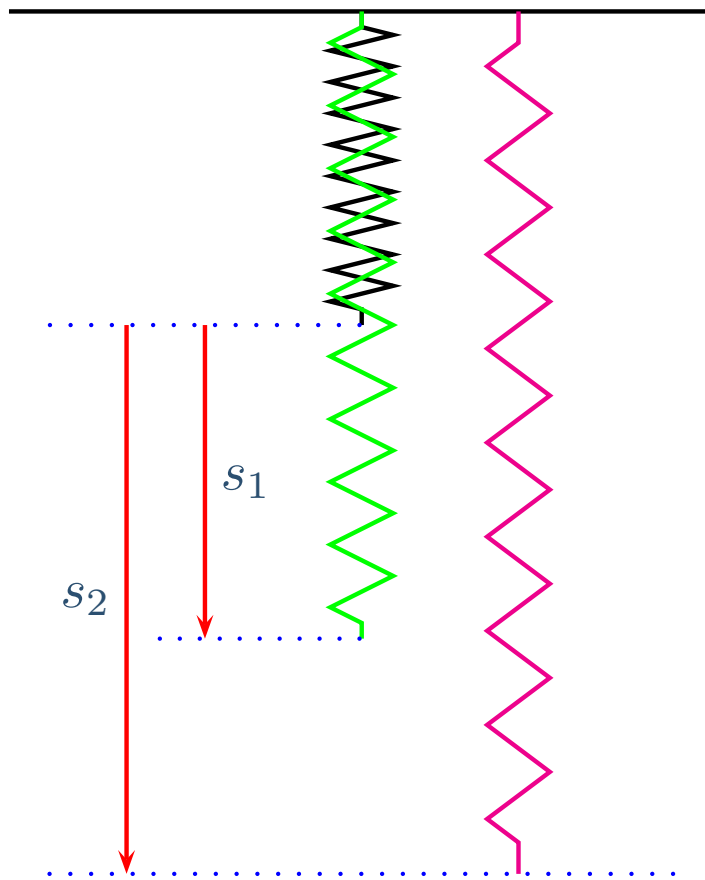
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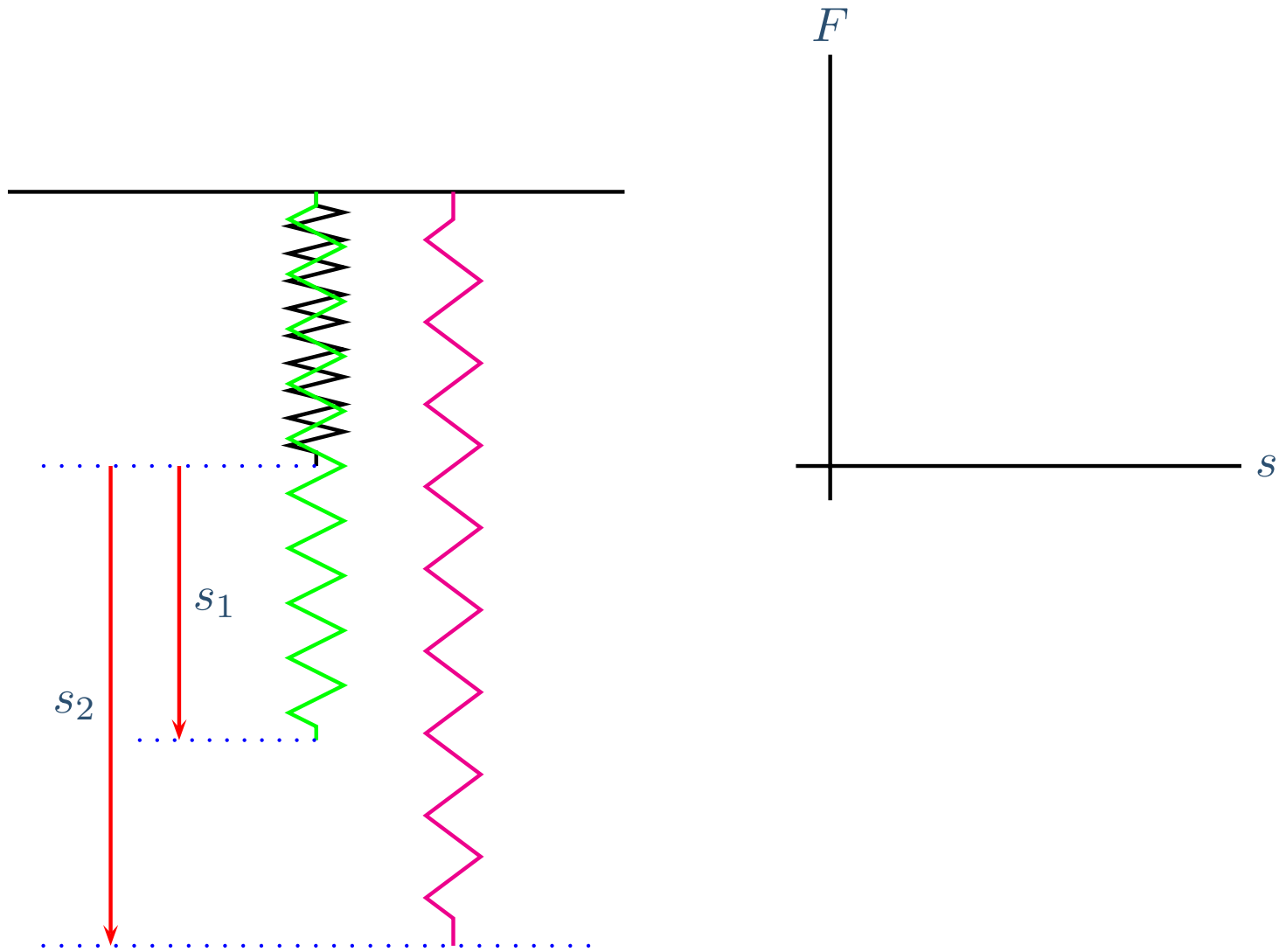
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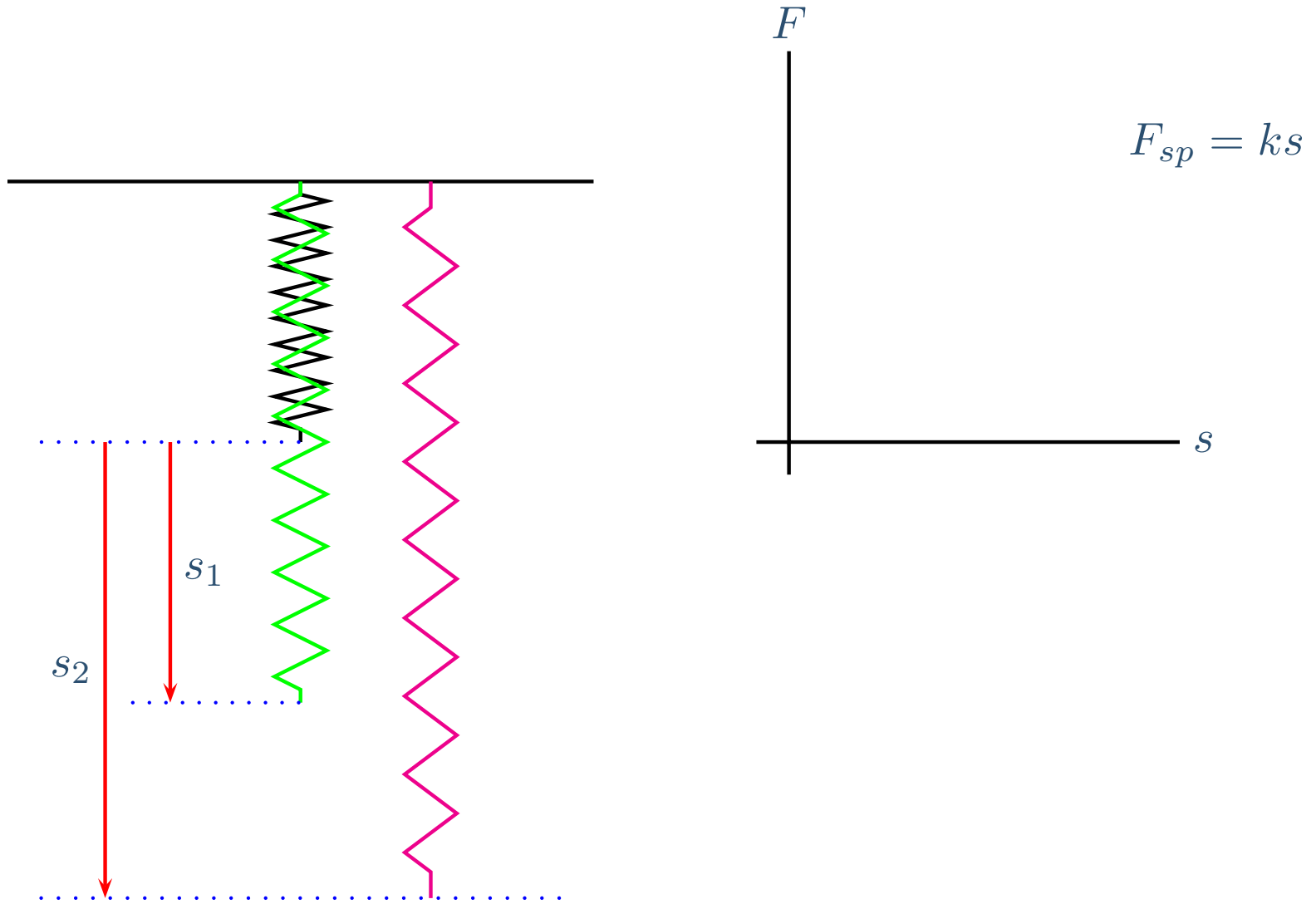
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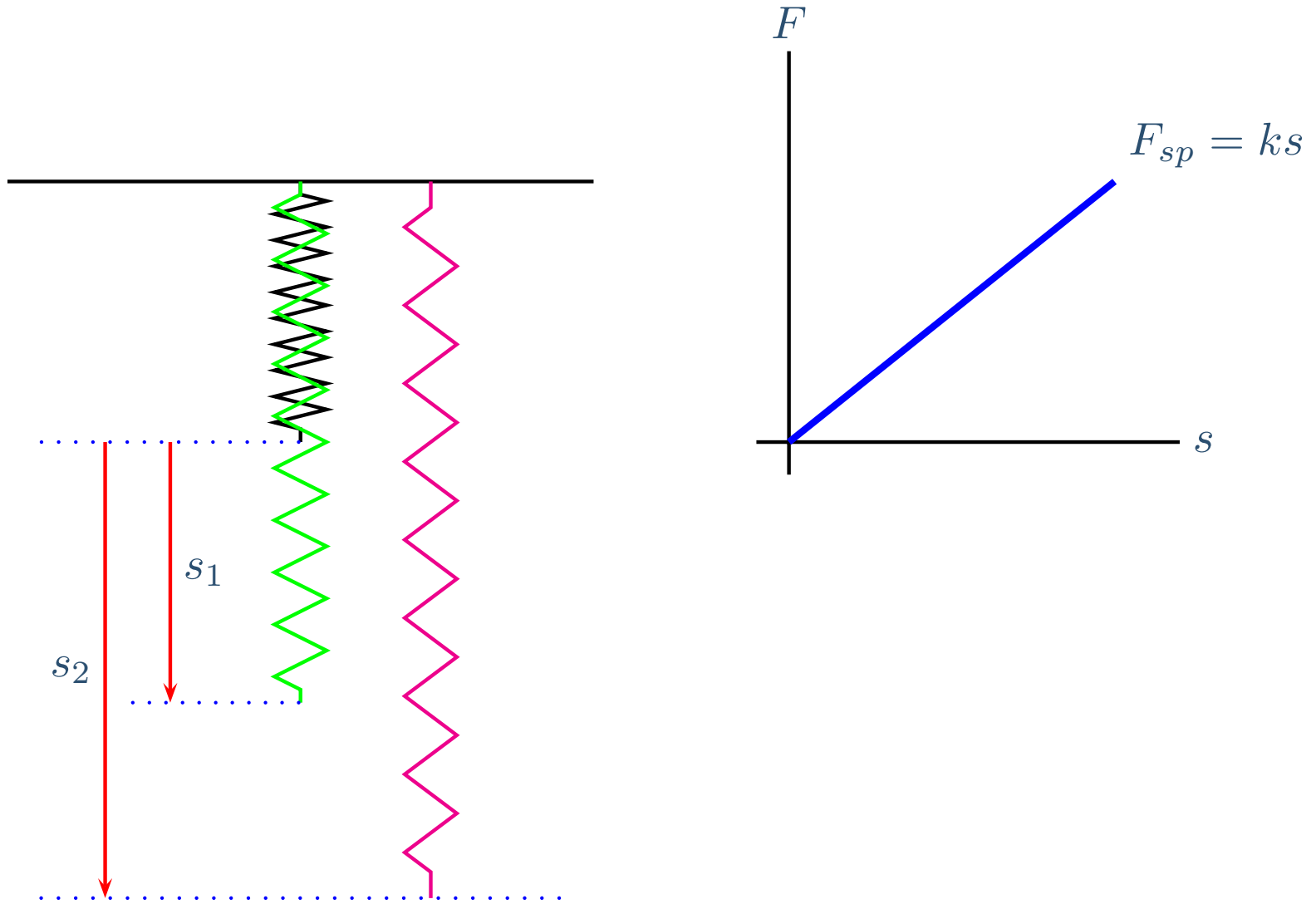
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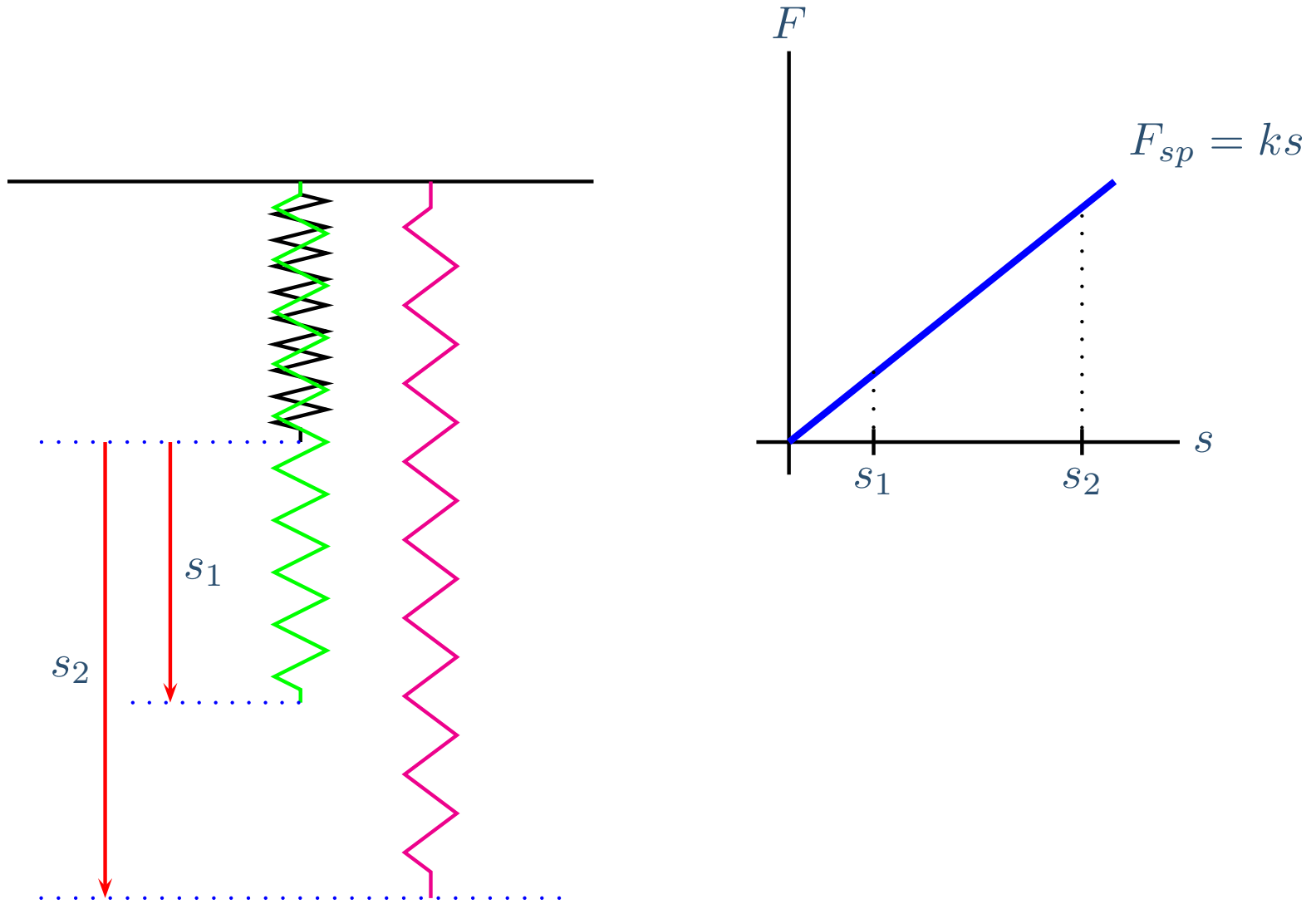
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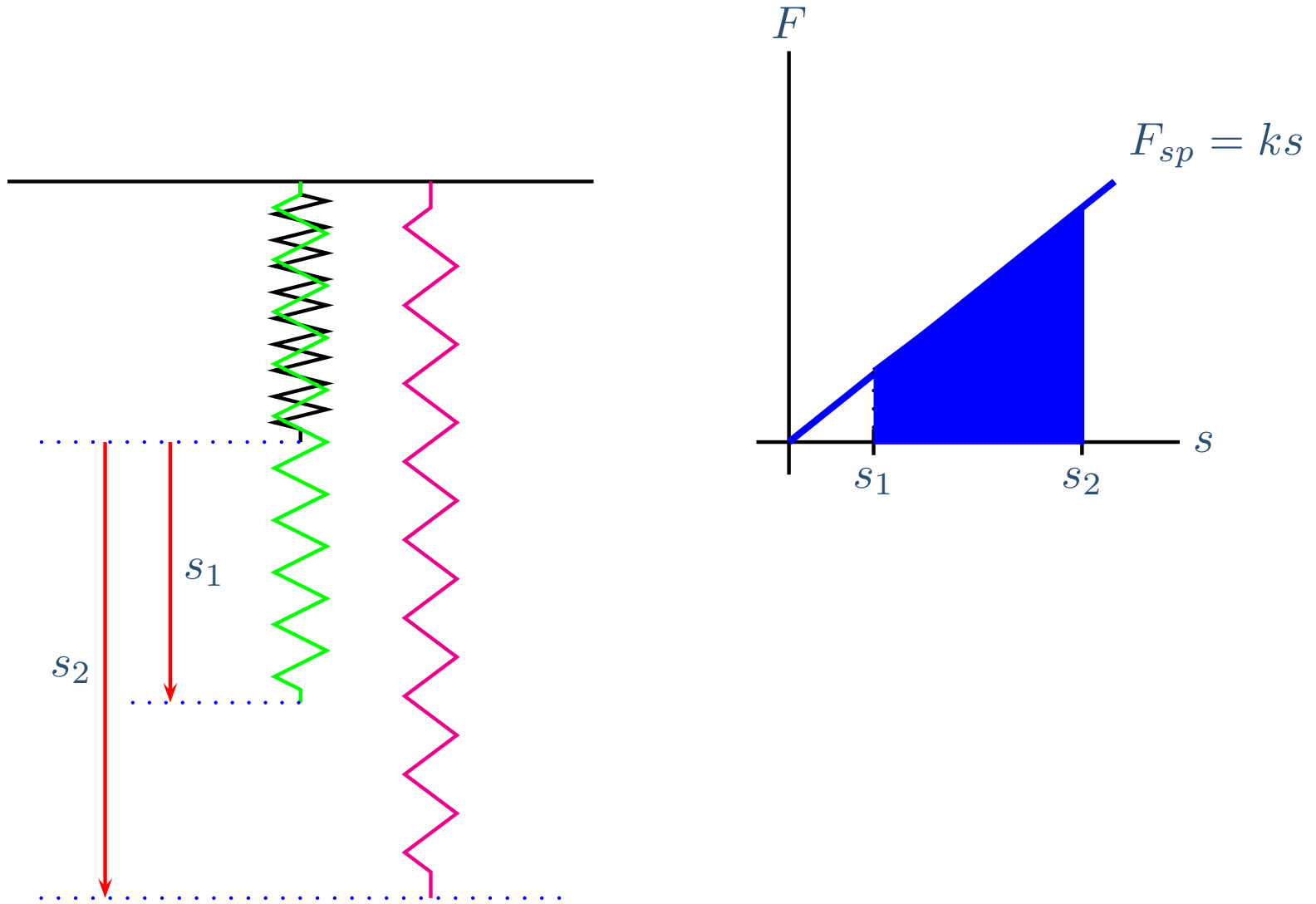
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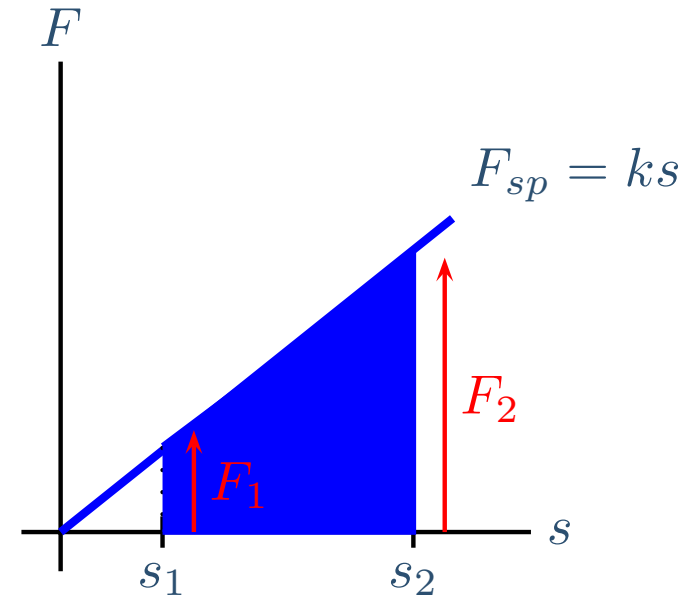
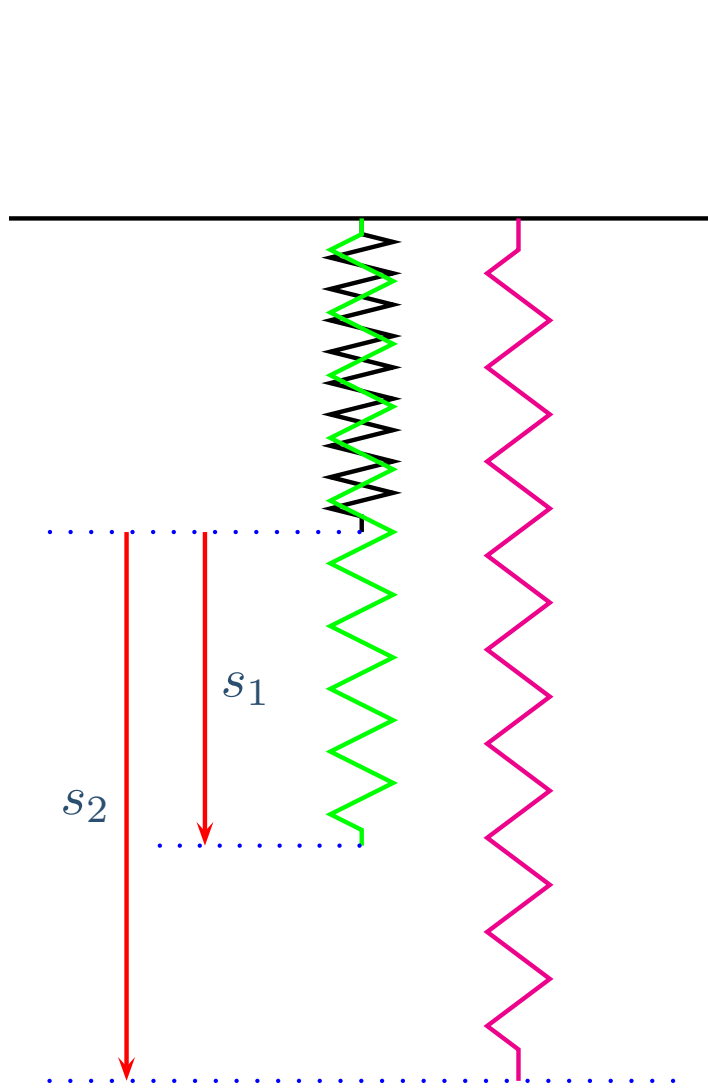
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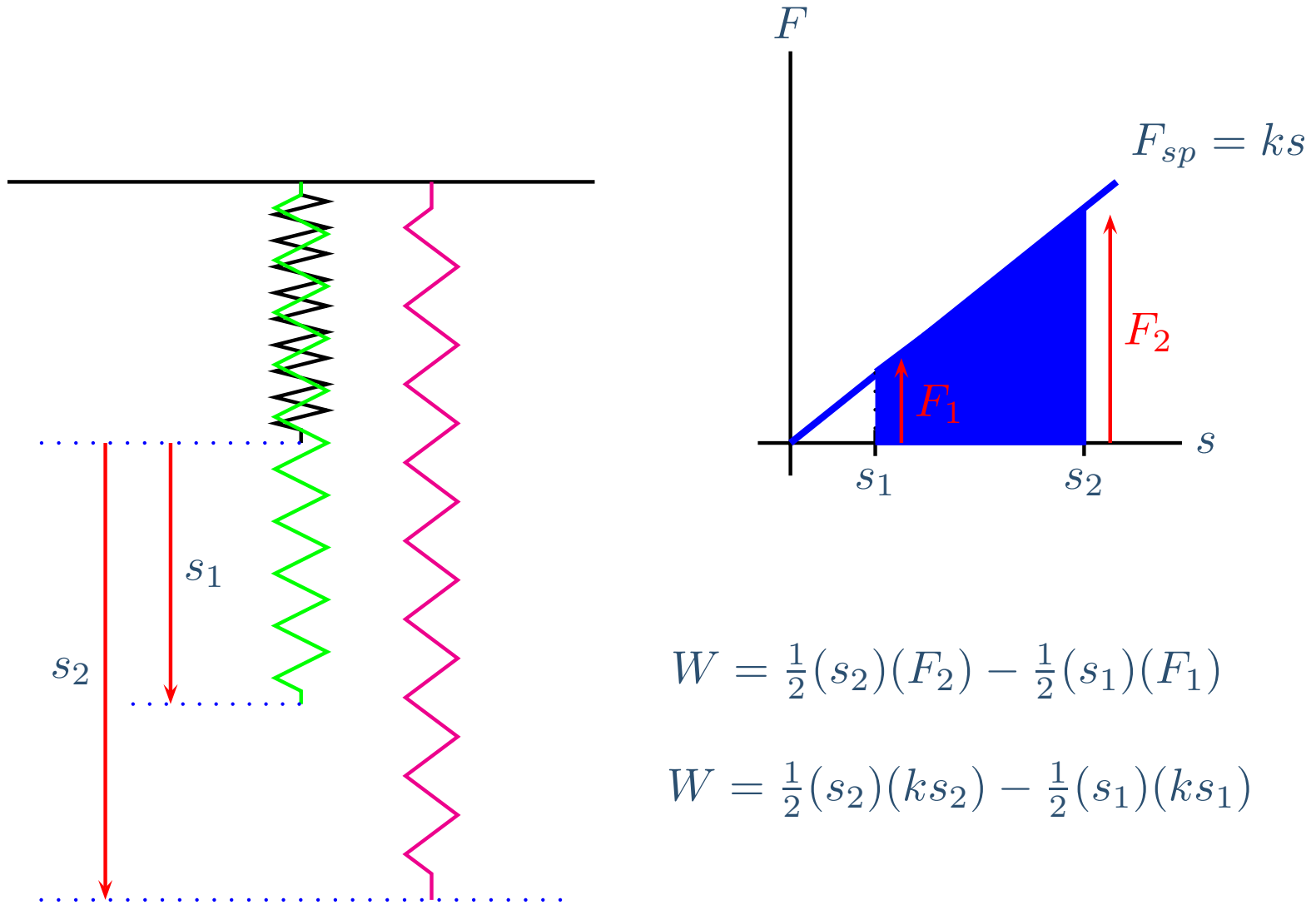


Work to Stretch a Spring



$$W = \frac{1}{2}(s_2)(F_2) - \frac{1}{2}(s_1)(F_1)$$

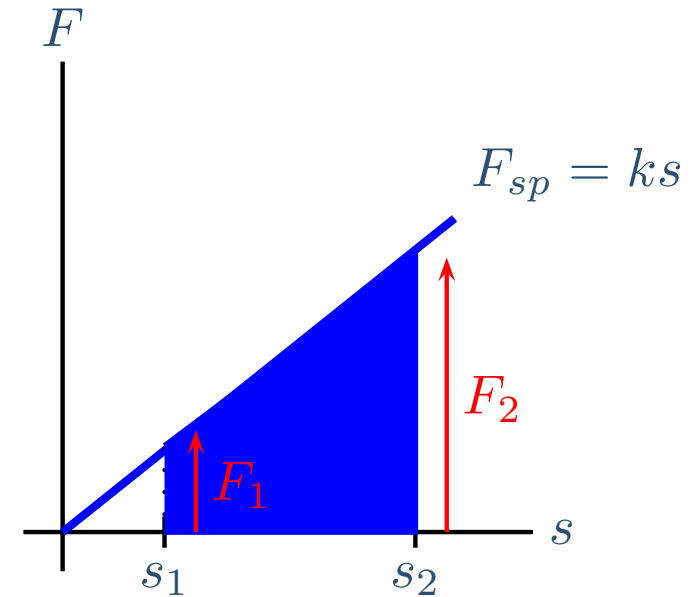
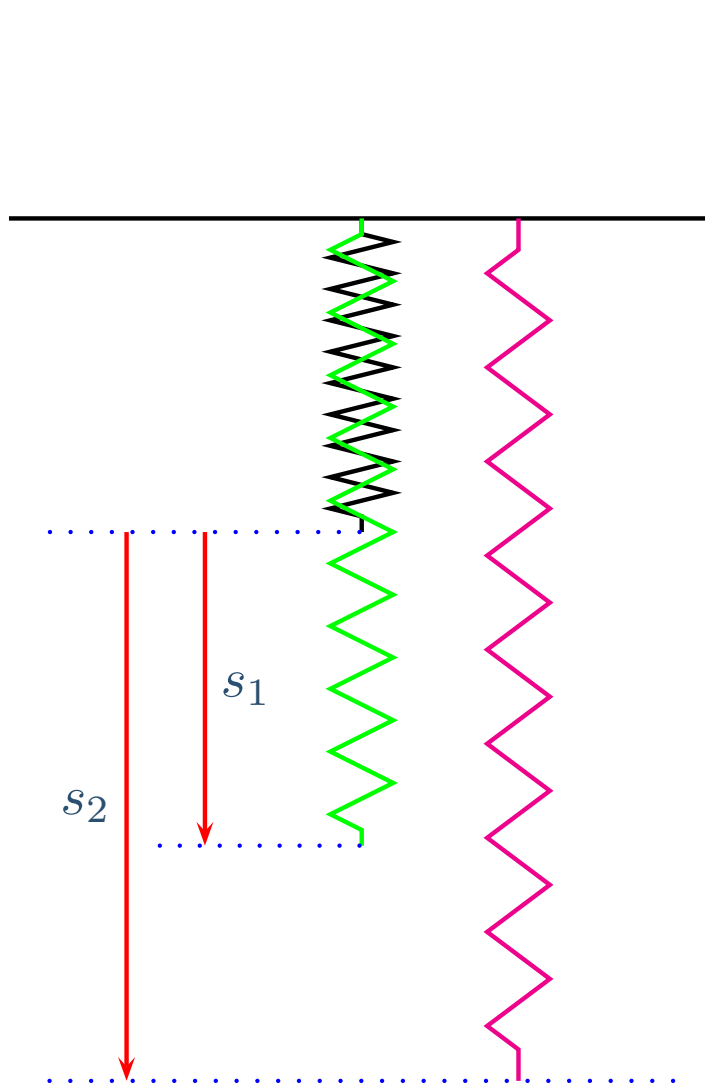
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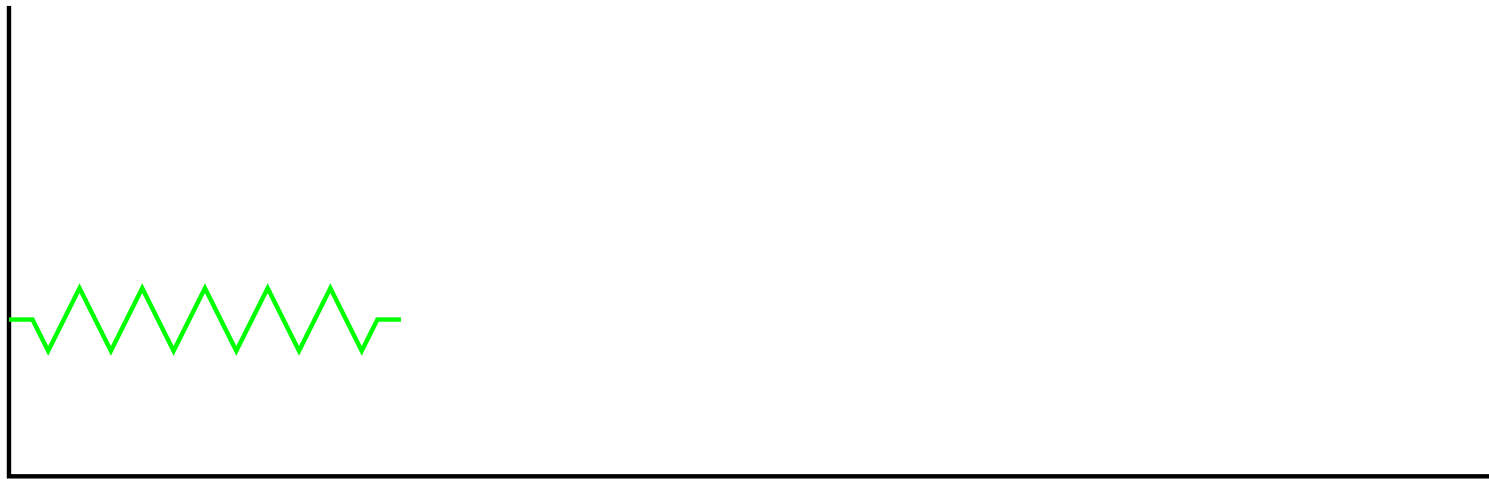
$$W = \frac{1}{2}ks_2^2 - \frac{1}{2}ks_1^2$$

Elastic Potential Energy

Elastic Potential energy - Potential energy due to a spring.

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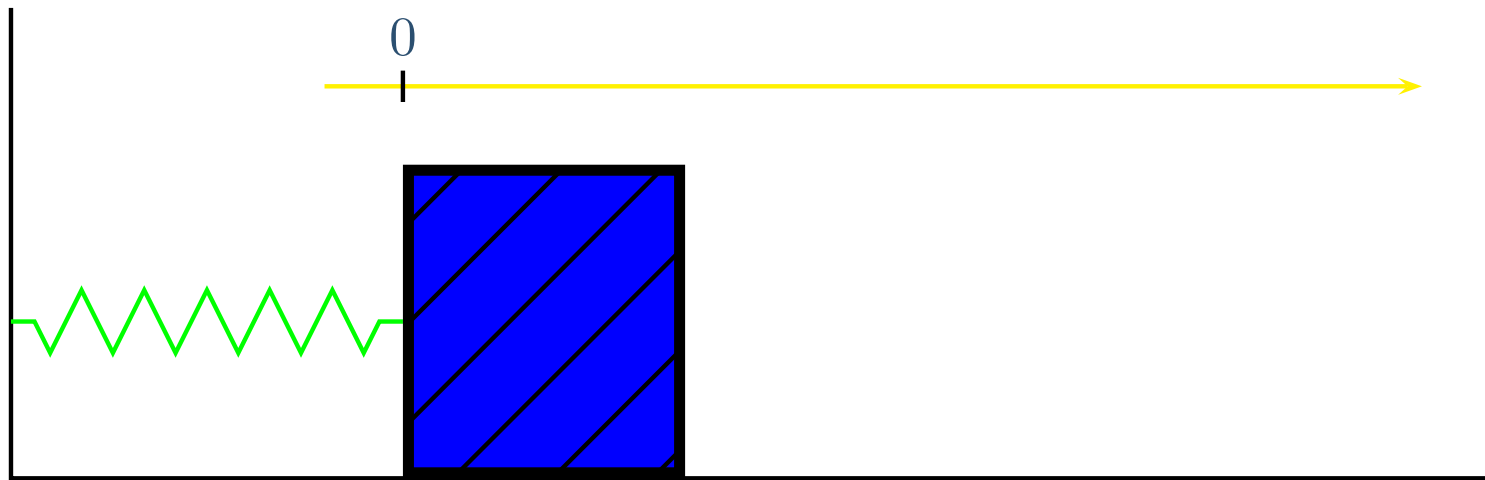
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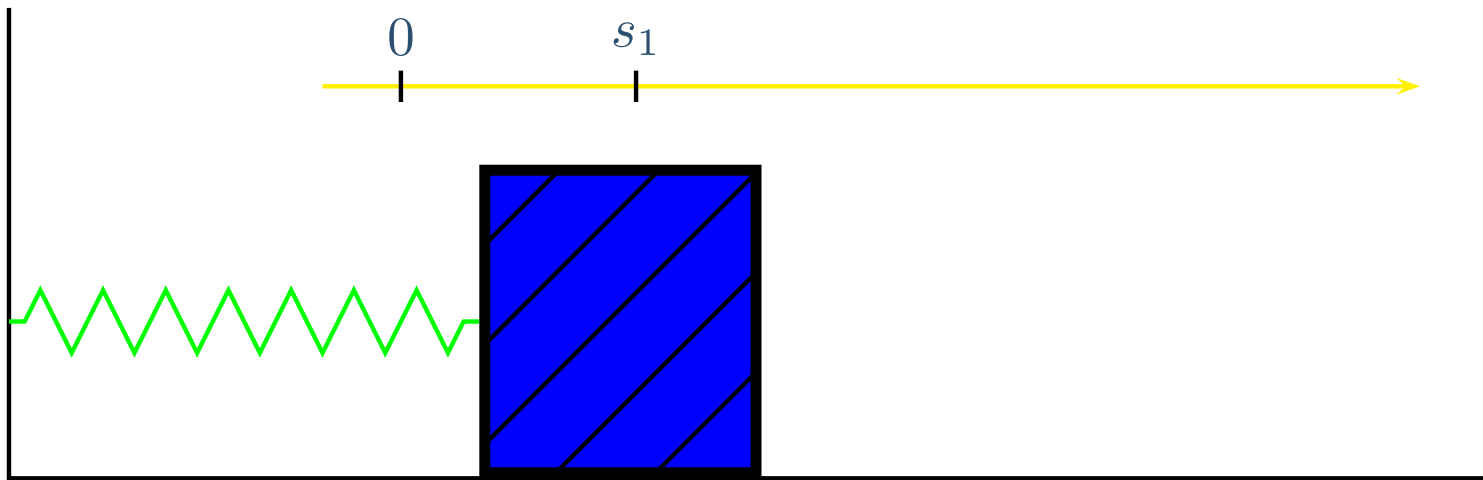
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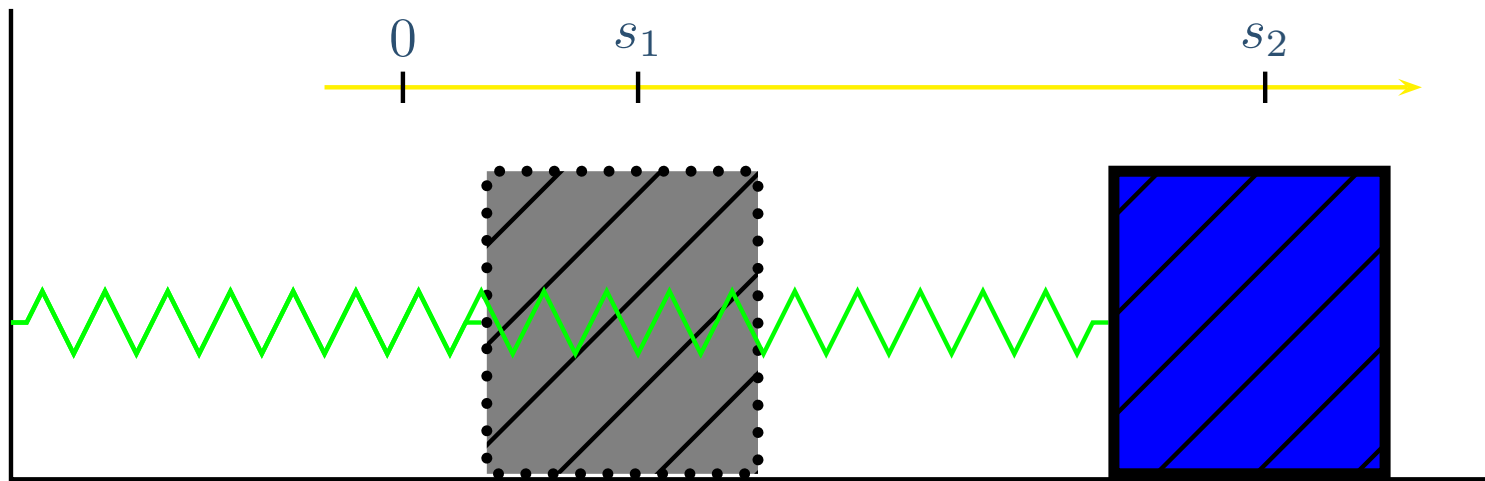
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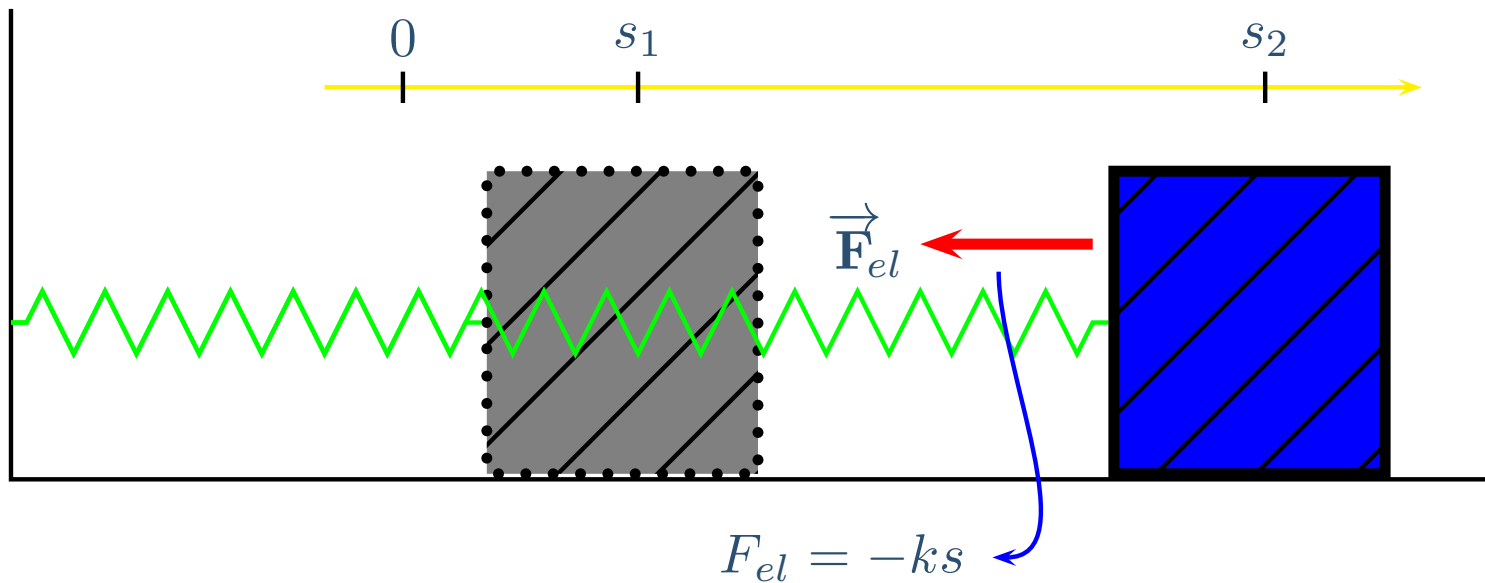
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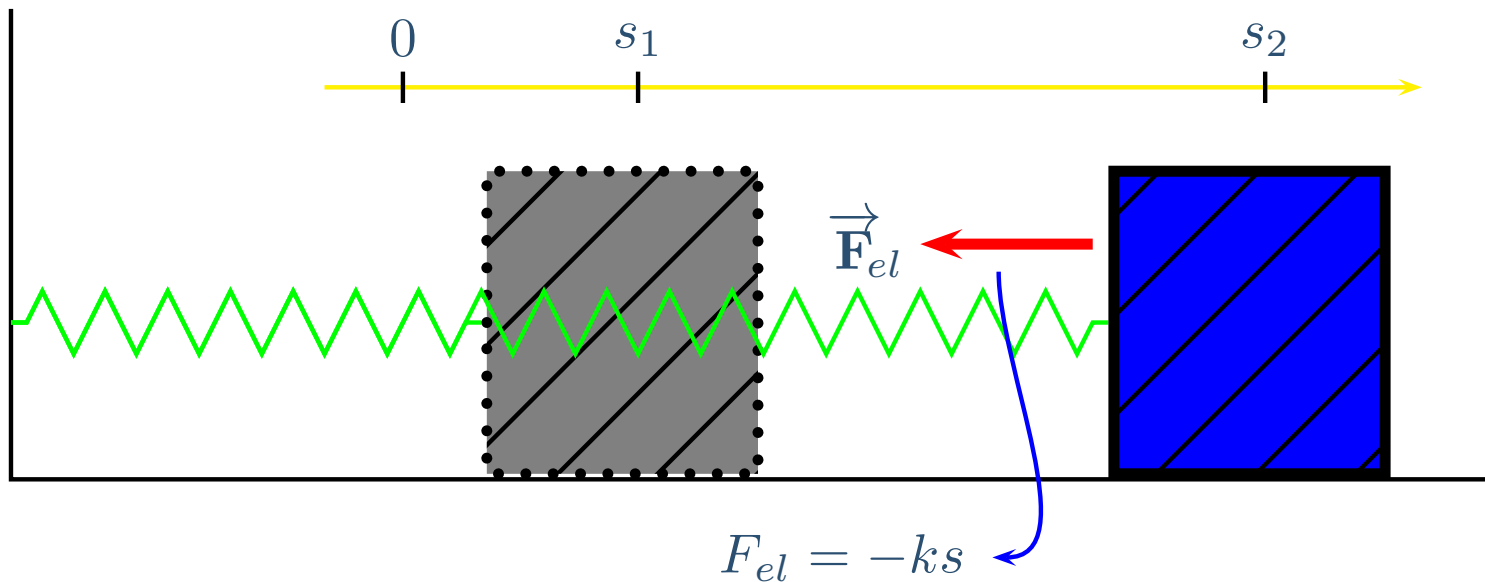
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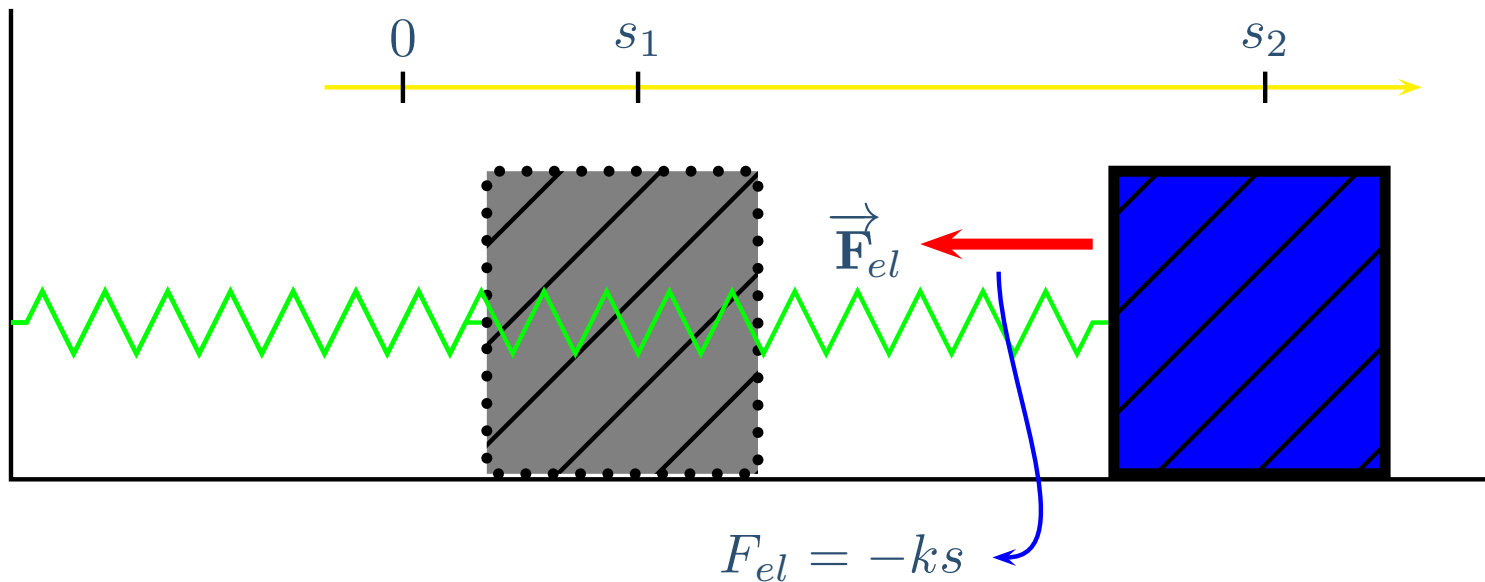
$W_{el} = - \left(\frac{1}{2}ks_2^2 - \frac{1}{2}ks_1^2 \right)$ - Elastic work converted to potential energy



Elastic Potential Energy

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$$W_{el} = - \left(\frac{1}{2} k s_2^2 - \frac{1}{2} k s_1^2 \right) - \text{Elastic work converted to potential energy}$$



$$W_{el} = -\Delta U_{el} \Rightarrow U_{el} = \frac{1}{2} k s^2$$

Conservation of Elastic Energy

If a spring is the only force doing work on something,

$$E_1 = E_2$$

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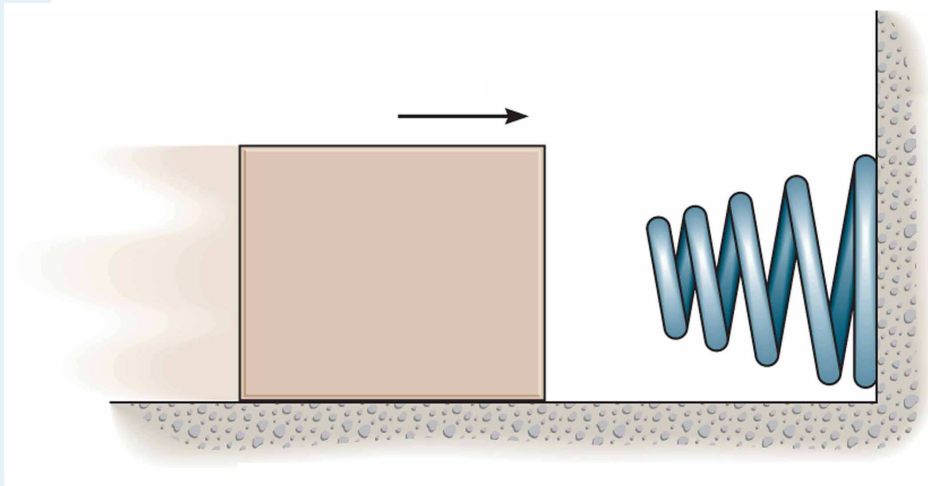
$$E_1 = E_2$$

$$E = K + U_{el} = \frac{1}{2}mv^2 + \frac{1}{2}ks^2$$

$$\frac{1}{2}mv_1^2 + \frac{1}{2}ks_1^2 = \frac{1}{2}mv_2^2 + \frac{1}{2}ks_2^2$$

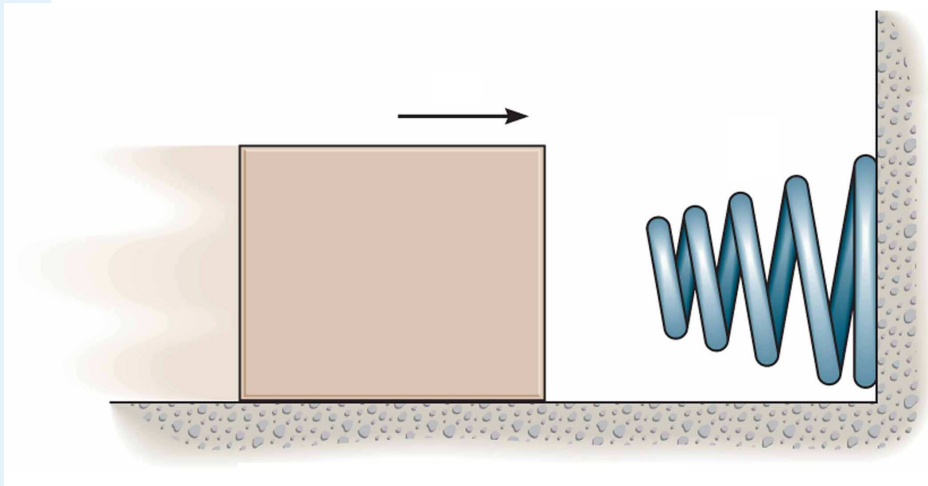
Elastic Potential Energy Exercise

A 10 kg mass slides across a frictionless, horizontal floor going 5 m/s (and therefore has 125 J of kinetic energy) when it collides with the $k = 500\text{ N/m}$ spring shown. What is the maximum compression of the spring?



Elastic Potential Energy Exercise

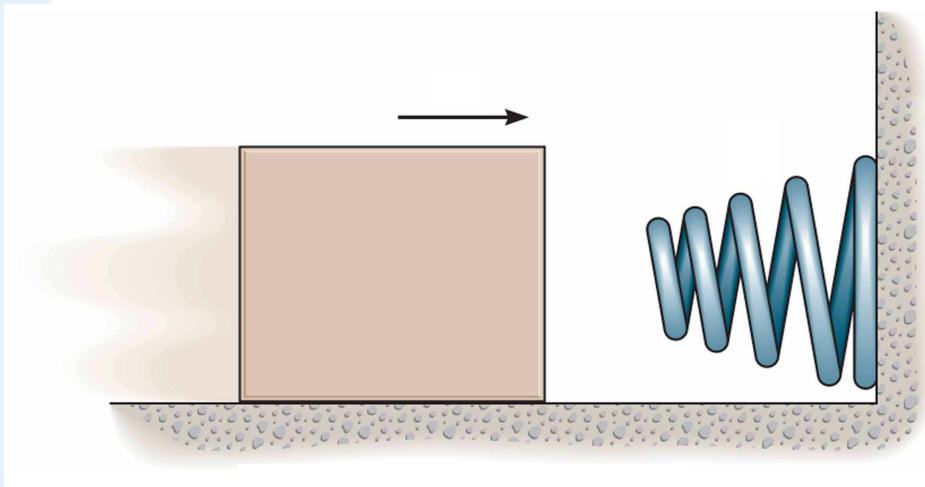
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$$(a) \frac{125\text{ J}}{500\text{ N/m}} = 0.25\text{ m}$$

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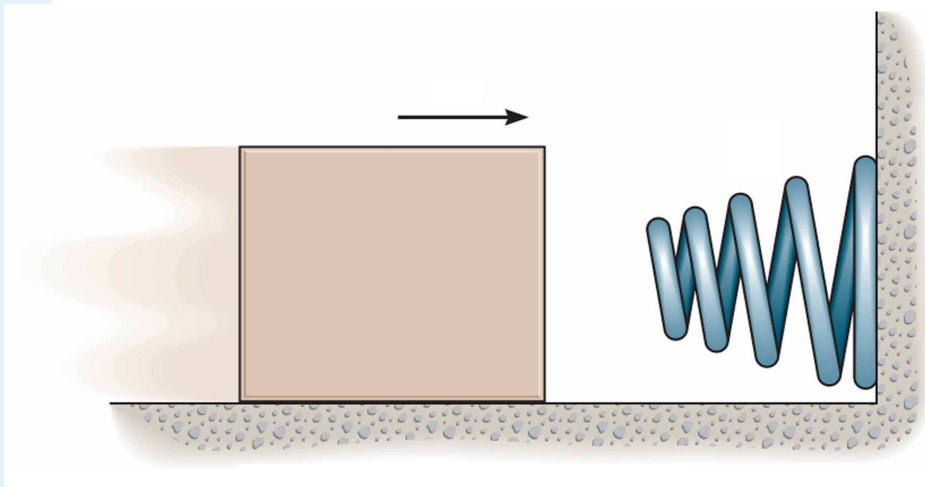


$$(a) \frac{125\text{ J}}{500\text{ N/m}} = 0.25\text{ m}$$

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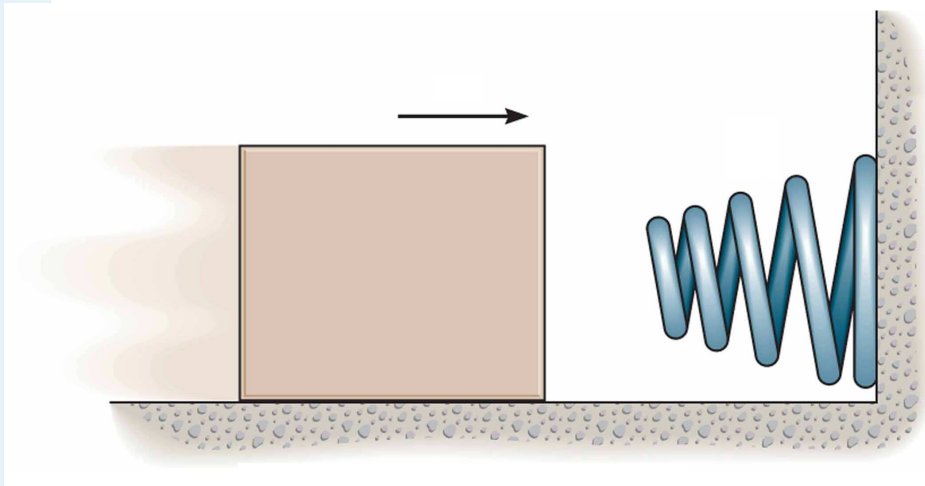
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(b) $\frac{50\text{ kg} \cdot \text{m/s}}{500\text{ N/m}} = 0.1\text{ m}$

(c) $\frac{125\text{ J}}{250\text{ N/m}} = 0.5\text{ m}$

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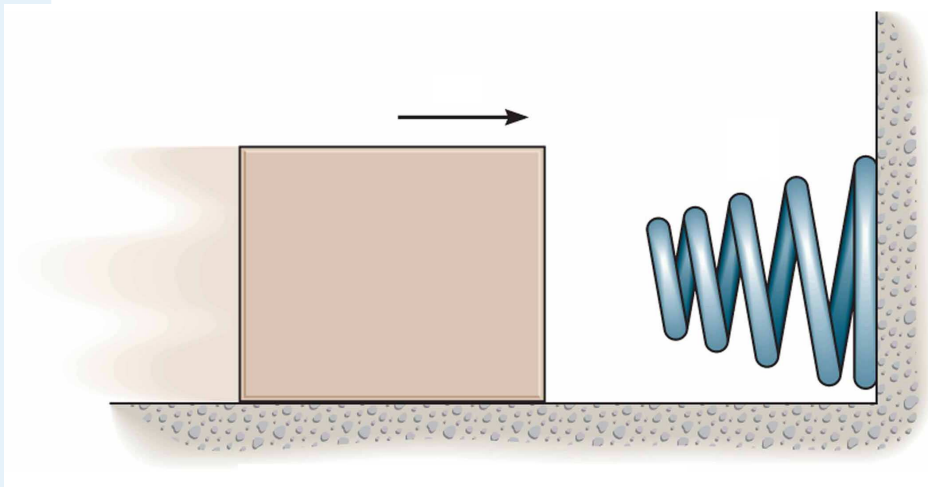
(b) $\frac{50\text{ kg} \cdot \text{m/s}}{500\text{ N/m}} = 0.1\text{ m}$

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(d) $\sqrt{\frac{125\text{ J}}{250\text{ N/m}}} = 0.7071\text{ m}$

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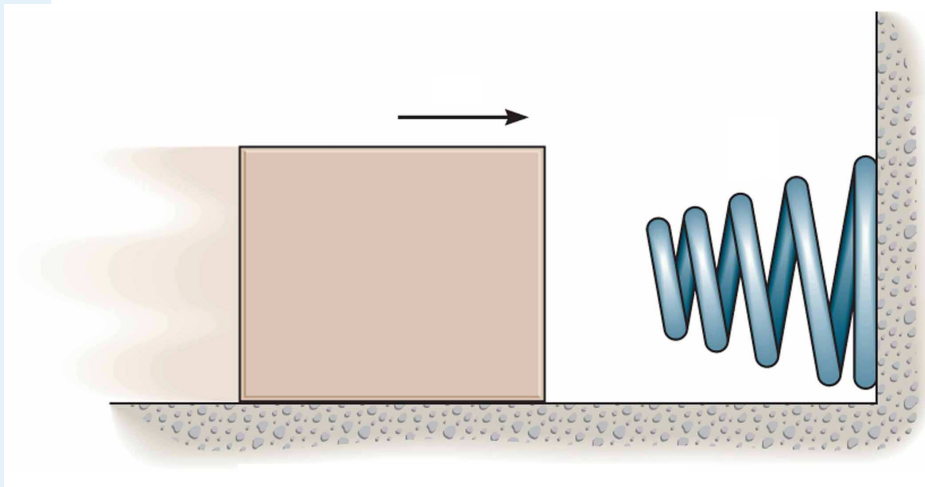
(c) $\frac{125\text{ J}}{250\text{ N/m}} = 0.5\text{ m}$

(e) $\sqrt{\frac{125\text{ J}}{500\text{ N/m}}} = 0.5\text{ m}$

(d) $\sqrt{\frac{125\text{ J}}{250\text{ N/m}}} = 0.7071\text{ m}$

Elastic Potential Energy Exercise

A 10 kg mass slides across a frictionless, horizontal floor going 5 m/s (and therefore has 125 J of kinetic energy) when it collides with the $k = 500\text{ N/m}$ spring shown. What is the maximum compression of the spring?



(a) $\frac{125\text{ J}}{500\text{ N/m}} = 0.25\text{ m}$

(b) $\frac{50\text{ kg} \cdot \text{m/s}}{500\text{ N/m}} = 0.1\text{ m}$

(c) $\frac{125\text{ J}}{250\text{ N/m}} = 0.5\text{ m}$

(e) $\sqrt{\frac{125\text{ J}}{500\text{ N/m}}} = 0.5\text{ m}$

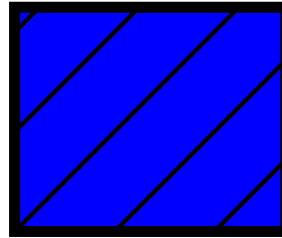
(d) $\sqrt{\frac{125\text{ J}}{250\text{ N/m}}} = 0.7071\text{ m}$

General Energy Problems

The most general problems (this term) involve gravity, springs, and other forces all doing work.

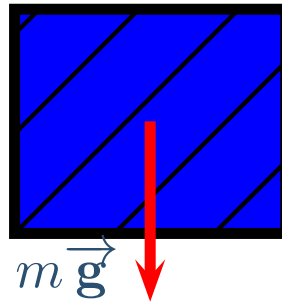
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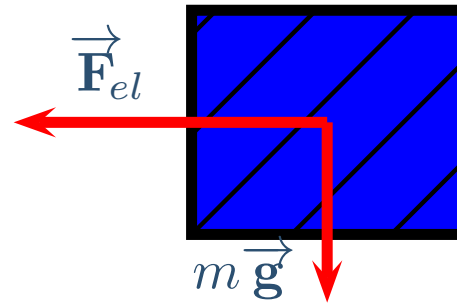
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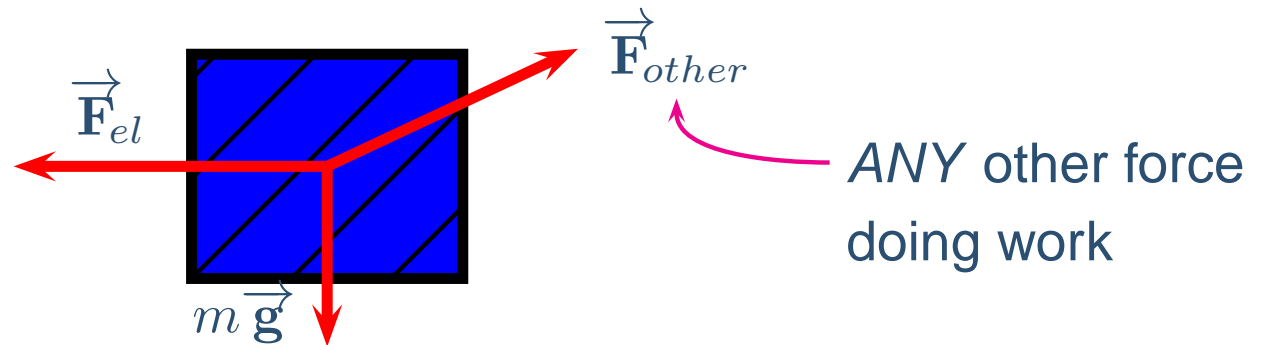
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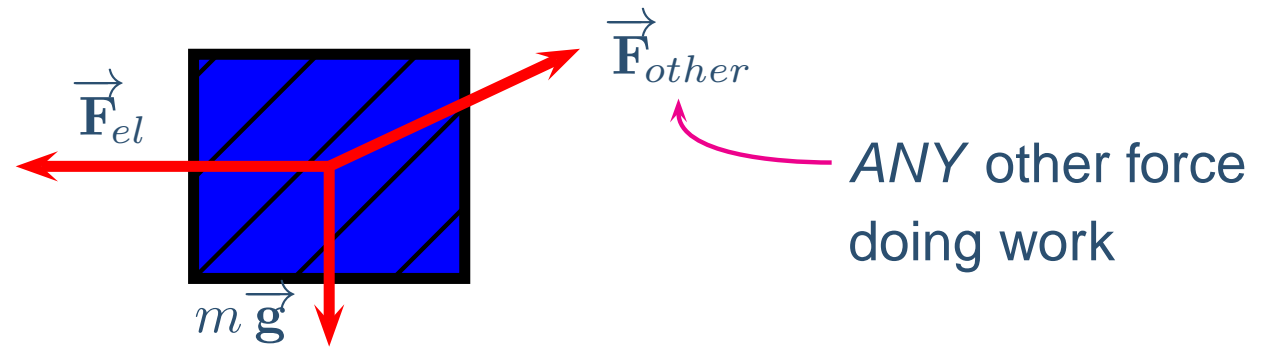
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General Energy Problems

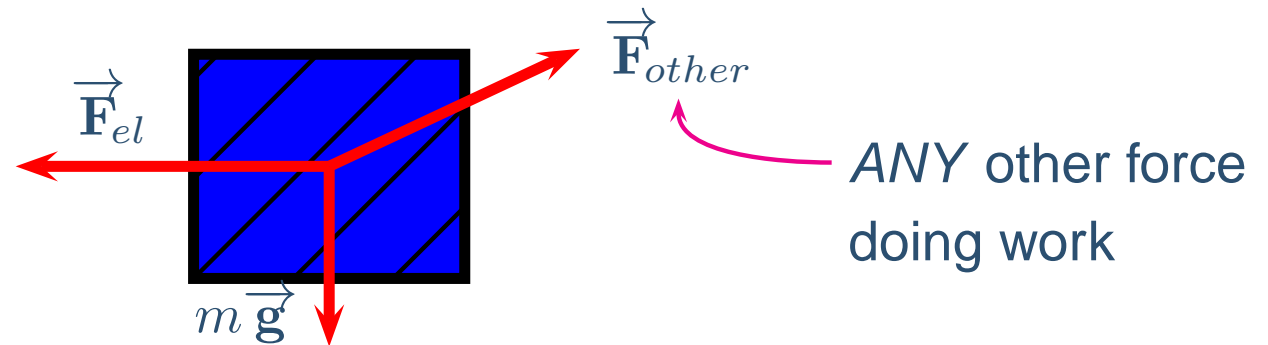
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$$W_{total} = W_g + W_{el} + W_{other}$$

General Energy Problems

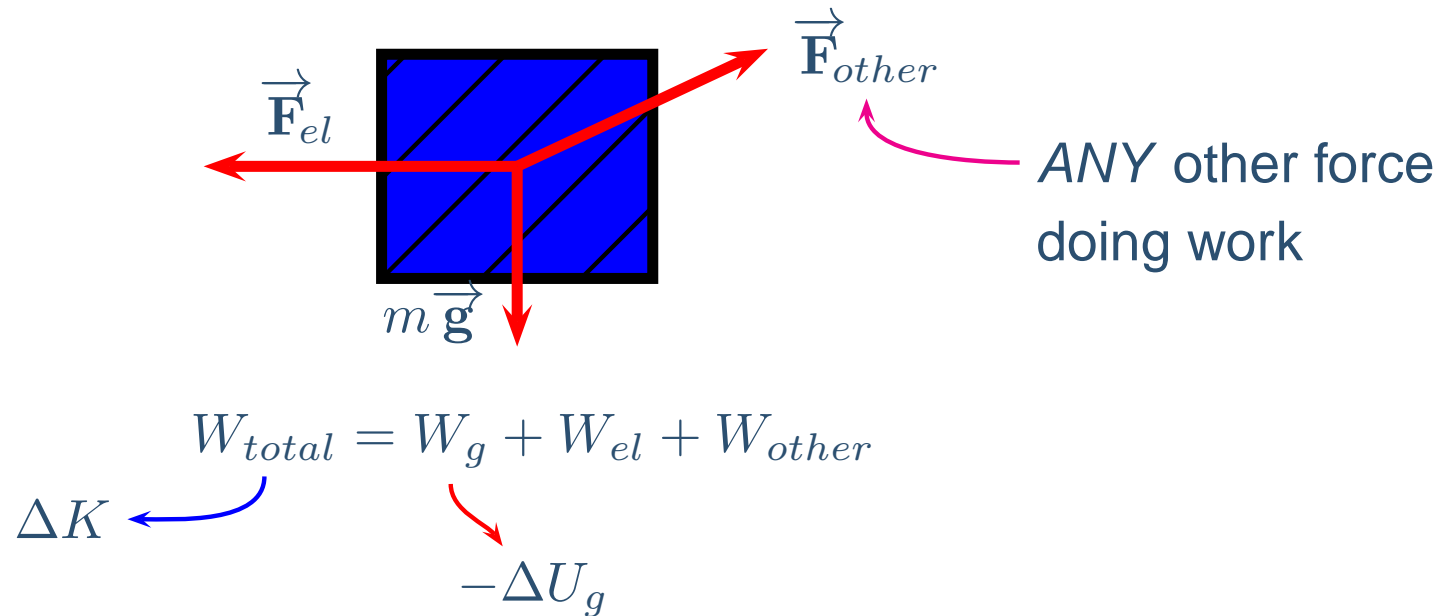
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$$\Delta K \leftarrow W_{total} = W_g + W_{el} + W_{other}$$

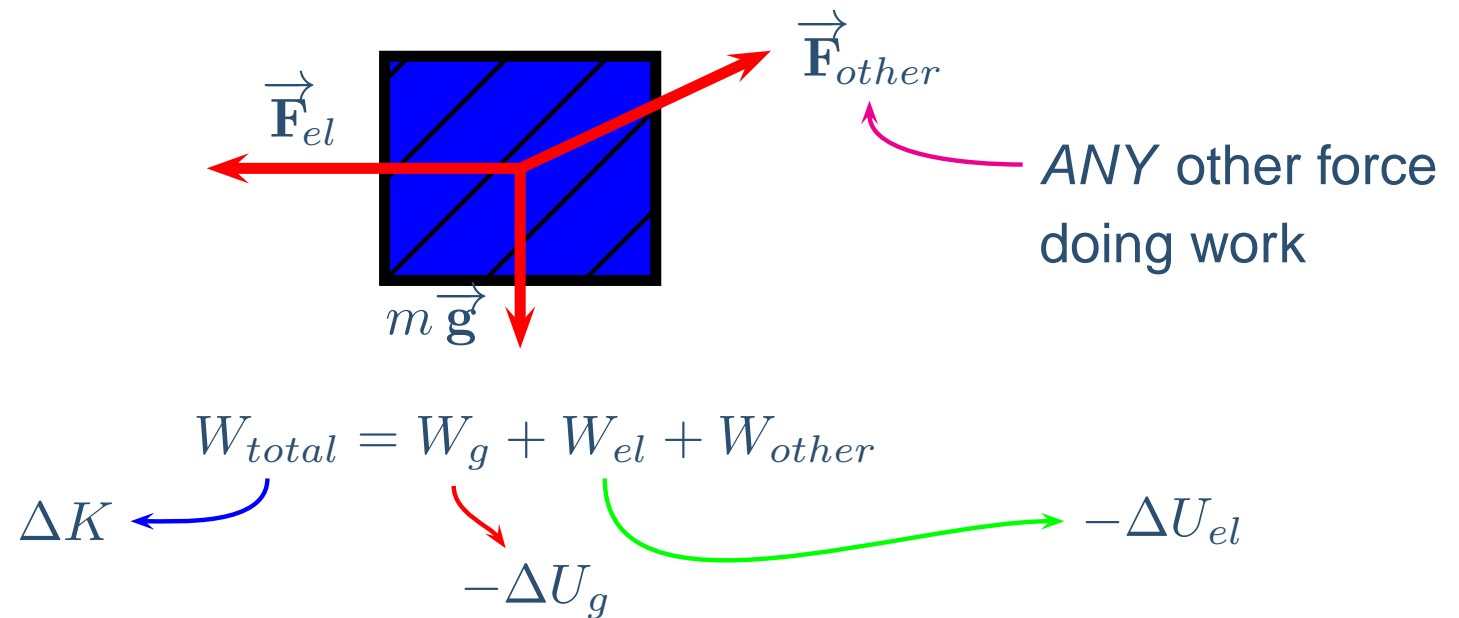
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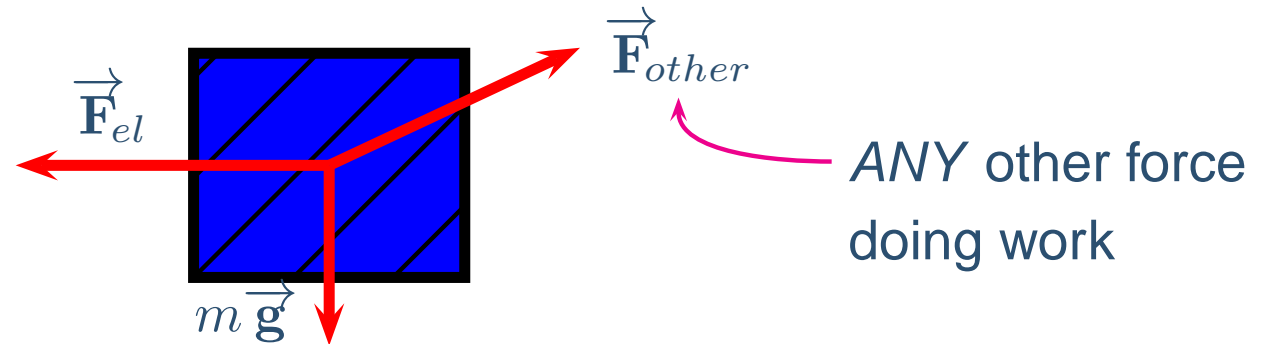
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$$W_{total} = W_g + W_{el} + W_{other}$$

ΔK ← (blue arrow from W_{total})

← (red arrow from W_g) $-\Delta U_g$

← (green arrow from W_{el}) $-\Delta U_{el}$

$$\frac{1}{2}mv_i^2 + mgy_i + \frac{1}{2}ks_i^2 + W_{other} = \frac{1}{2}mv_f^2 + mgy_f + \frac{1}{2}ks_f^2$$