

March 18, Week 9

Today: Finish Chapter 6 and begin Chapter 7, Energy

Homework Assignment #6 - Due Friday, March 22

Mastering Physics: 9 problems from chapters 5 and 6

Written Questions: 6.73

Exams and Midterm grades are in your mailbox. Exam #2 grade is on white sheet.

If interested in Physics 110, you can still start attending tomorrow

Help sessions with Jonathan:

M: 1000-1100, RH 111

T: 1000-1100, RH 114

Th: 0900-1000, RH 114

Work Review

Work - How much effort goes into causing motion.

Unit: $N \cdot m = kg \cdot m^2/s^2 = J$.

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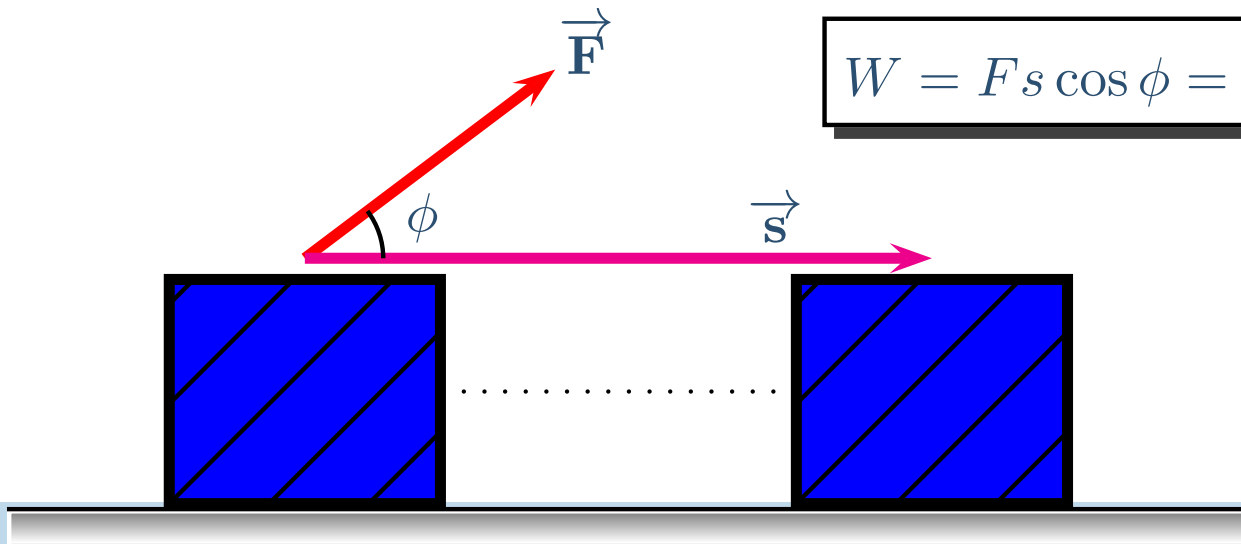
Unit: $N \cdot m = kg \cdot m^2/s^2 = J$.

For Constant Force and Straight-line Motion:

\vec{s} = displacement
= distance and direction

ϕ = angle between \vec{F} and \vec{s}

$$W = F s \cos \phi = \vec{F} \cdot \vec{s}$$



Variable Forces

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Constant Force, $W = Fs$



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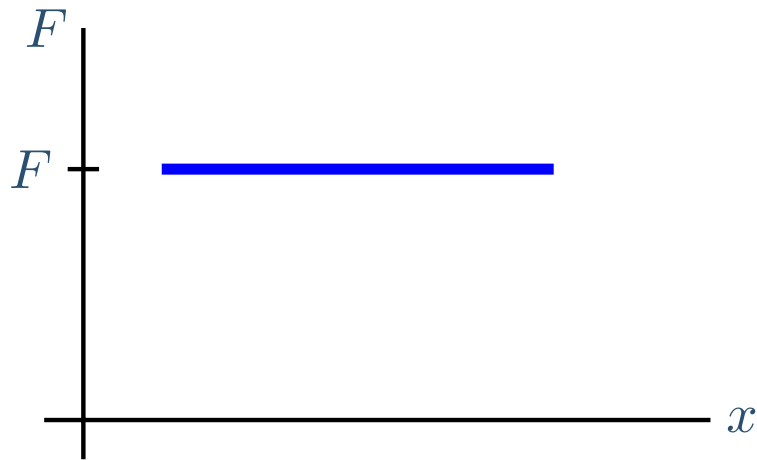
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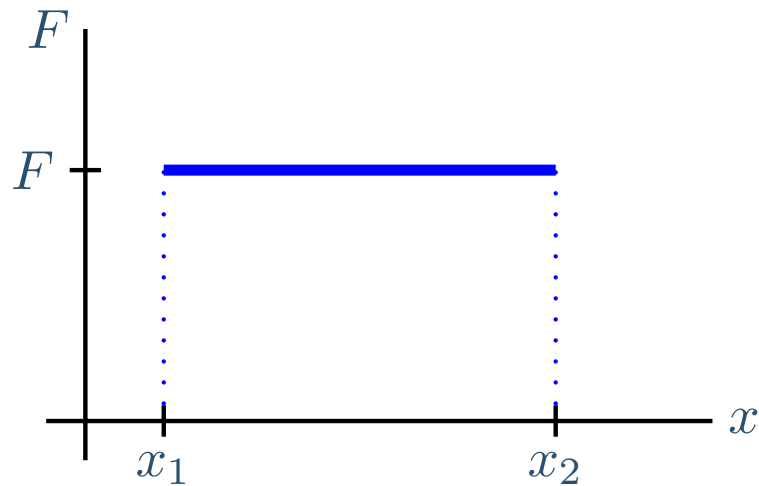
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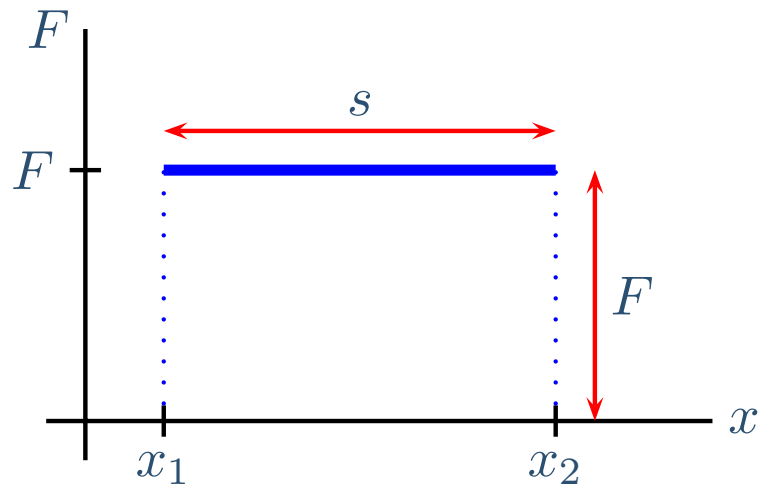
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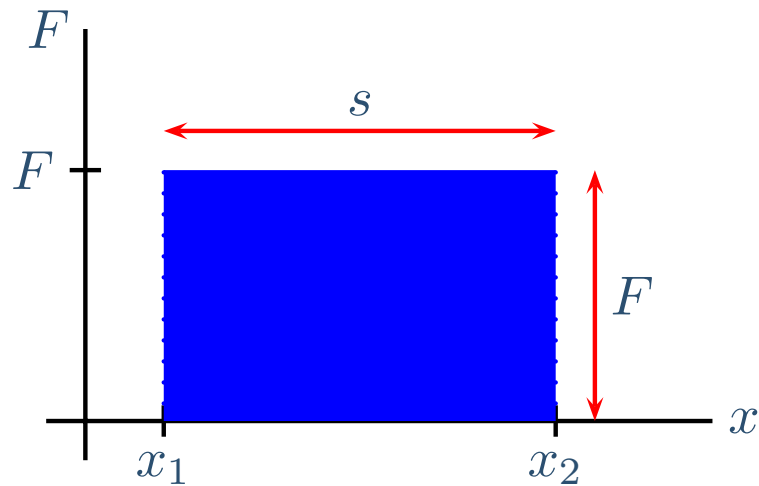
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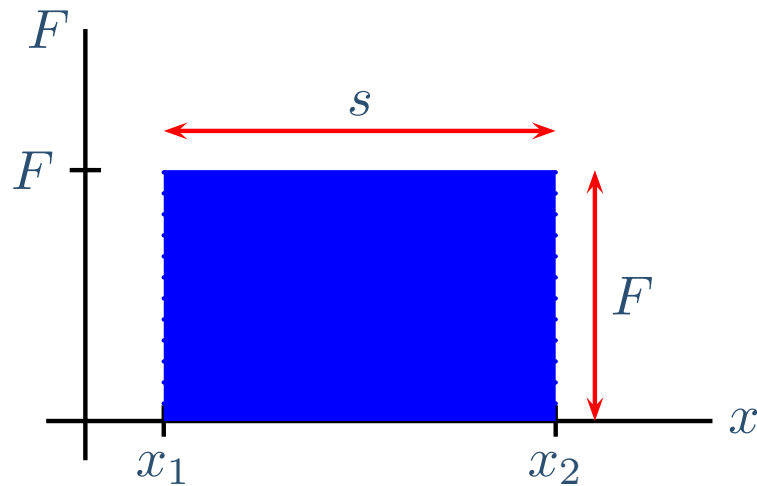
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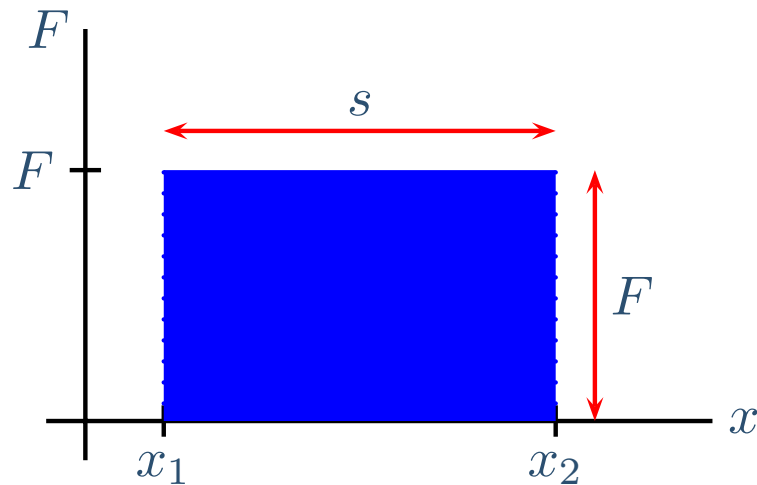
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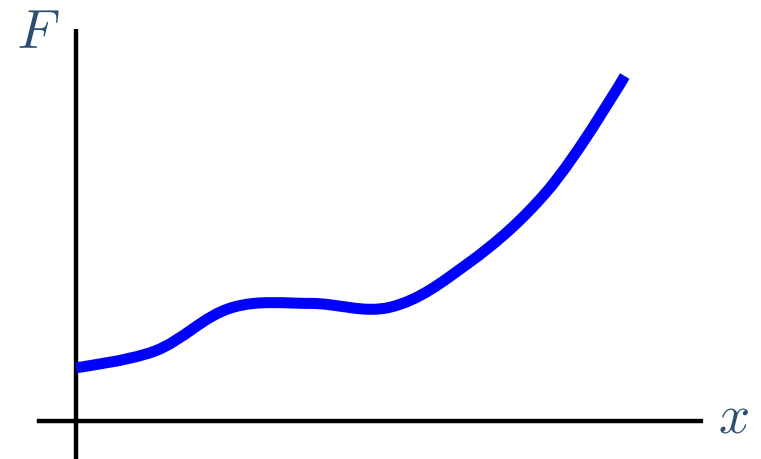
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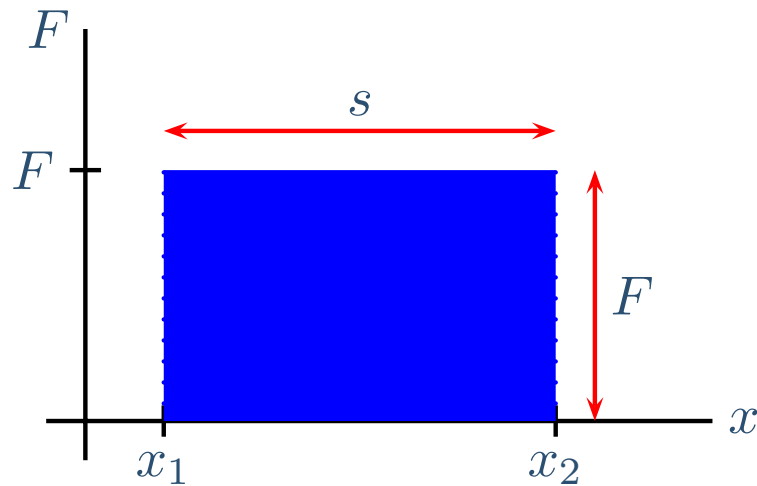
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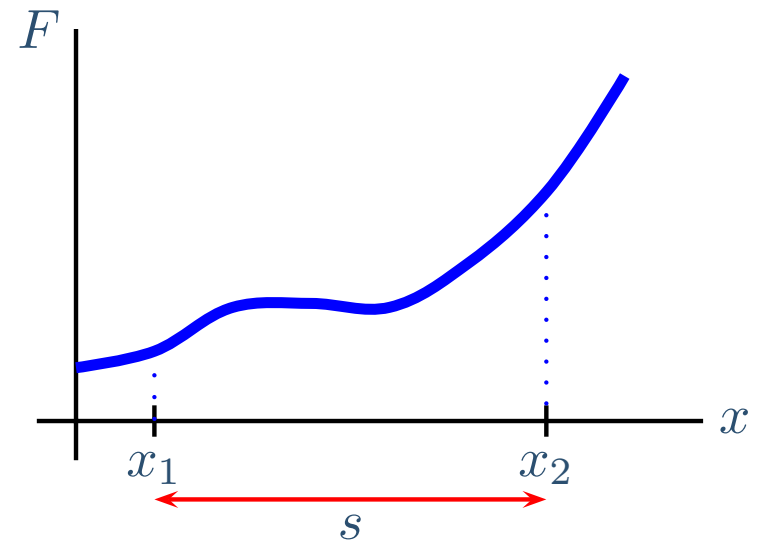
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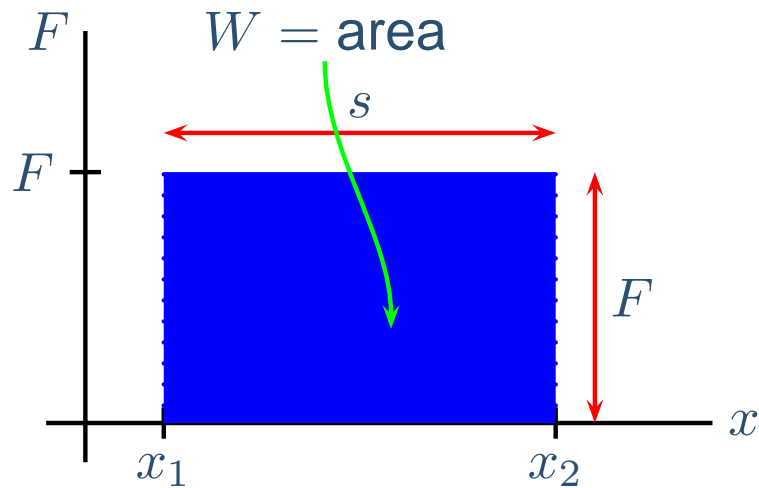
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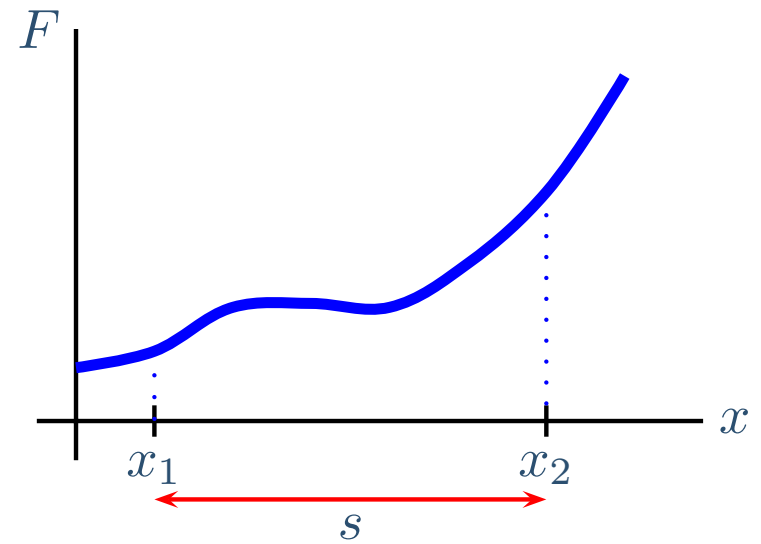
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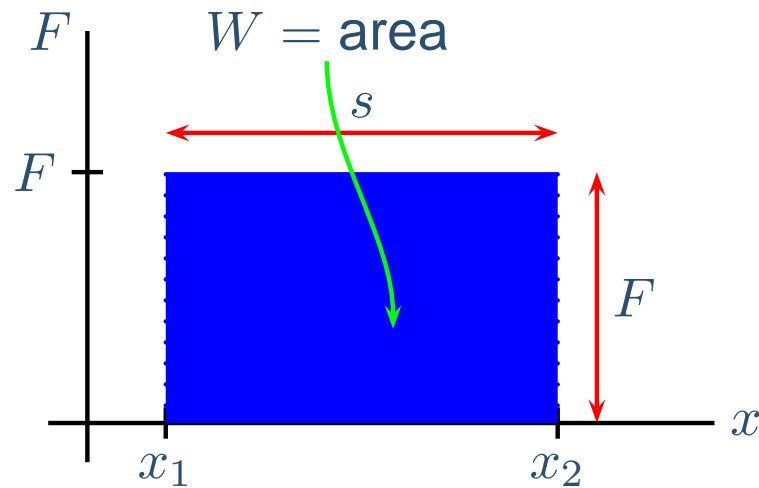
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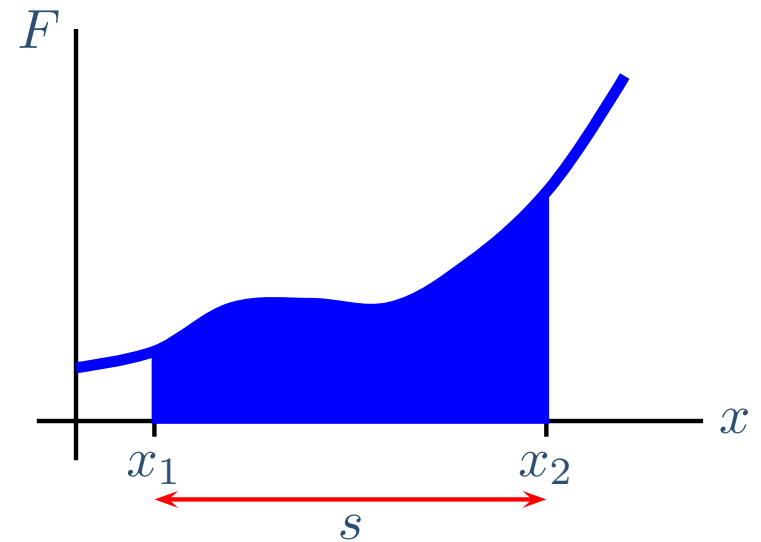
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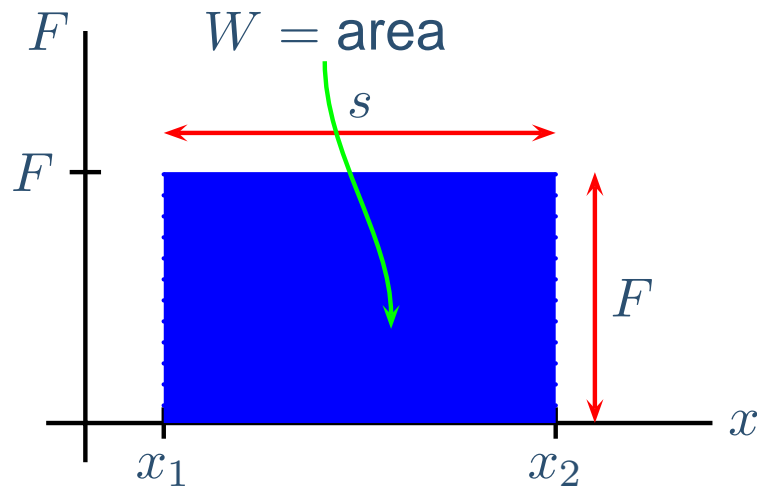
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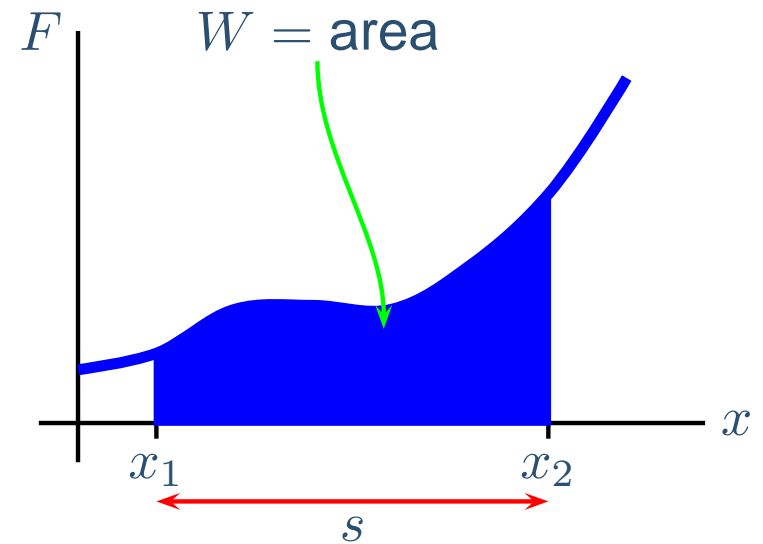
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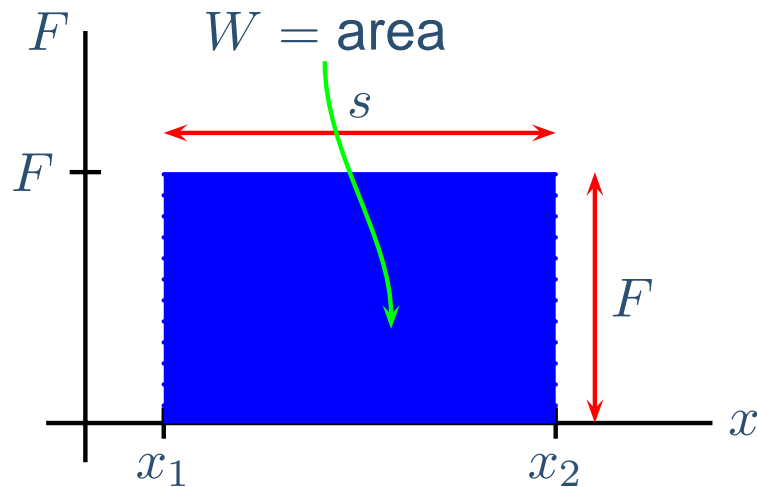
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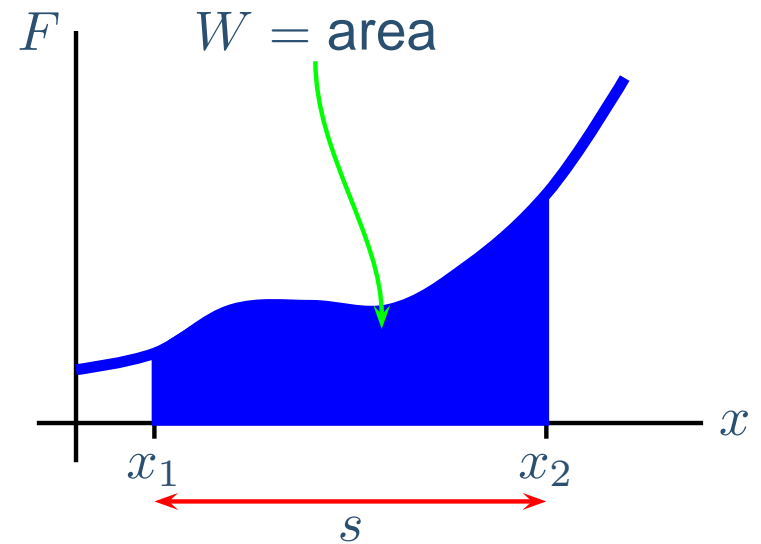
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Variable Force



For any type of force, it can be shown that the work-energy theorem holds!

$$W_{total} = \Delta K = \frac{1}{2}mv_2^2 - \frac{1}{2}mv_1^2$$

Power

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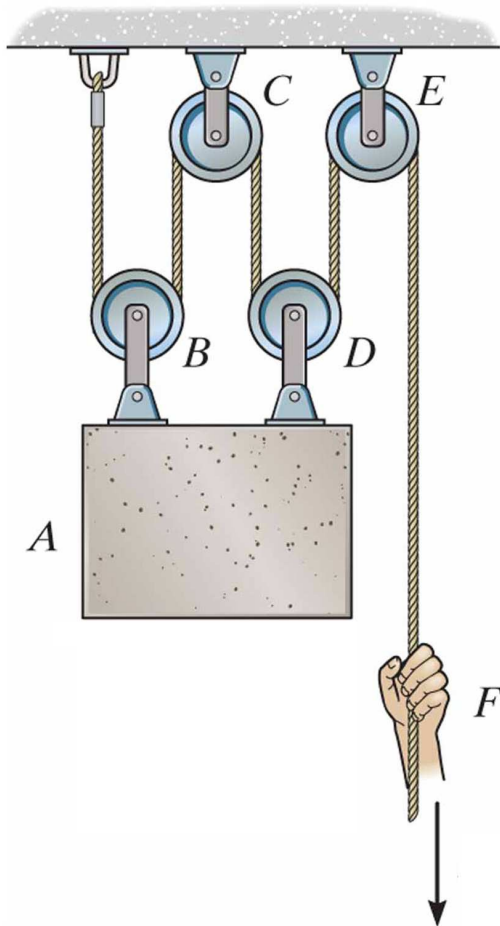
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$$1 \text{ hp} = 550 \text{ lb} \cdot \text{ft}/s = 746 \text{ Watt}$$

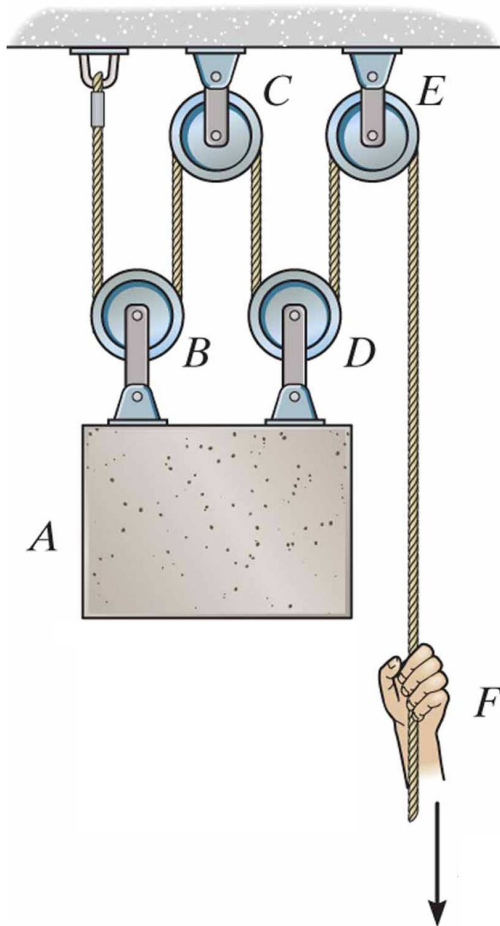
Power Exercise

The power supplied by the person pulling the rope can't exceed the power of the rising block! If the person is pulling the rope down at 4 m/s , with what speed is the block rising?



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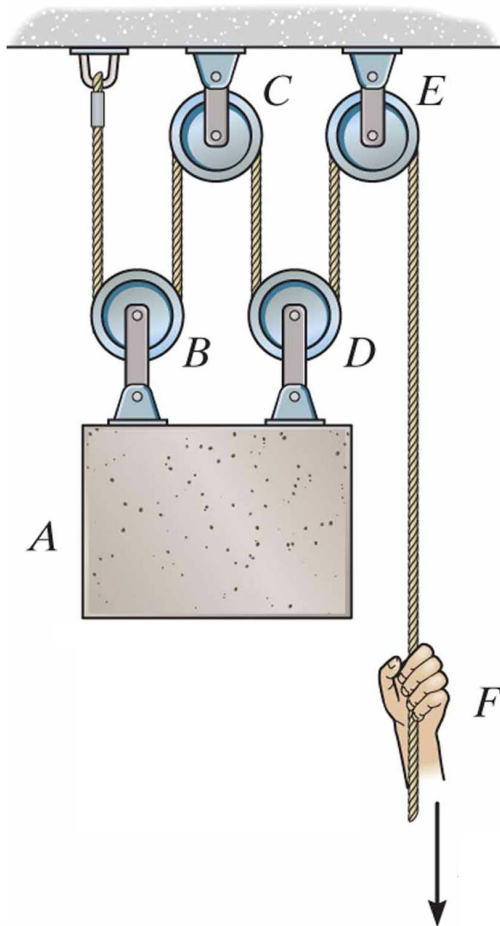
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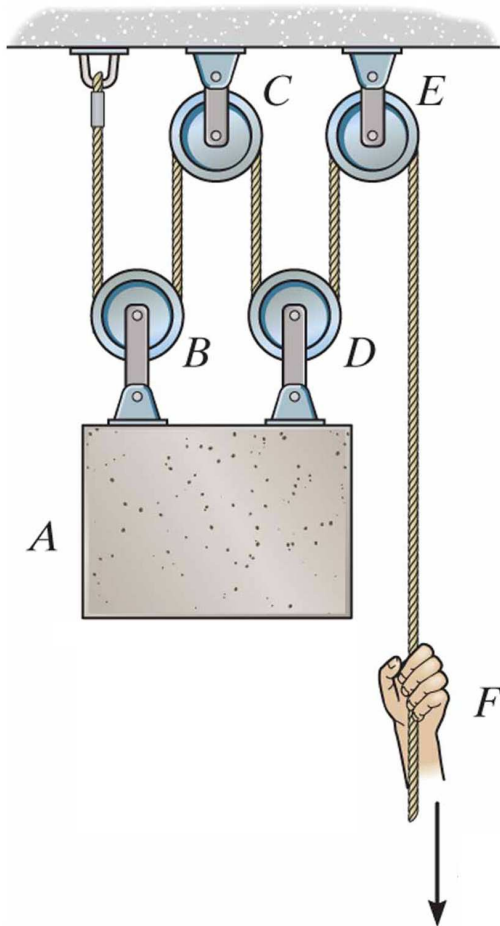


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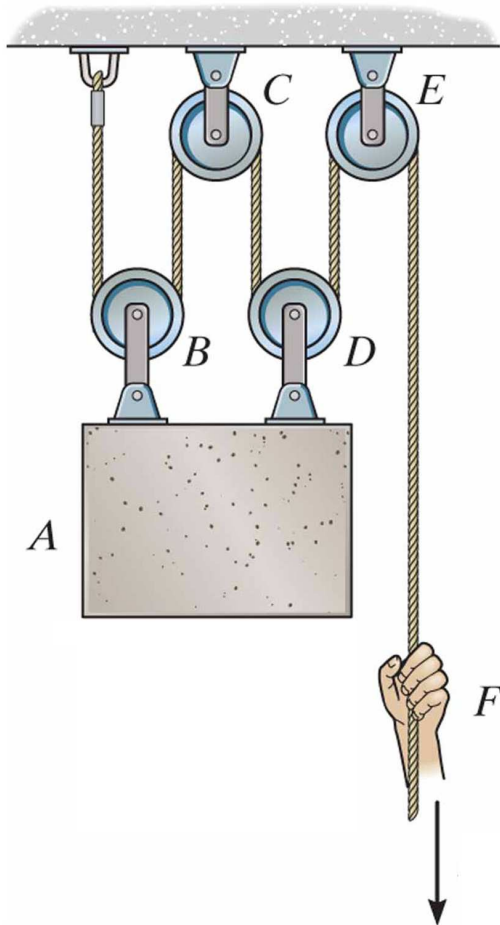
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(c) 2 m/s

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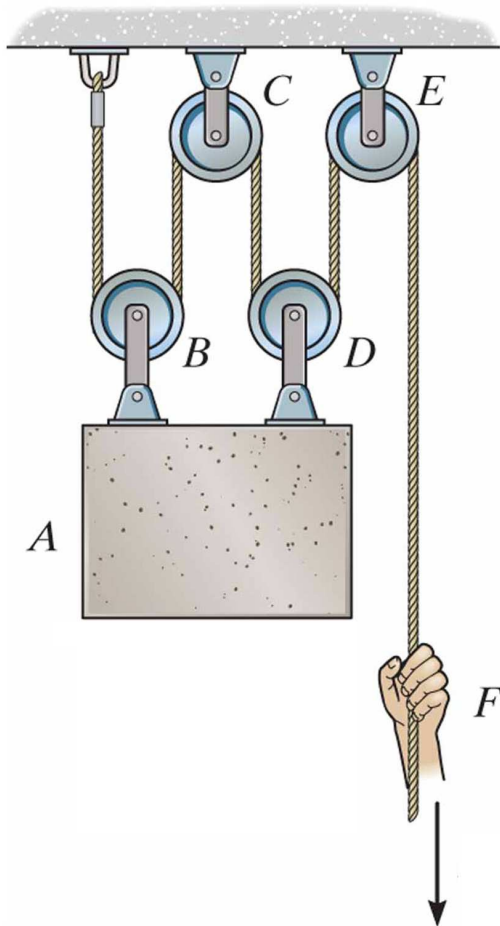
(b) 1 m/s

(c) 2 m/s

(d) 3 m/s

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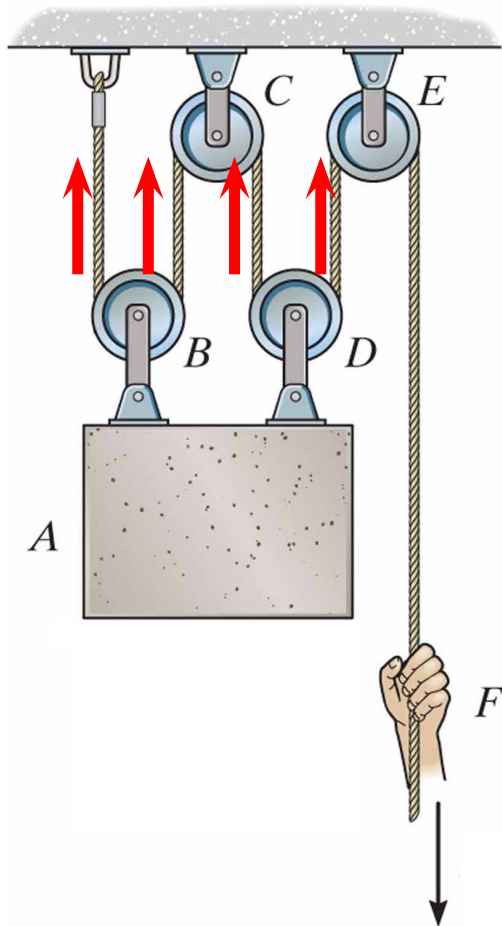
(c) 2 m/s

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(e) 4 m/s

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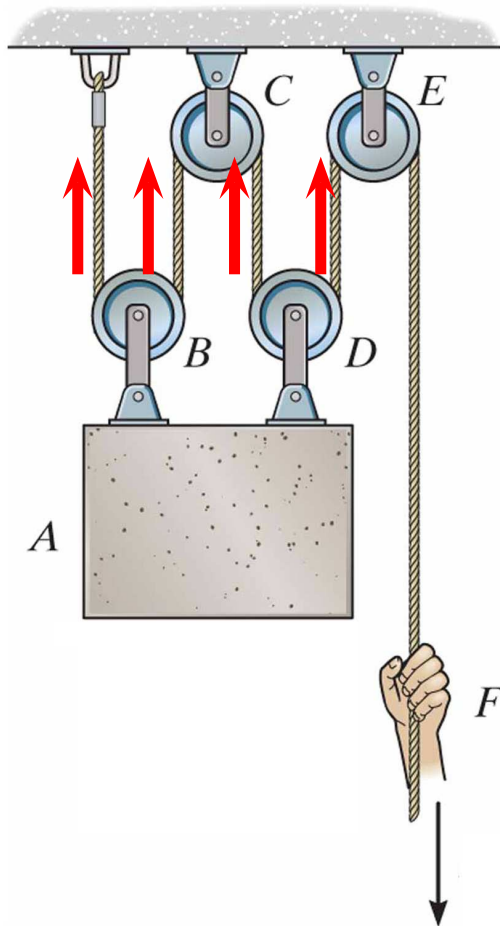
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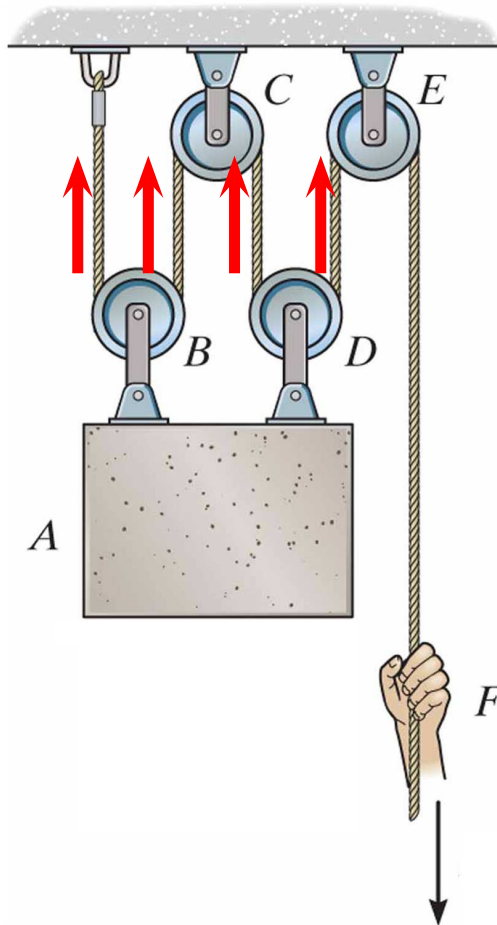
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(e) 4 m/s

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$$P_{Hand} = T(4\text{ m/s}) \text{ (Downwards pull and velocity } \Rightarrow \phi = 0^\circ)$$

$$P_{Block} = (4T)v_{block} \text{ (Upwards force and velocity on block } \Rightarrow \phi = 0^\circ \text{ here too)}$$

$$P_{Hand} = P_{Block} \Rightarrow T(4\text{ m/s}) = (4T)v_{block}$$

$$(b) 1\text{ m/s}$$

Potential Energy

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Conservative Forces - Forces that create potential energy.

Conservative forces are rare. Only gravity and the spring force are conservative. (You'll learn two more next term - the electric and magnetic force.) For a force to be conservative, the work it does must be independent of path.

Conservation of Energy

For a conservative force,

$$W = -\Delta U$$

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Conservation of Energy - If only conservative forces do work on an object, its total energy cannot change.

Total Energy, E = the sum of kinetic and potential energy.

$$E = K + U$$

Conservation of Energy II

Proof: If a conservative force is the only force doing work on an object then:

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$$K_2 - K_1 = -(U_2 - U_1)$$

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$$\Rightarrow E_1 = E_2$$

Energy Conservation Exercise

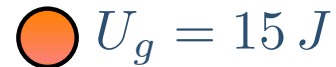
A block having 15 J of gravitational potential energy is dropped from rest. When the block hits the ground, it has 15 J of kinetic energy. If gravity is the only force acting on the block, how much potential energy does the block have when it hits the ground?

 $U_g = 15 \text{ J}$



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A diagram showing a block at the start of its fall. It consists of a small orange circle with a black outline, representing the block, positioned to the left of the equation $U_g = 15\text{ J}$.

$$U_g = 15\text{ J}$$



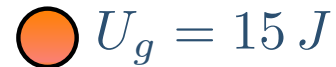
A diagram showing a block at the end of its fall. It consists of a small orange circle with a black outline, representing the block, positioned to the left of the equation $K = 15\text{ J}$. Below the block is a thick, dark gray horizontal bar representing the ground.

$$K = 15\text{ J}$$

Energy Conservation Exercise

A block having 15 J of gravitational potential energy is dropped from rest. When the block hits the ground, it has 15 J of kinetic energy. If gravity is the only force acting on the block, how much potential energy does the block have when it hits the ground?

(a) 0 J



A diagram showing a block at an initial state. The block is represented by a small orange circle with a black outline. To its right is the equation $U_g = 15\text{ J}$.

$$U_g = 15\text{ J}$$



A diagram showing a block at a final state. The block is represented by a small orange circle with a black outline, resting on a thick grey horizontal line representing the ground. To its right is the equation $K = 15\text{ J}$.

$$K = 15\text{ J}$$

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(a) 0 J

$U_g = 15\text{ J}$

(b) 7.5 J

$K = 15\text{ J}$

A diagram showing a grey horizontal bar representing the ground. An orange circle representing the block is positioned on top of the bar.

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(a) 0 J

$U_g = 15\text{ J}$

(b) 7.5 J

(c) 15 J

(d) 30 J

$K = 15\text{ J}$

A horizontal grey bar representing the ground. A small orange circle representing the block is positioned on top of the bar.

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(a) 0 J

$U_g = 15\text{ J}$

(b) 7.5 J

(c) 15 J

(d) 30 J

$K = 15\text{ J}$


(e) Cannot be determined



Energy Conservation Exercise

A block having $15 J$ of gravitational potential energy is dropped from rest. When the block hits the ground, it has $15 J$ of kinetic energy. If gravity is the only force acting on the block, how much potential energy does the block have when it hits the ground?

(a) $0 J$

 $U_g = 15 J$

(b) $7.5 J$

(c) $15 J$

$$K_1 + U_1 = K_2 + U_2 \Rightarrow$$

$$0 + 15 J = 15 J + U_2$$

(d) $30 J$

 $K = 15 J$

(e) Cannot be determined