

March 6, Week 8

Today: Chapter 6, Work

Exam #2, Friday, March 8

Practice Exam Solutions on Website

Review Session, Thursday, March 7, 5:15pm Room 114
Regener Hall

Thursday office hours will be held in Room 109 of Regener
Hall from 1:00-3:30.

If interested in Physics 110, come talk to me

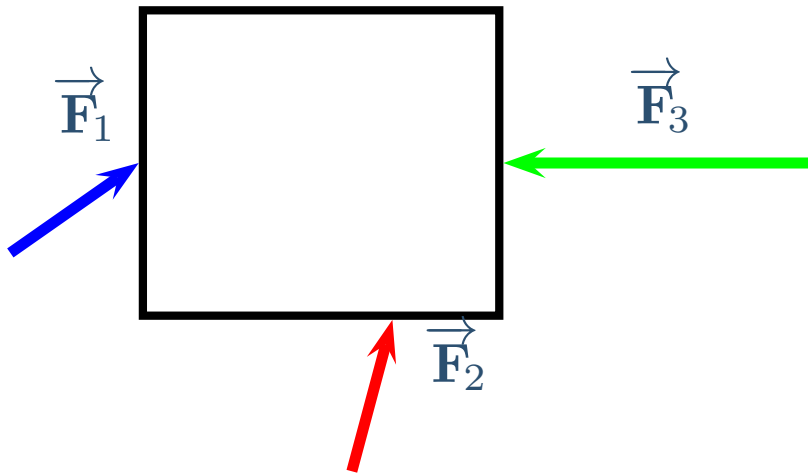
Total Work

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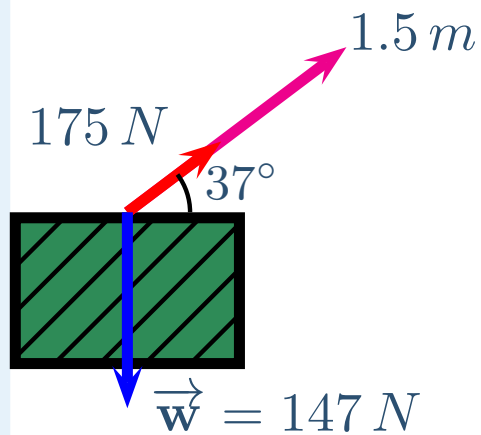
So total work done by a collection of forces is given by the sum of the individual works.



$$W_{total} = W_1 + W_2 + W_3 + \dots$$

Total Work Exercise

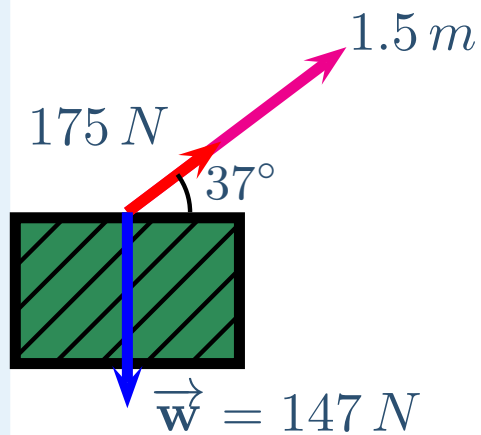
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$$(a) \quad (175\text{ N})(1.5\text{ m}) \cos 37^\circ + (147\text{ N})(1.5\text{ m}) \cos 127^\circ \\ = 209.6\text{ J} - 132.7\text{ J} = 76.9\text{ J}$$

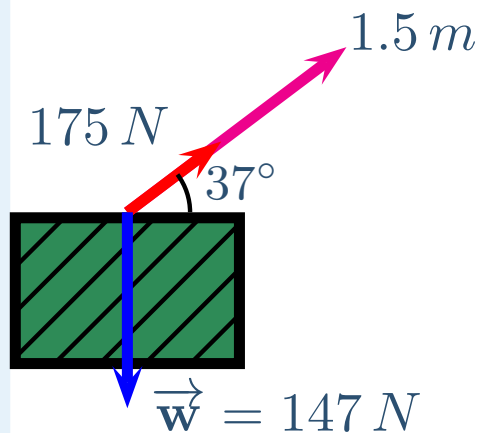


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(b) $(175\text{ N})(1.5\text{ m}) \cos 0^\circ + (147\text{ N})(1.5\text{ m}) \cos 127^\circ$
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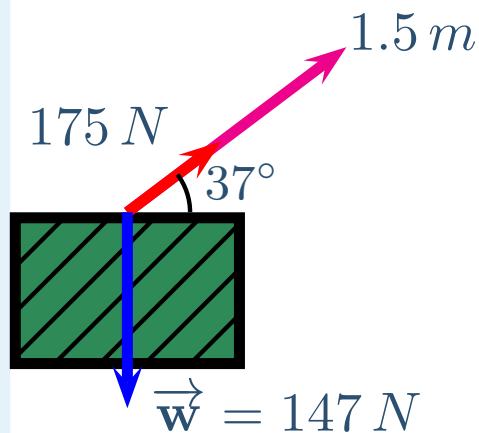
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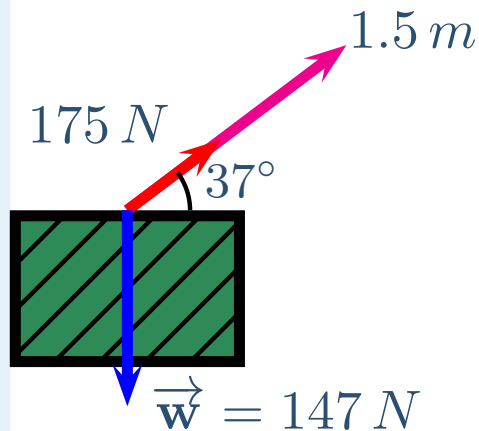
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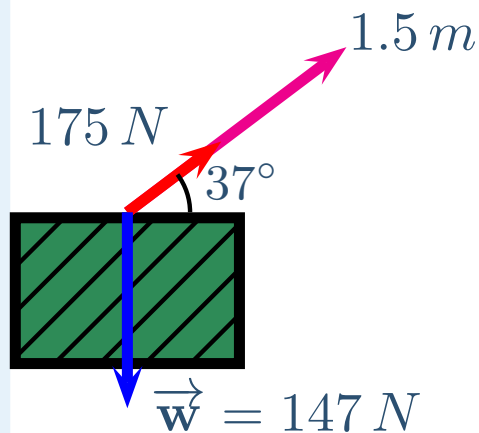
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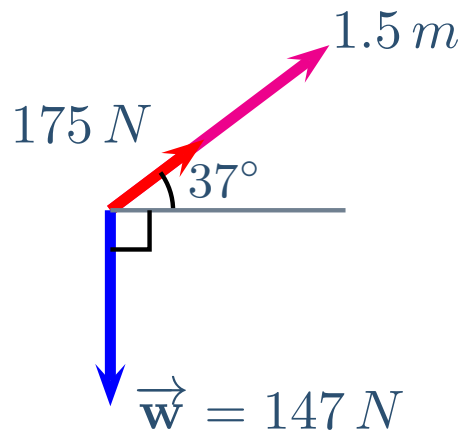
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Total Work Exercise

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ϕ is the angle *between* the force and the displacement



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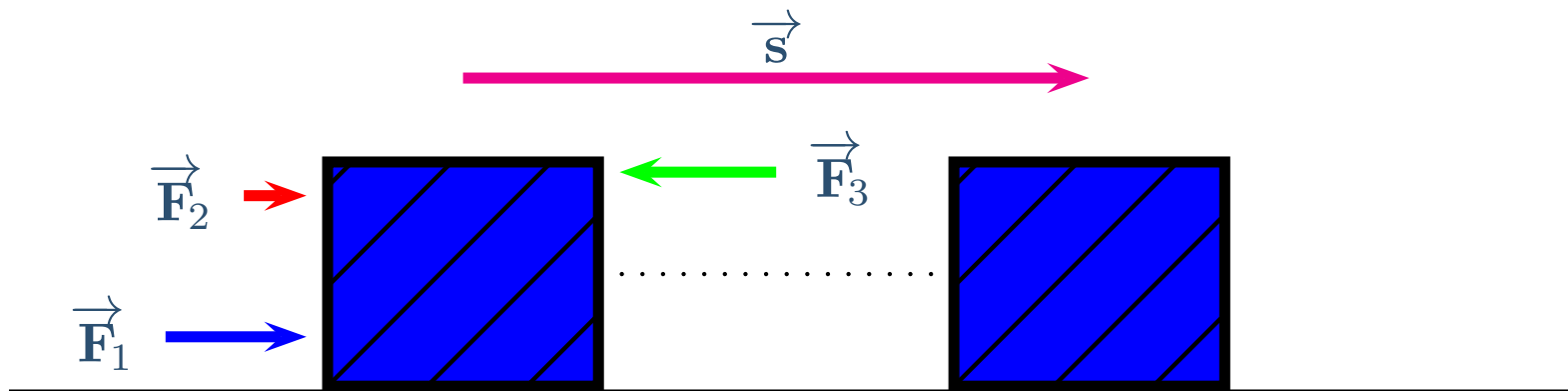
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Work-Energy Theorem

Work-Energy Theorem - Allows us to calculate the physical effect that work has on an object. It says that work causes a change in speed.

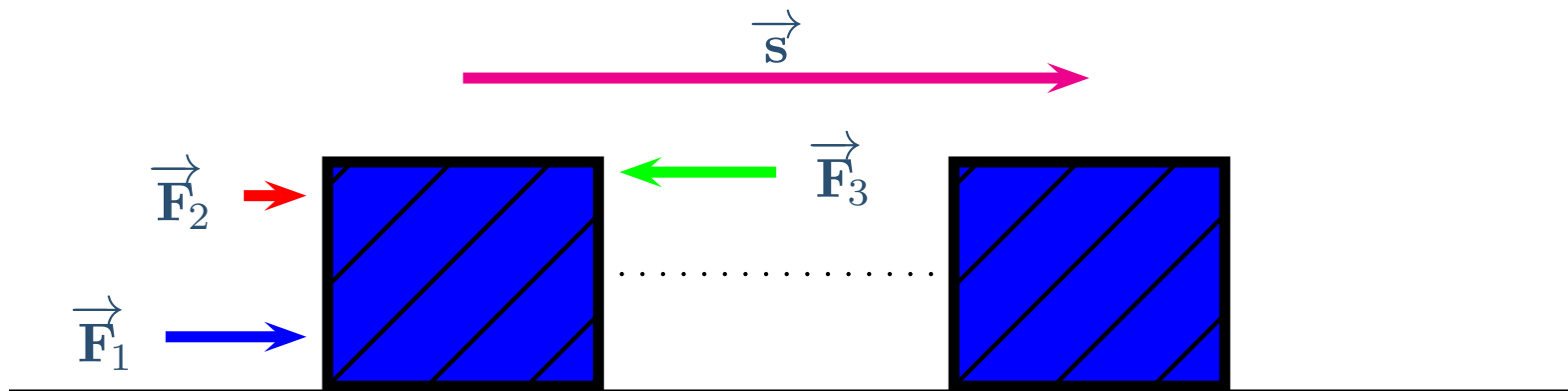
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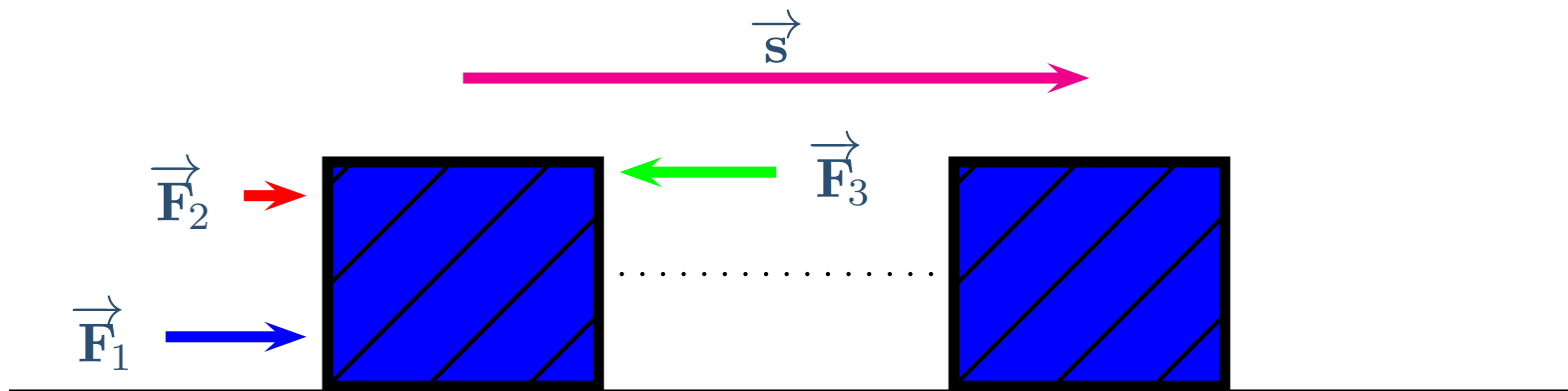
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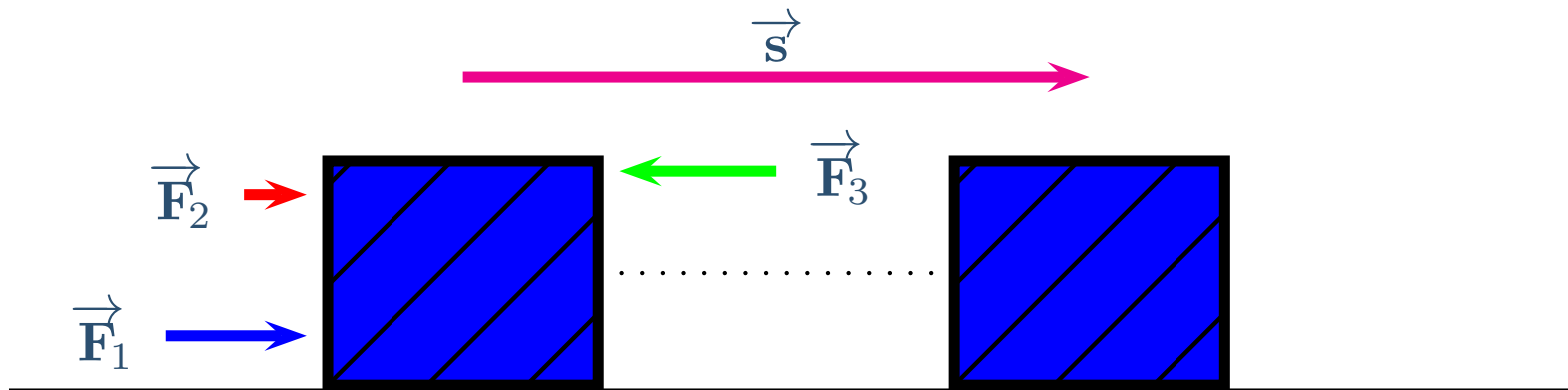
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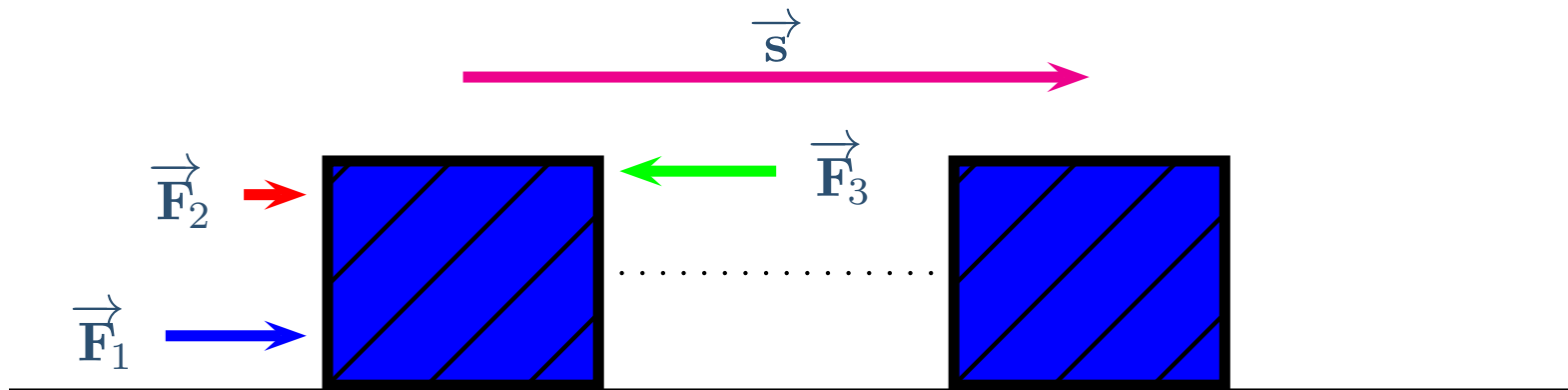


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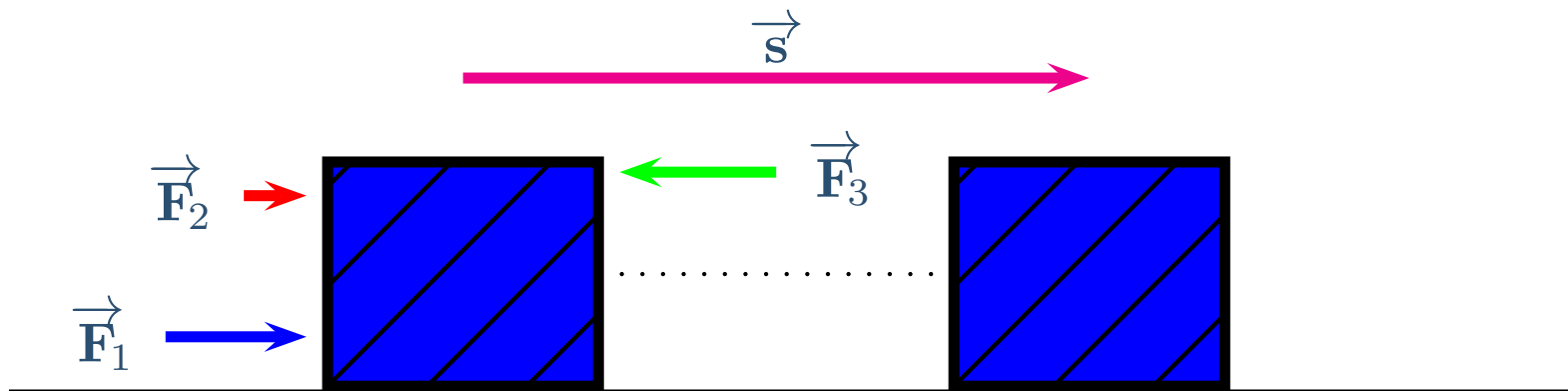


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Using $v_2^2 = v_1^2 + 2as \Rightarrow W_{total} = \frac{1}{2}mv_2^2 - \frac{1}{2}mv_1^2$

Work-Energy Theorem II

It can be shown that for constant forces in *ANY* direction that:

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Example: A 15 kg box is lifted, from rest, by applying a 175 N force at 37° . How fast will the box be going after it has moved 1.5 m ?

Work-Energy Exercise

A 15 kg box has a total of 129.8 J of work done to it (by different forces than before). How fast and in what direction is it going?

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Scalars cannot determine direction

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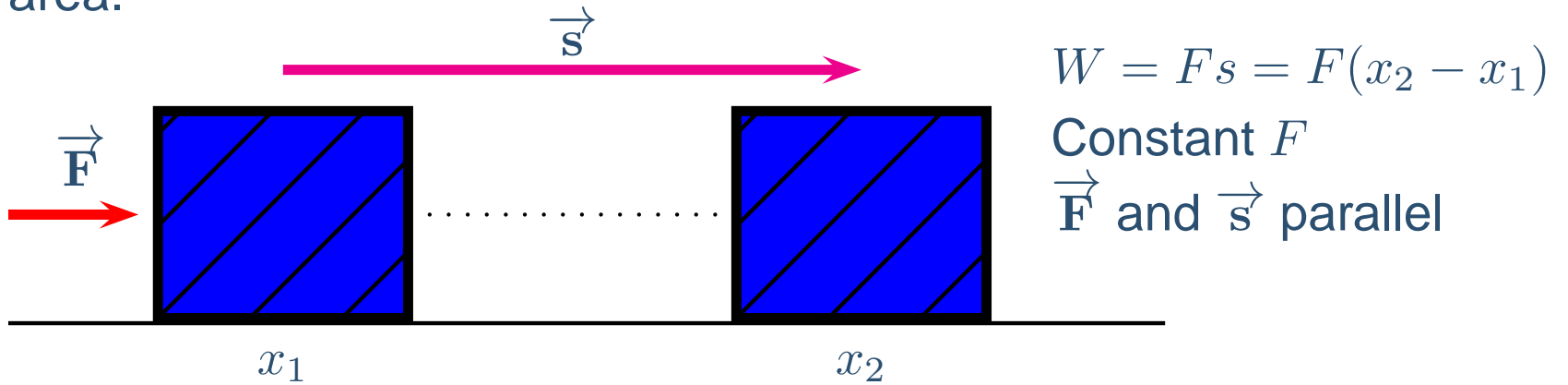
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Variable Forces

To find the work done by a changing force requires finding an area.

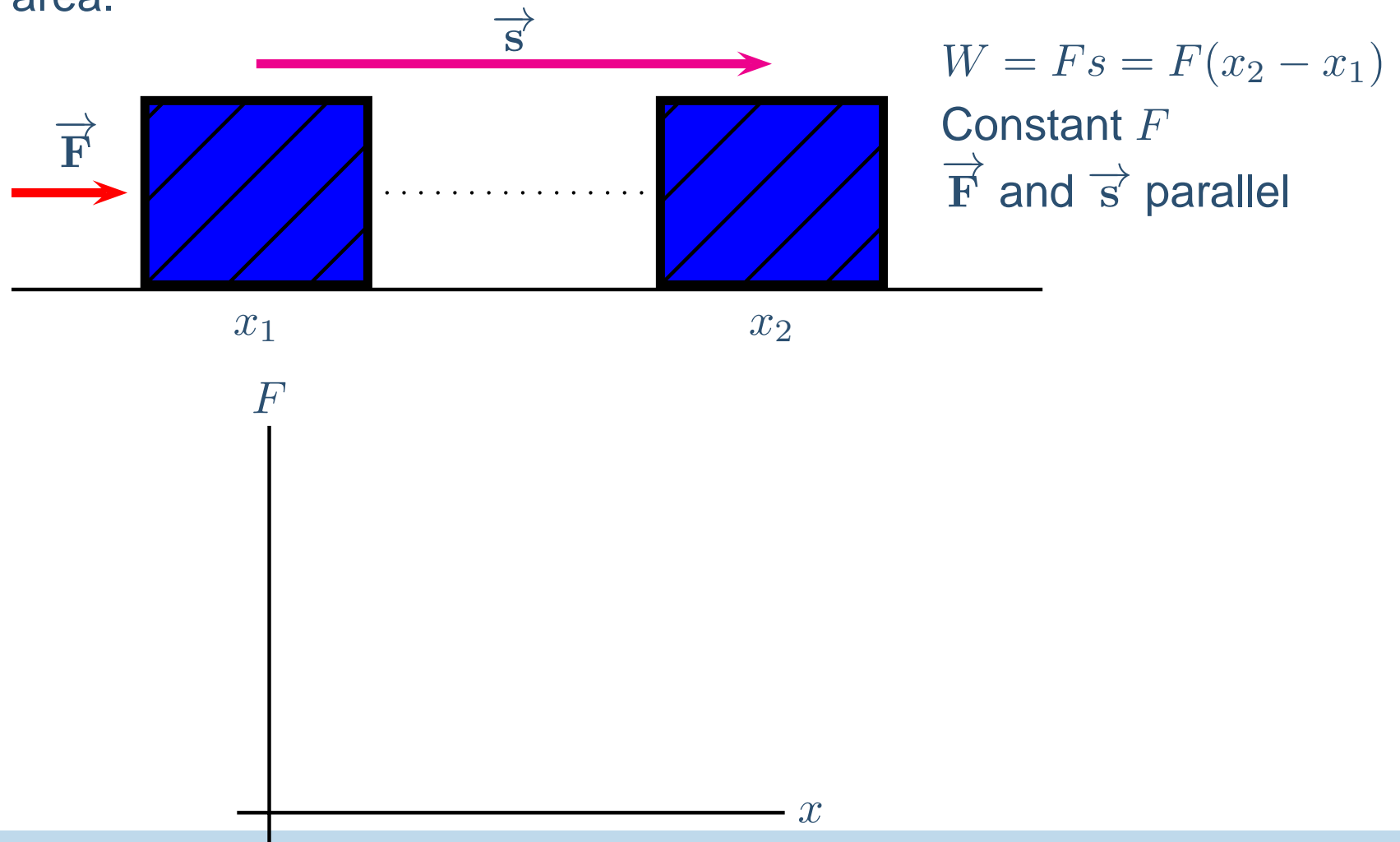
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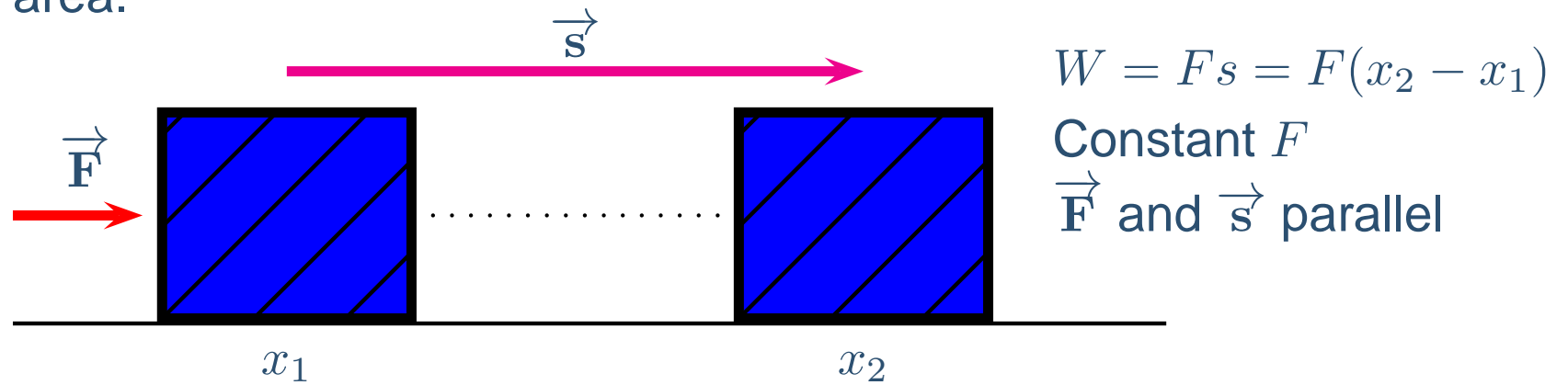
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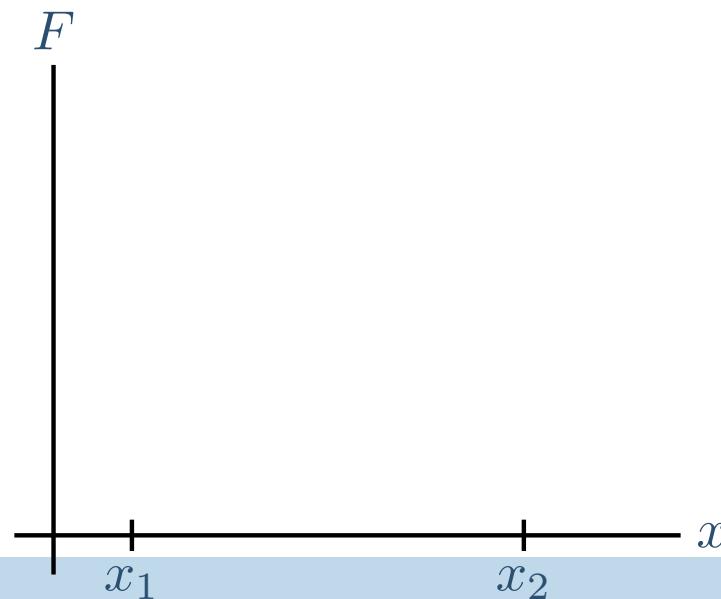
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$$W = F s = F(x_2 - x_1)$$

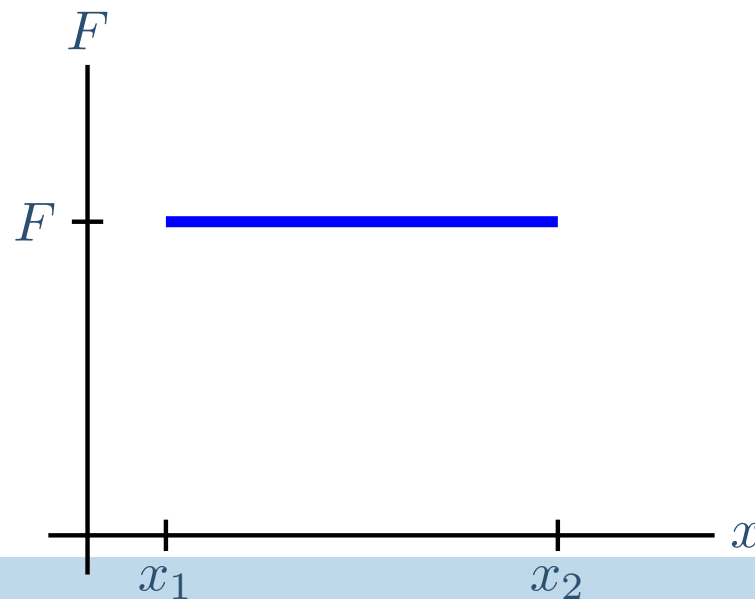
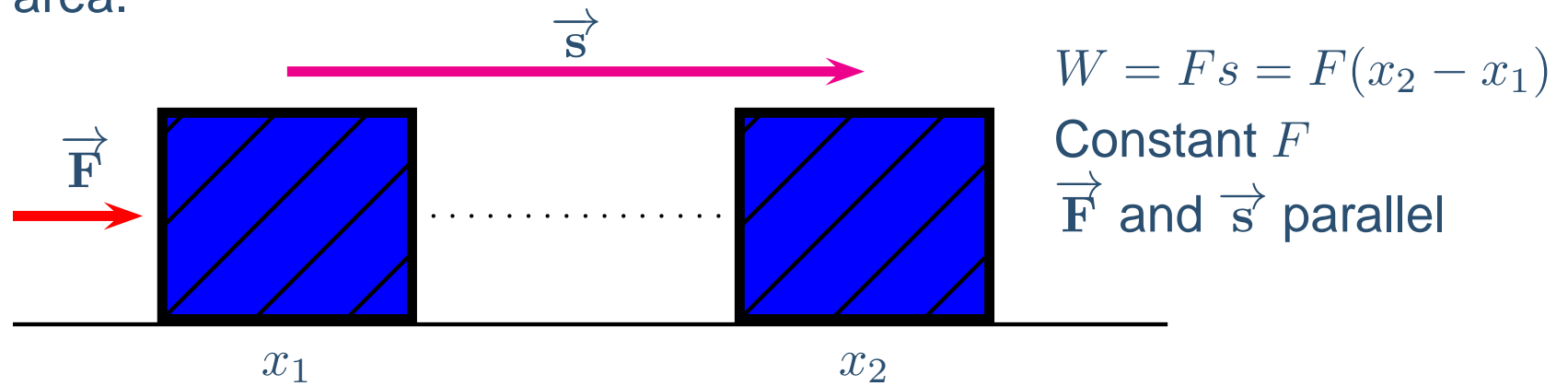
Constant F

\vec{F} and \vec{s} parallel



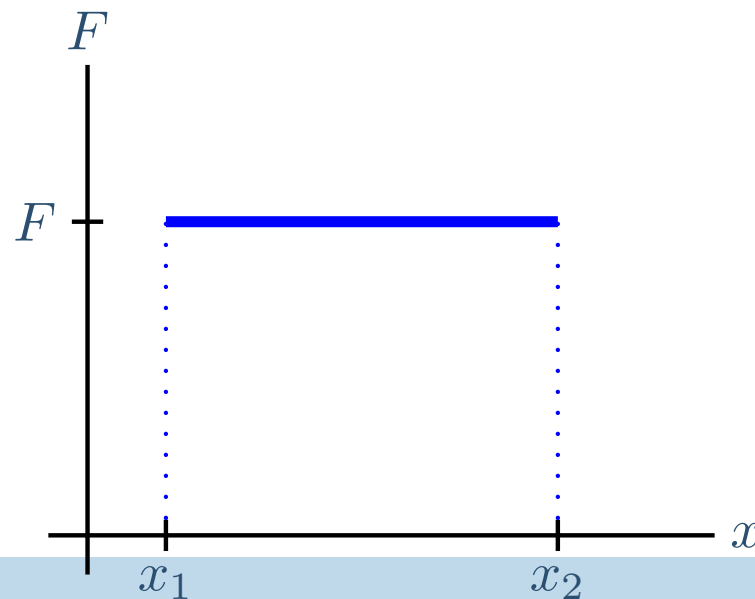
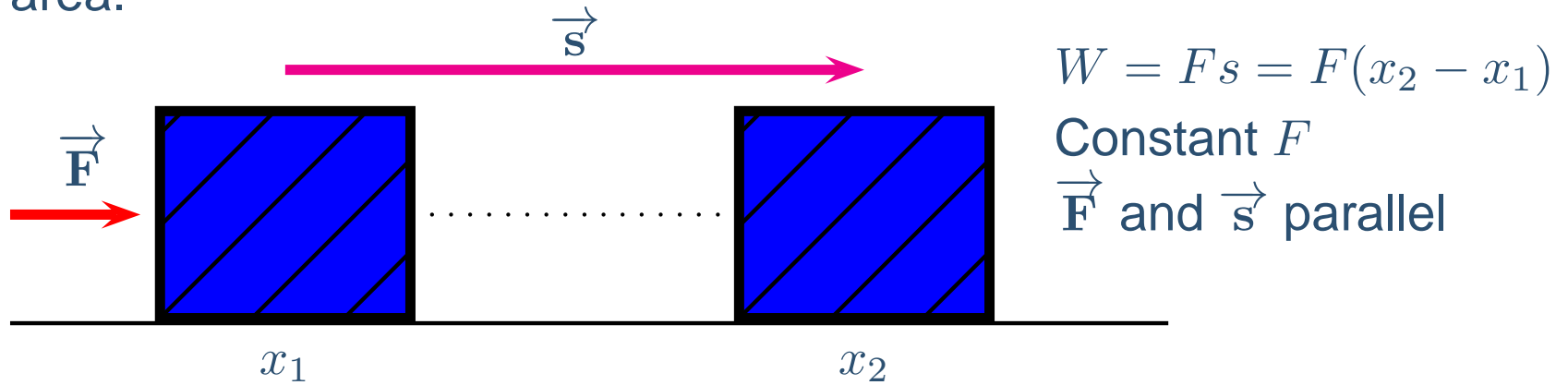
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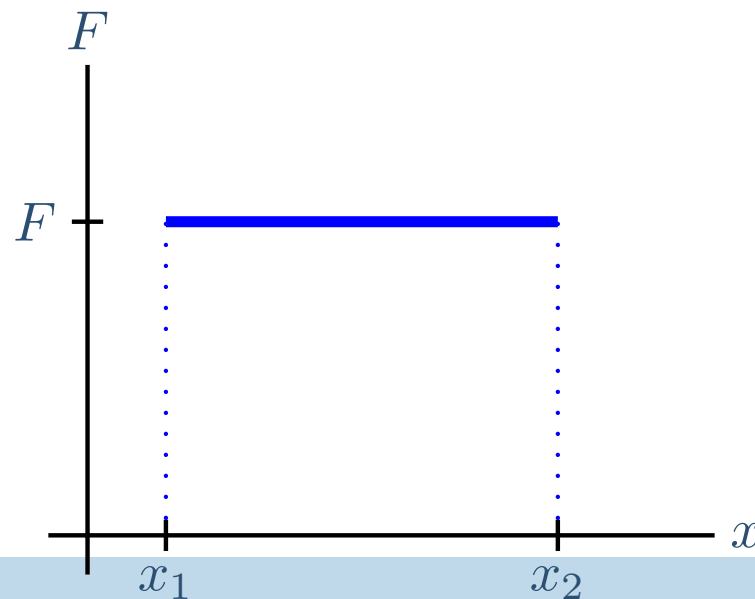
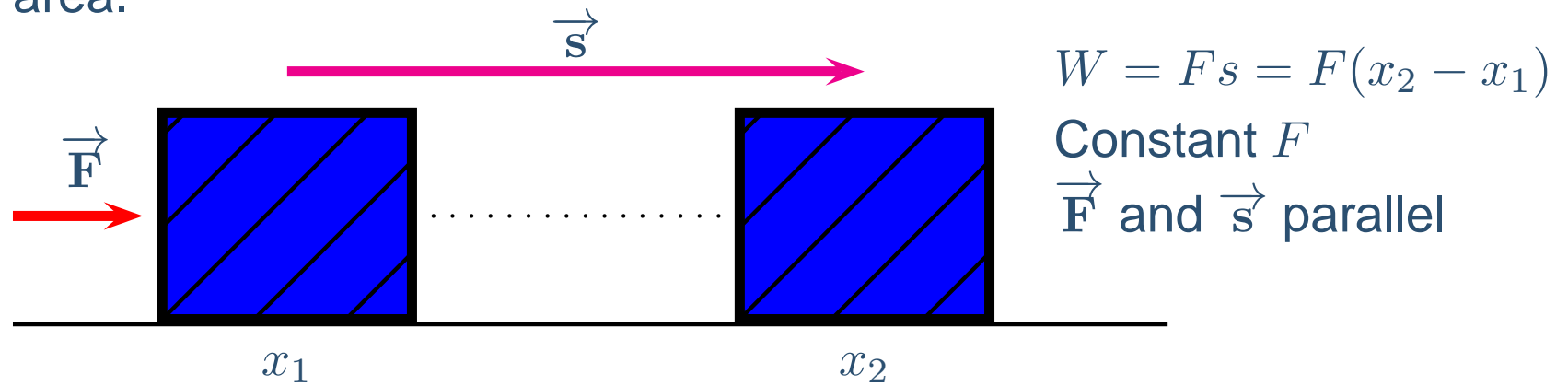
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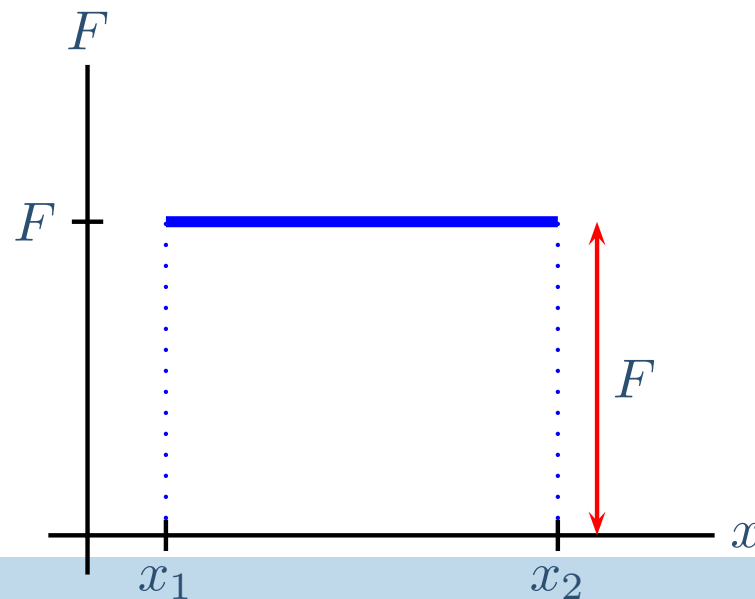
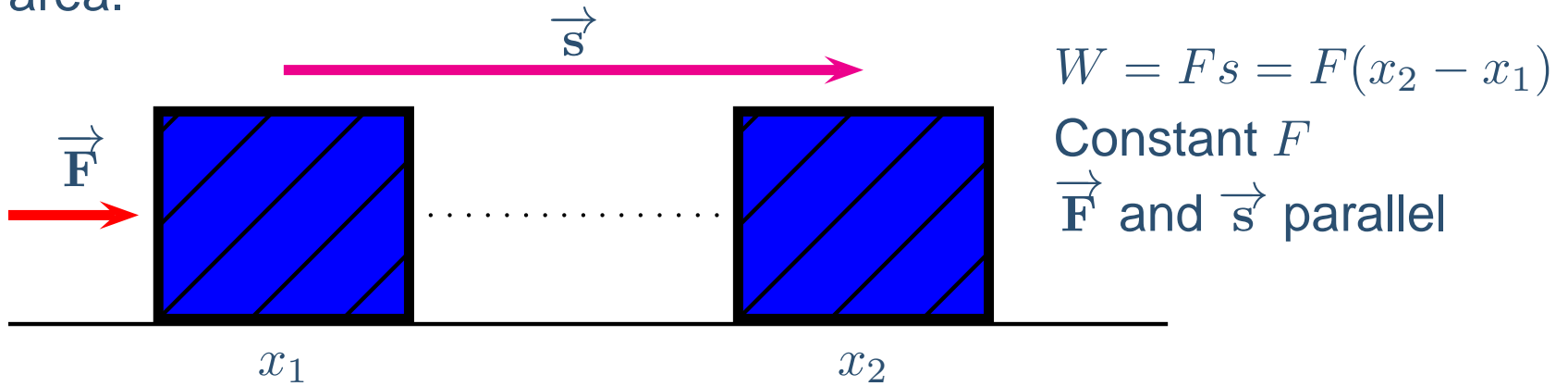
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$$W = F(x_2 - x_1)$$

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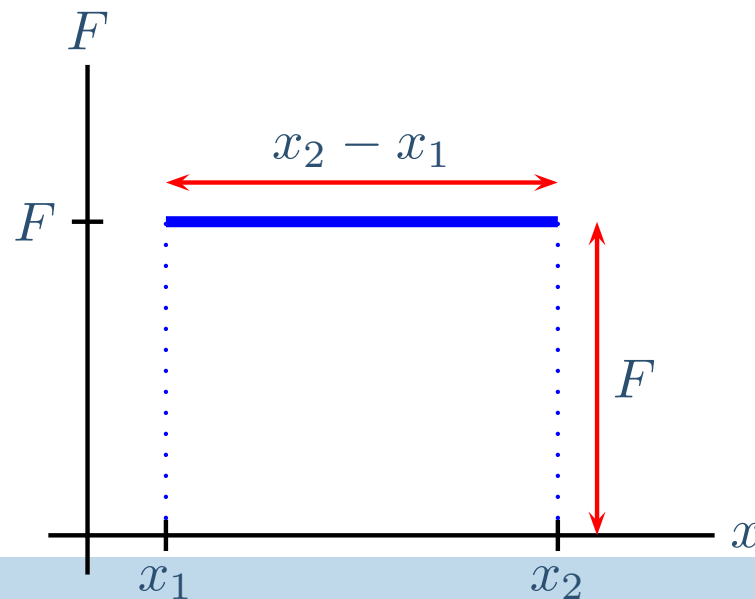
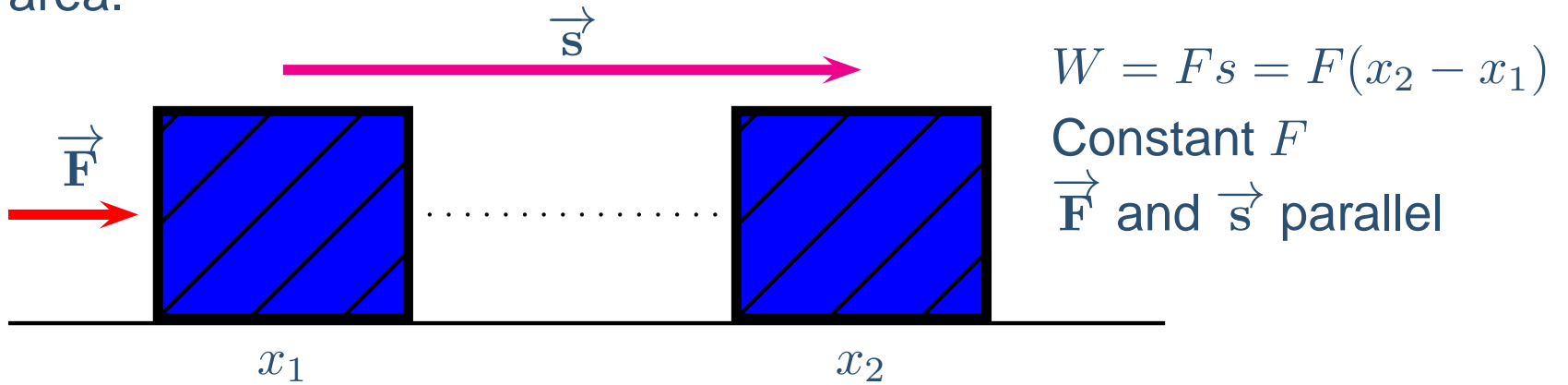
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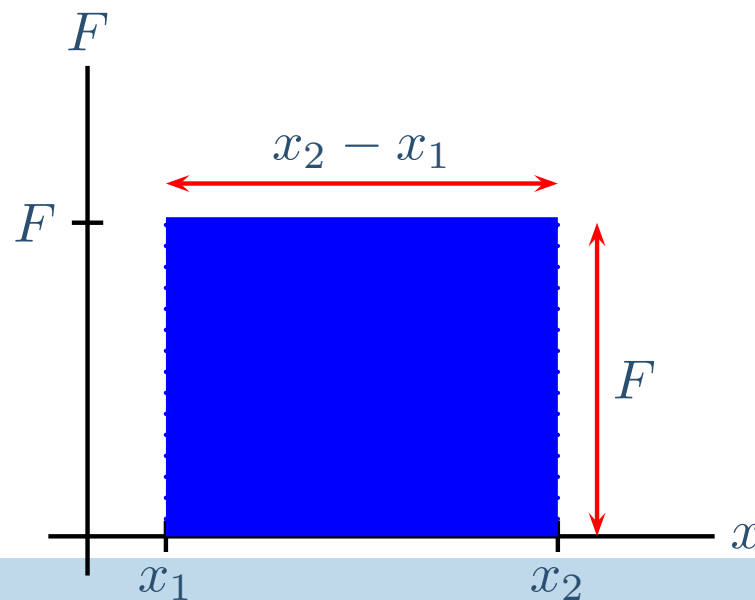
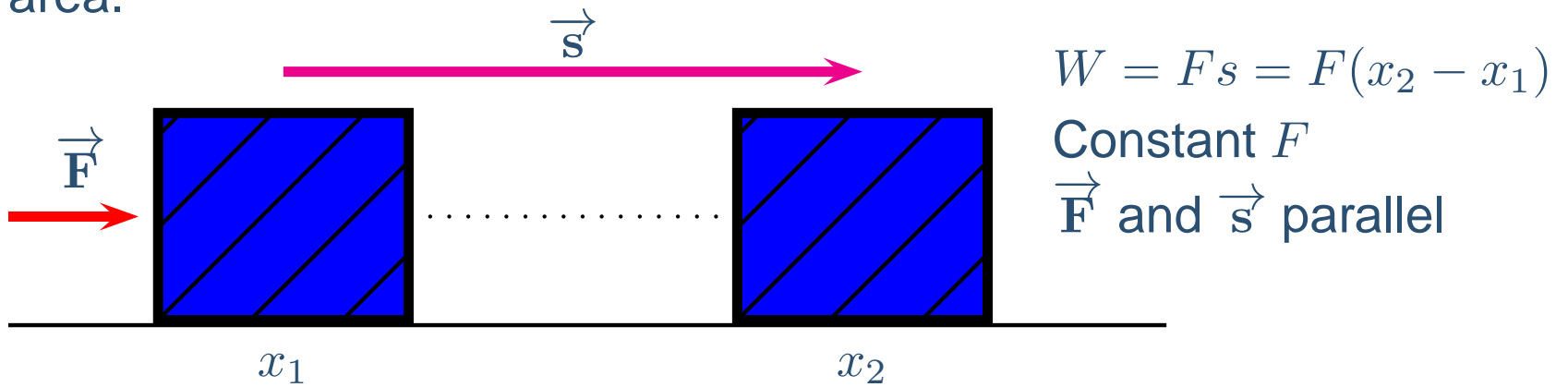
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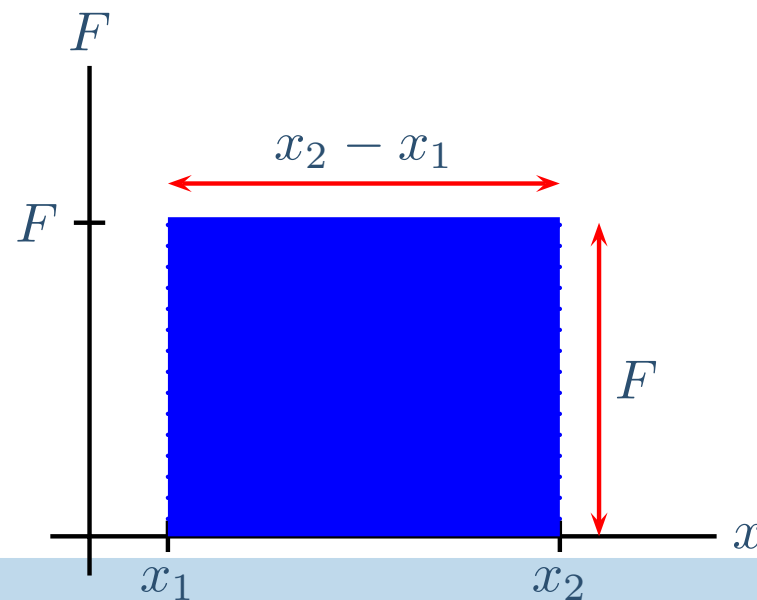
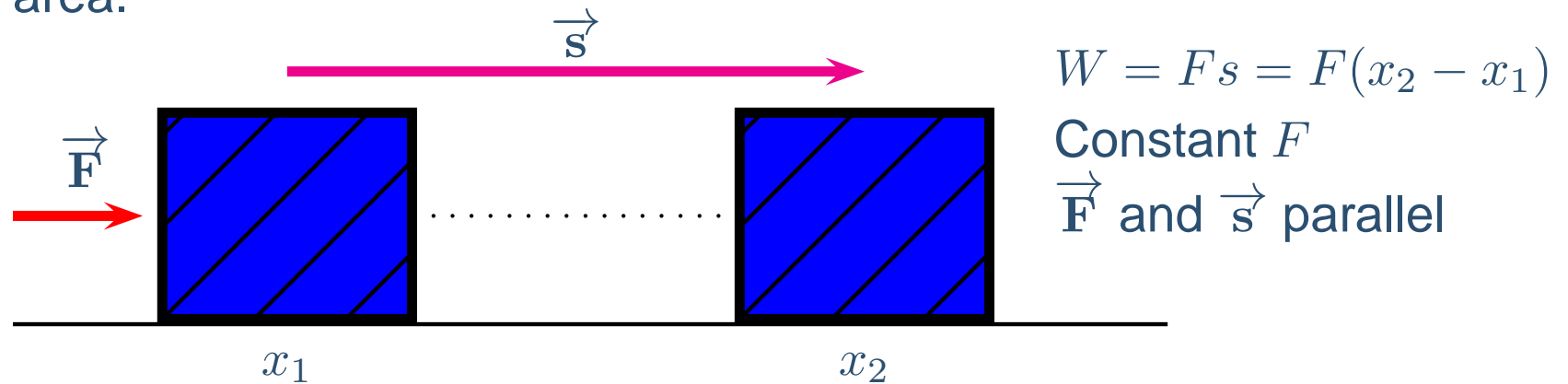
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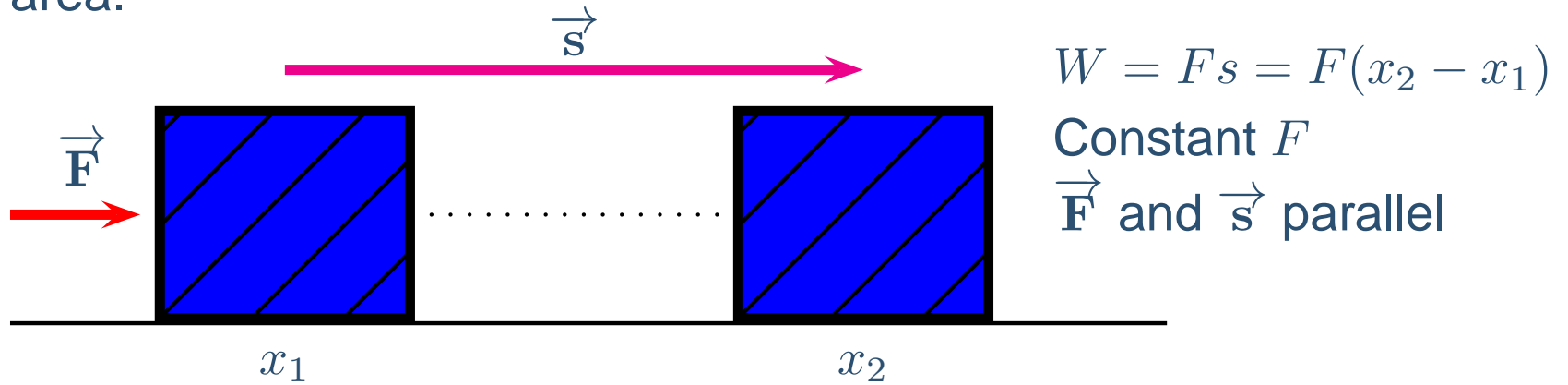


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Work is the area under the curve

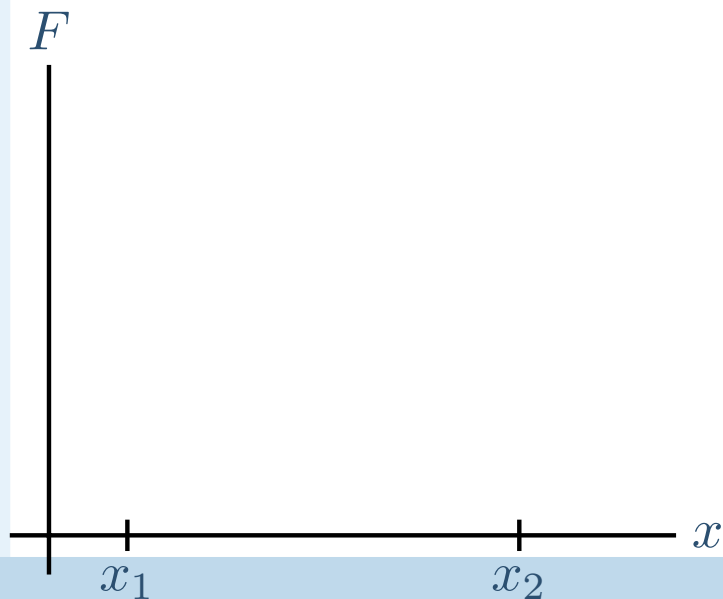
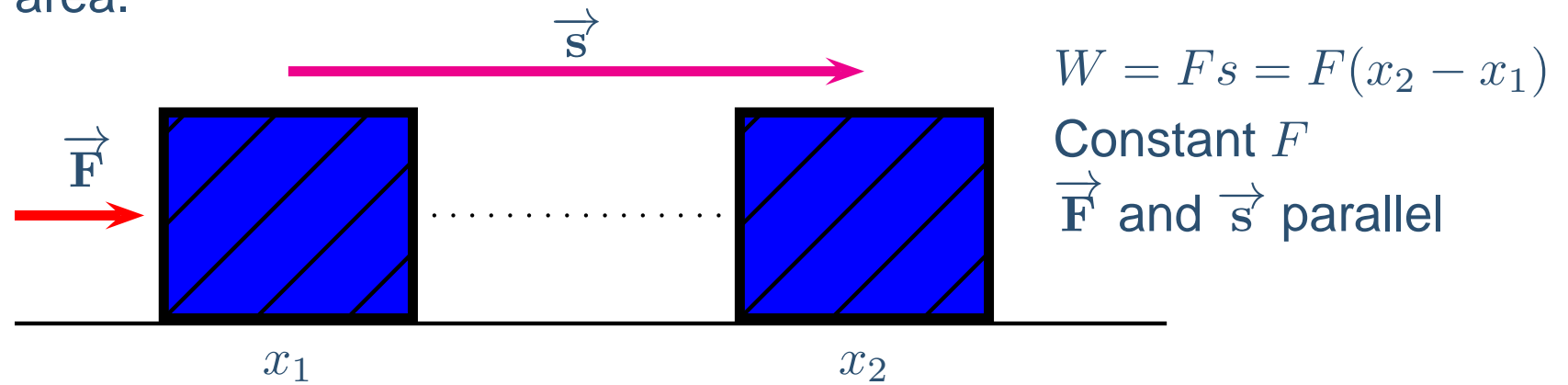
Variable Forces II

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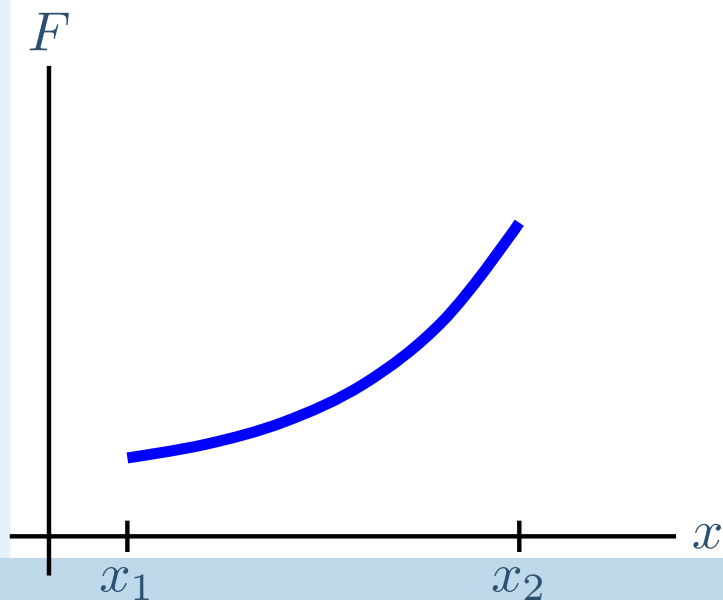
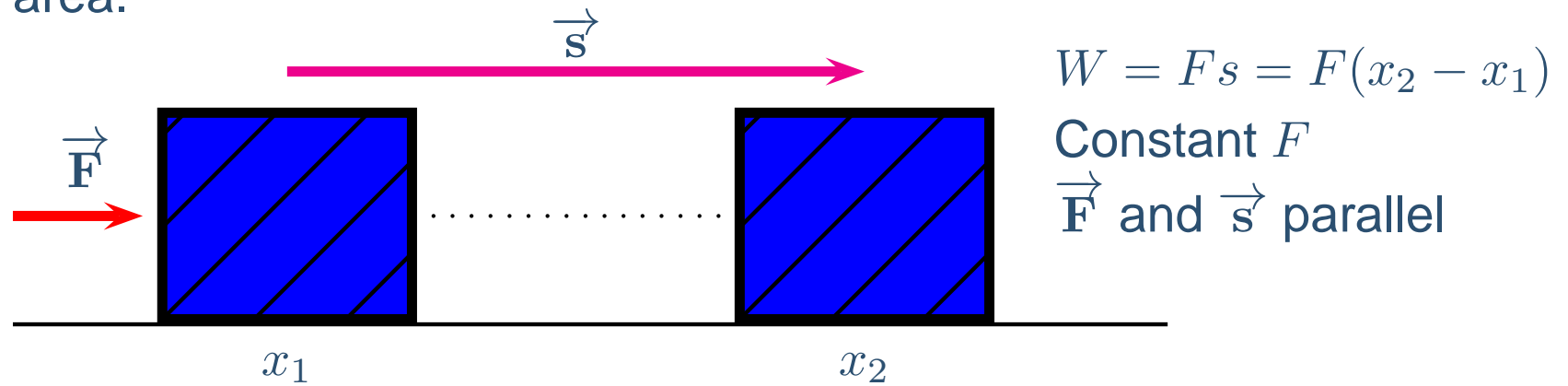
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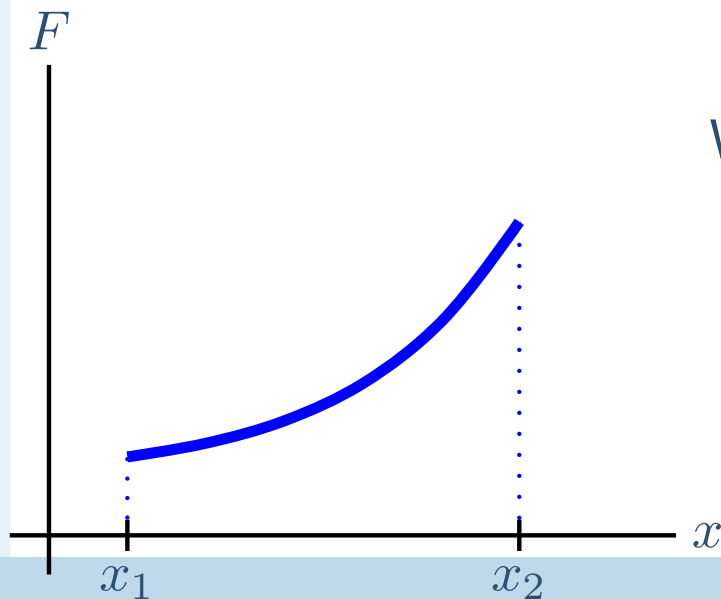
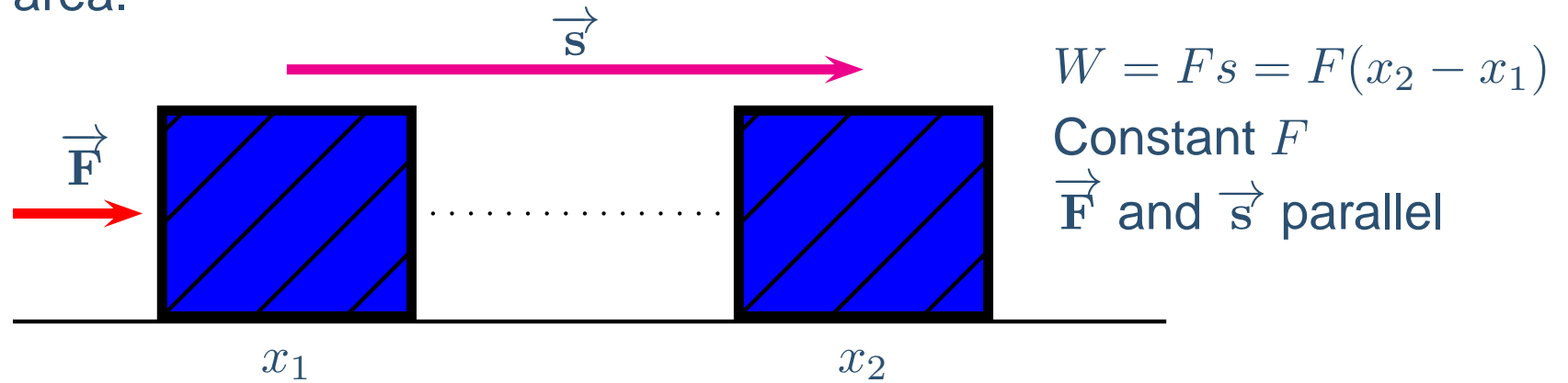
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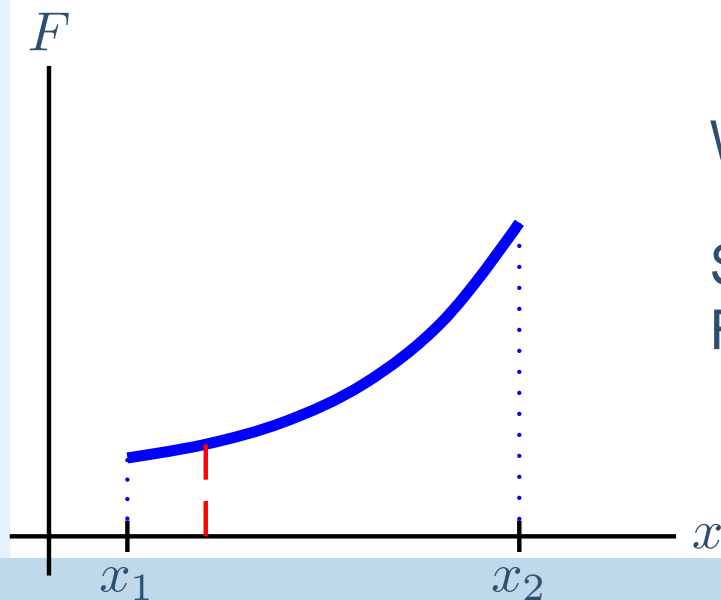
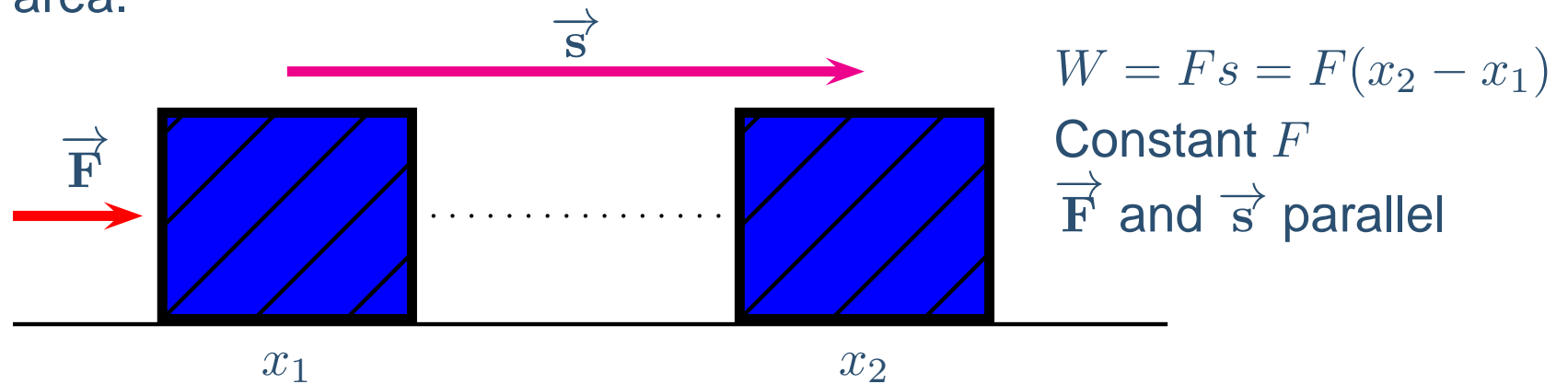
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Work is the area under this curve

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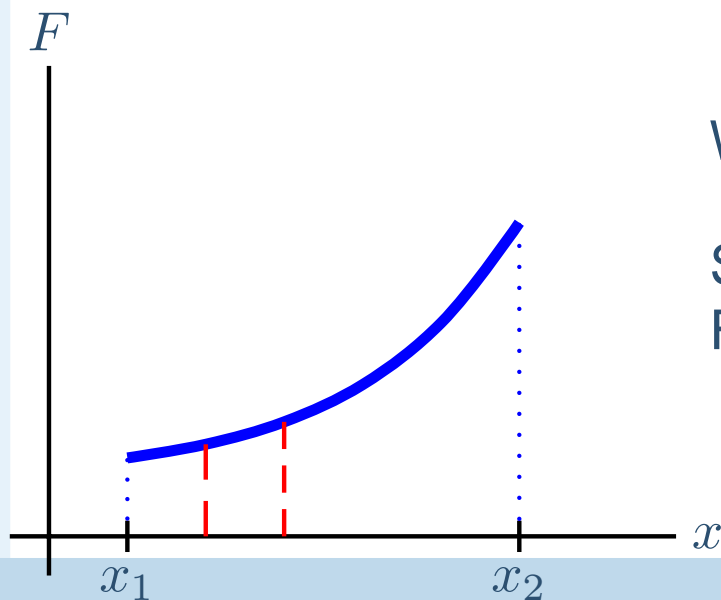
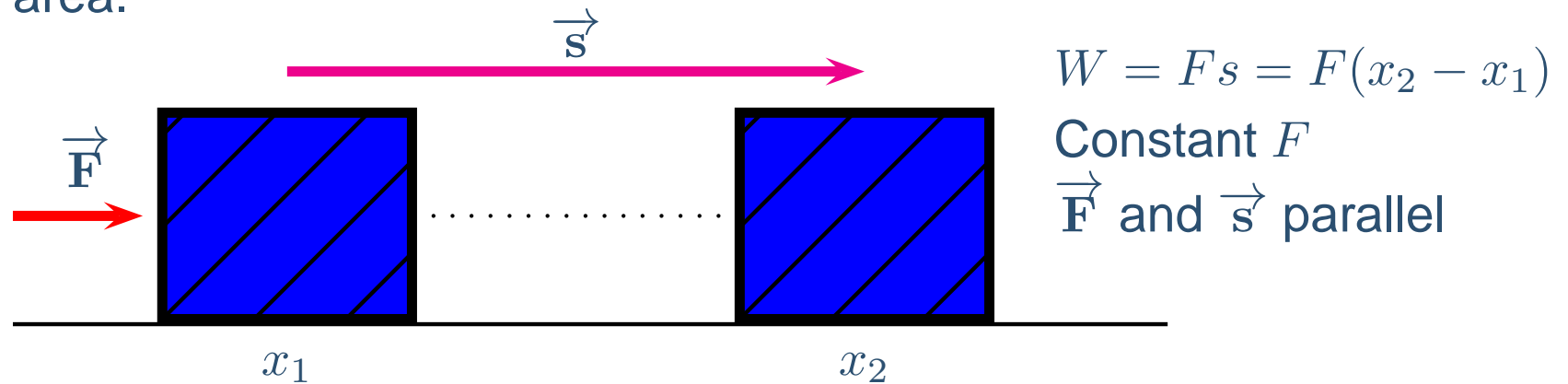


Work is the area under this curve

Split region into many small rectangles.
Find area of each rectangle and add.

Variable Forces II

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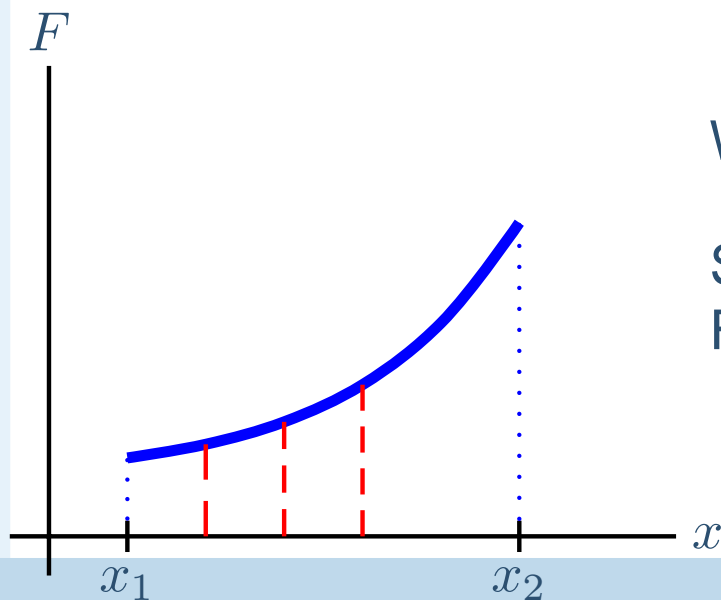
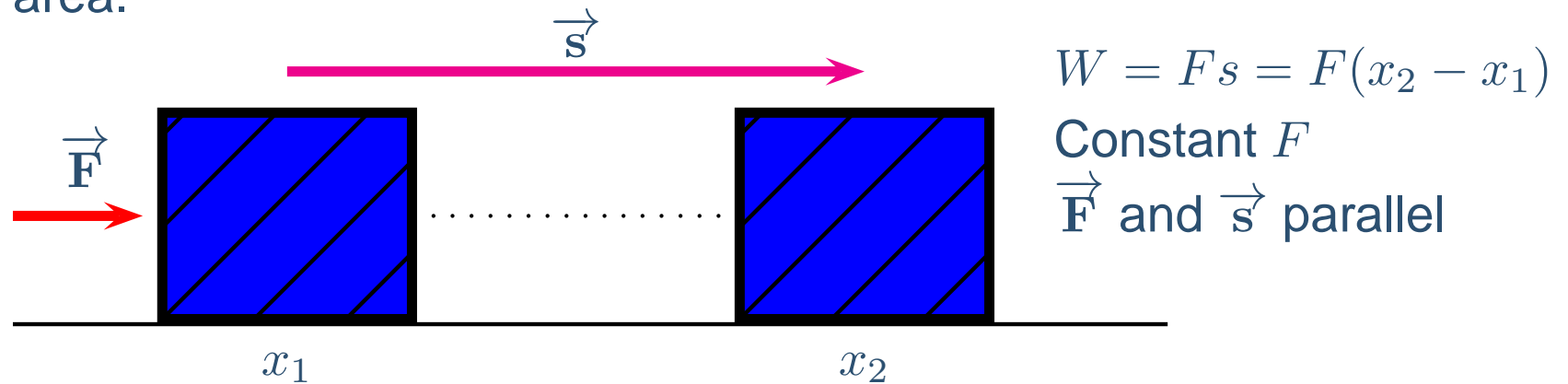


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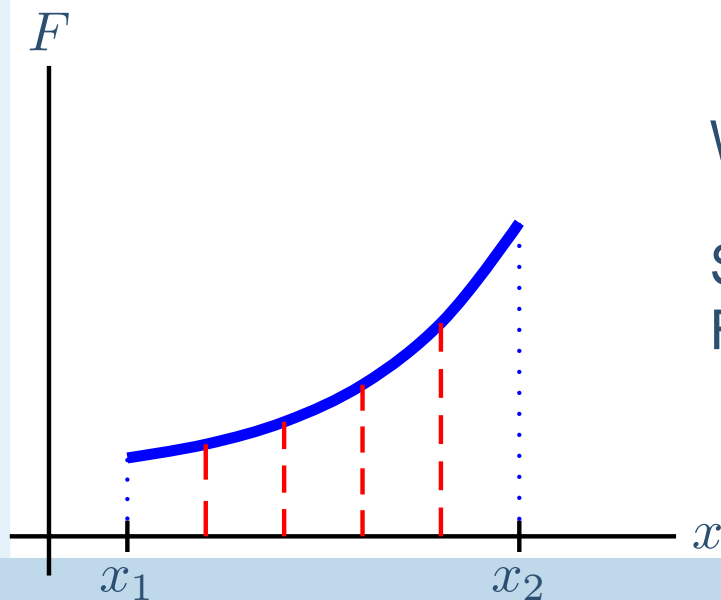
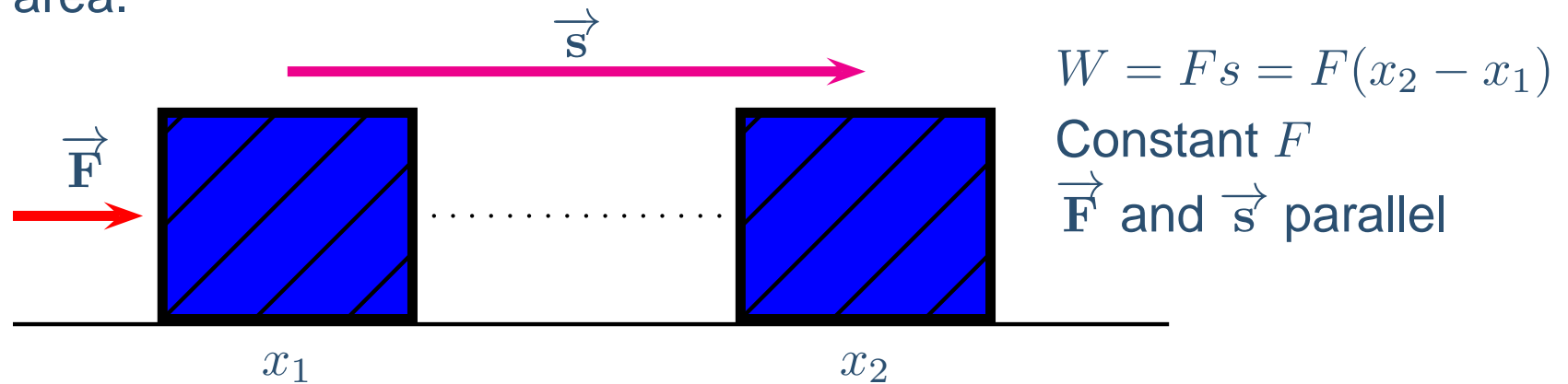


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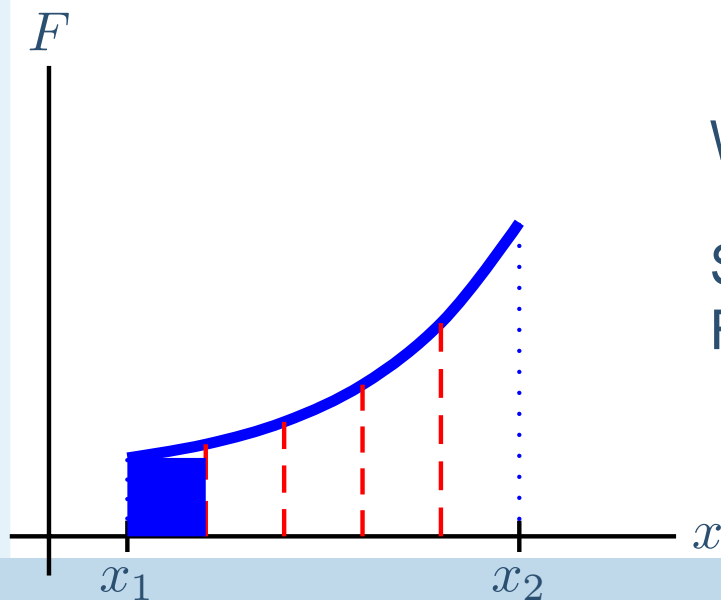
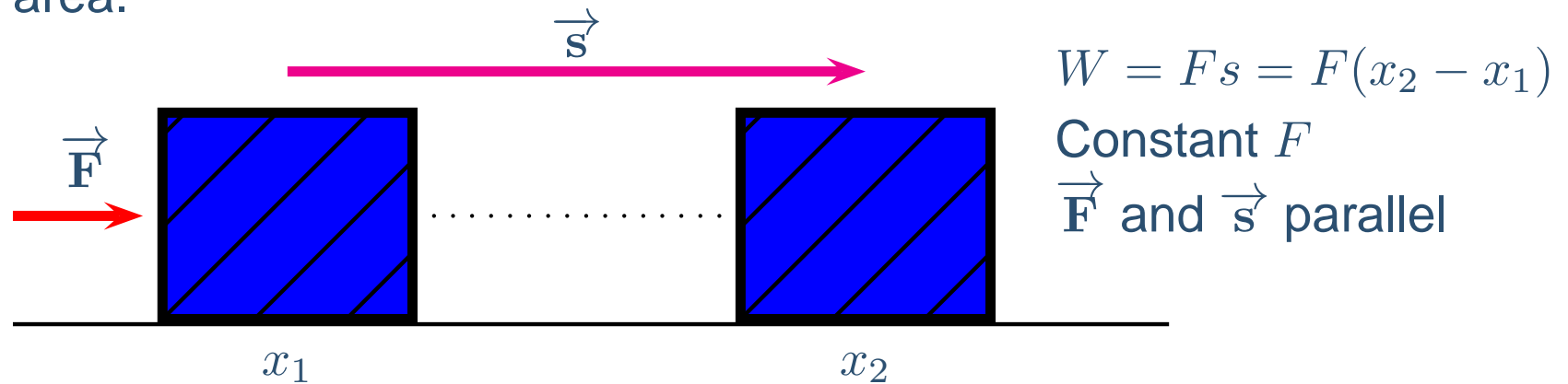


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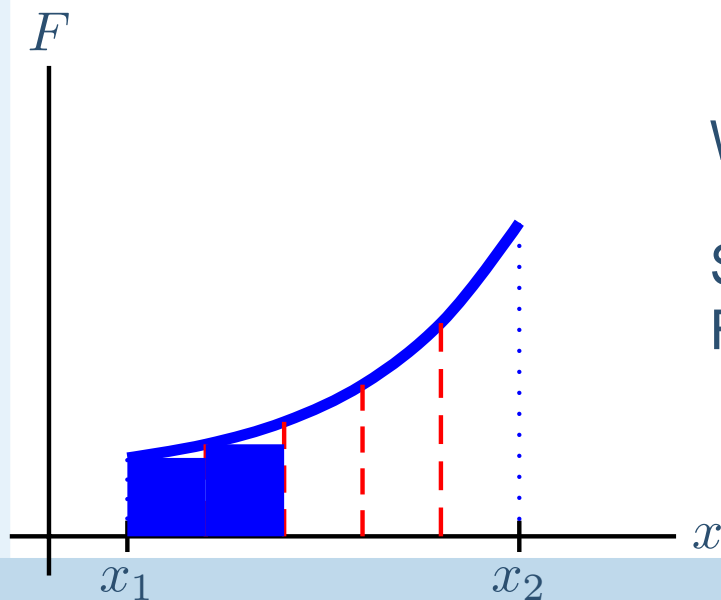
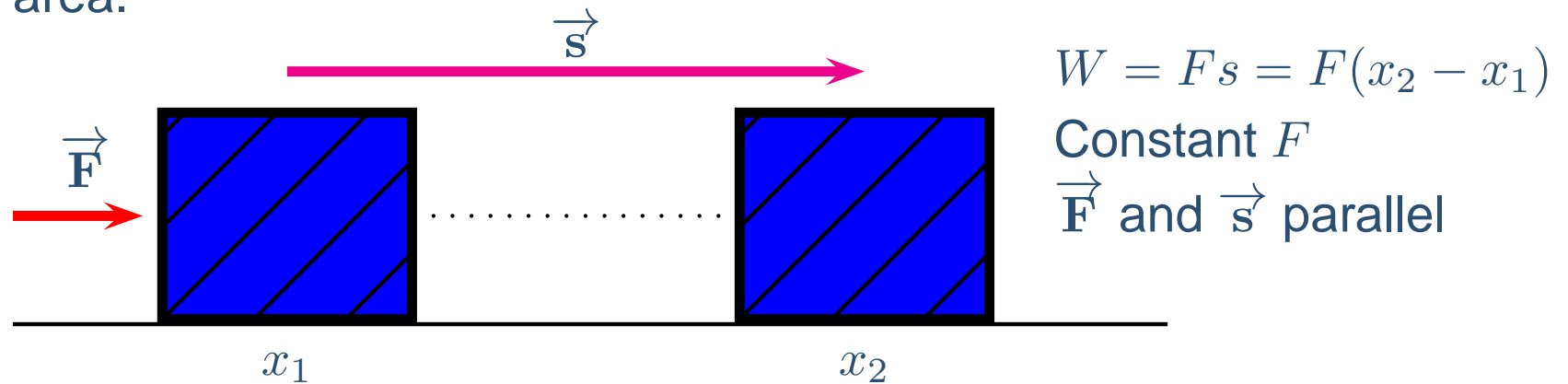


Work is the area under this curve

Split region into many small rectangles.
Find area of each rectangle and add.

Variable Forces II

To find the work done by a changing force requires finding an area.

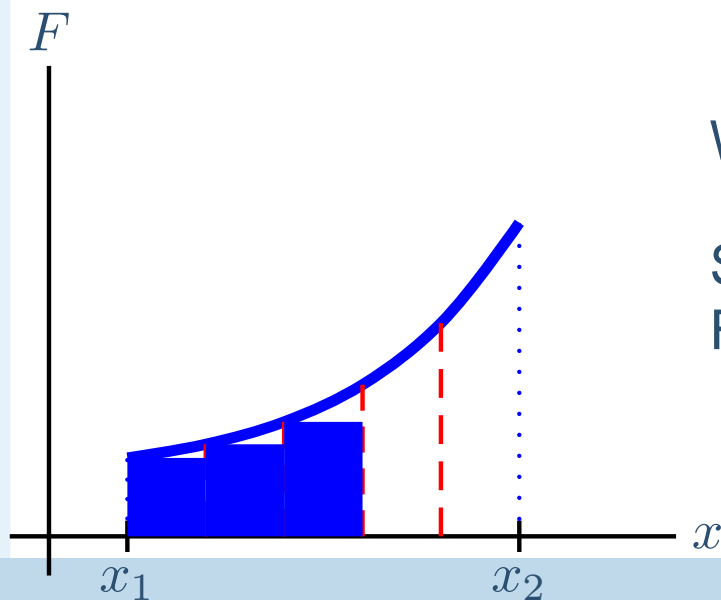
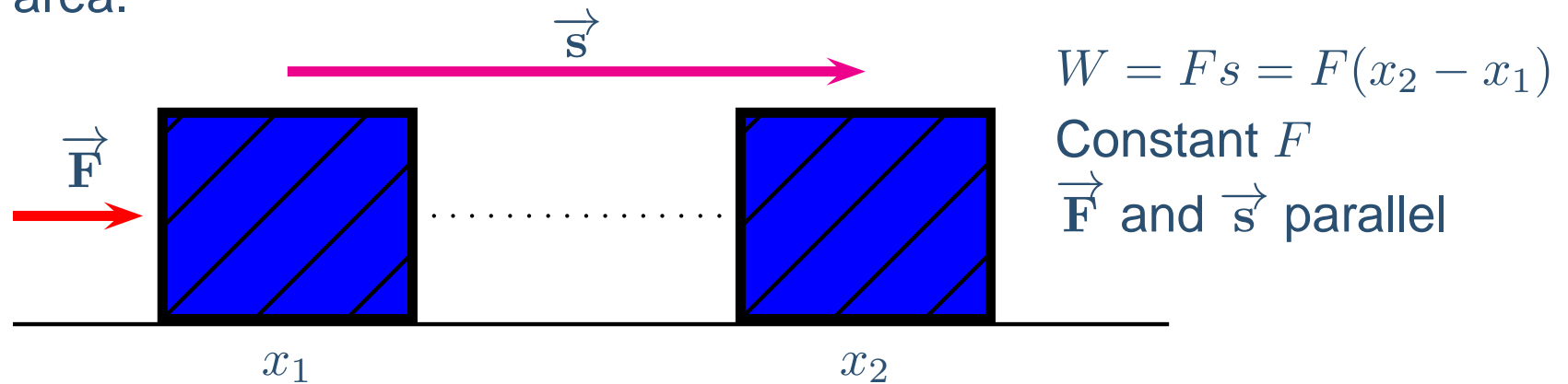


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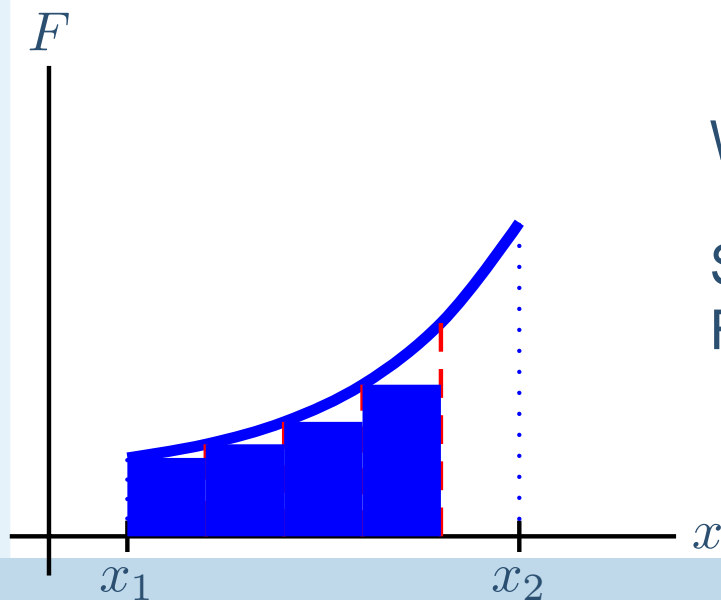
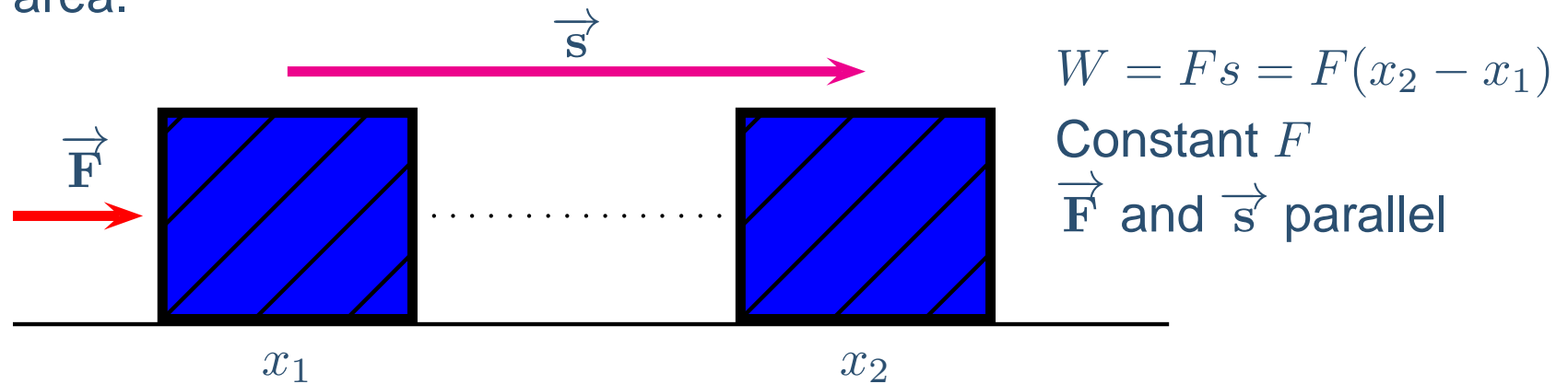


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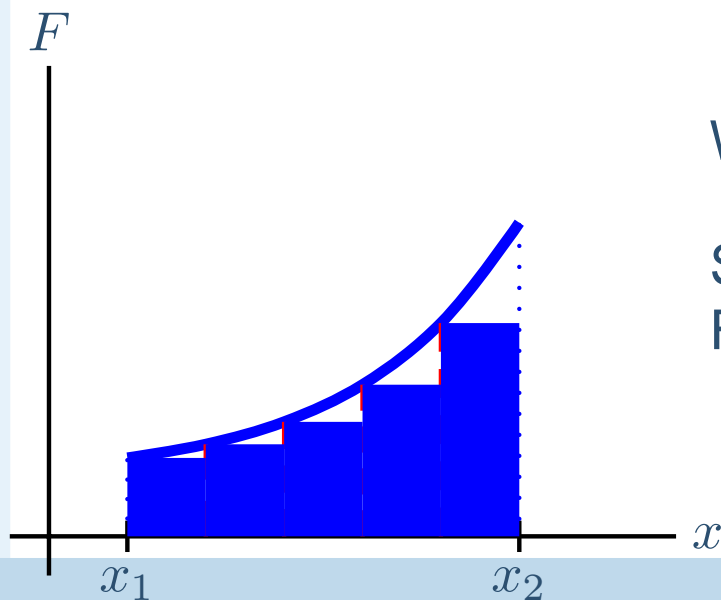
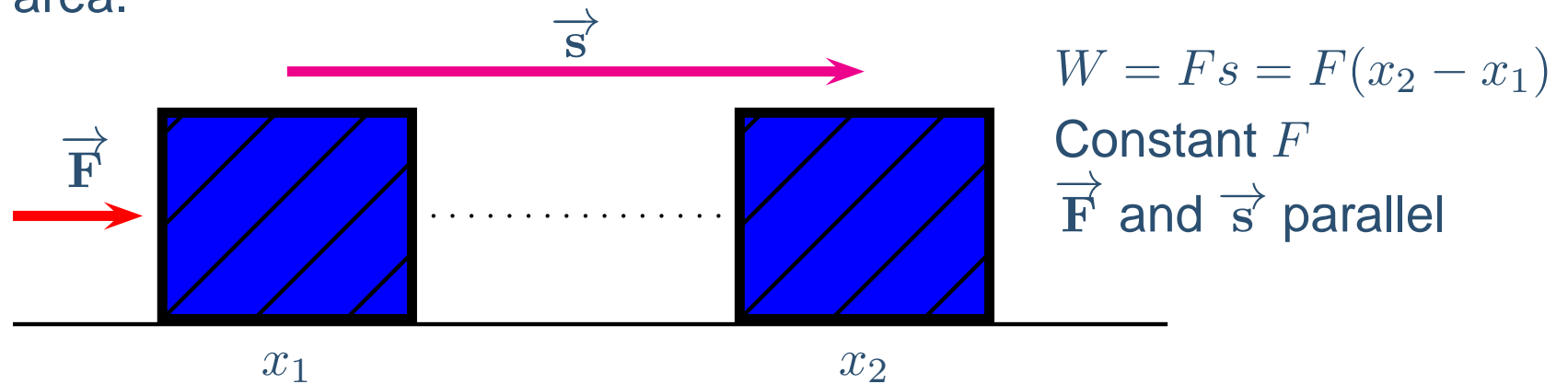


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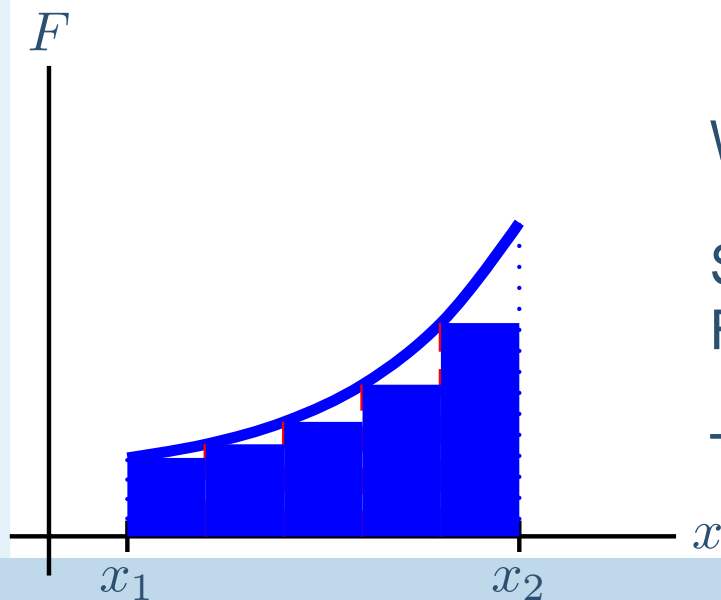
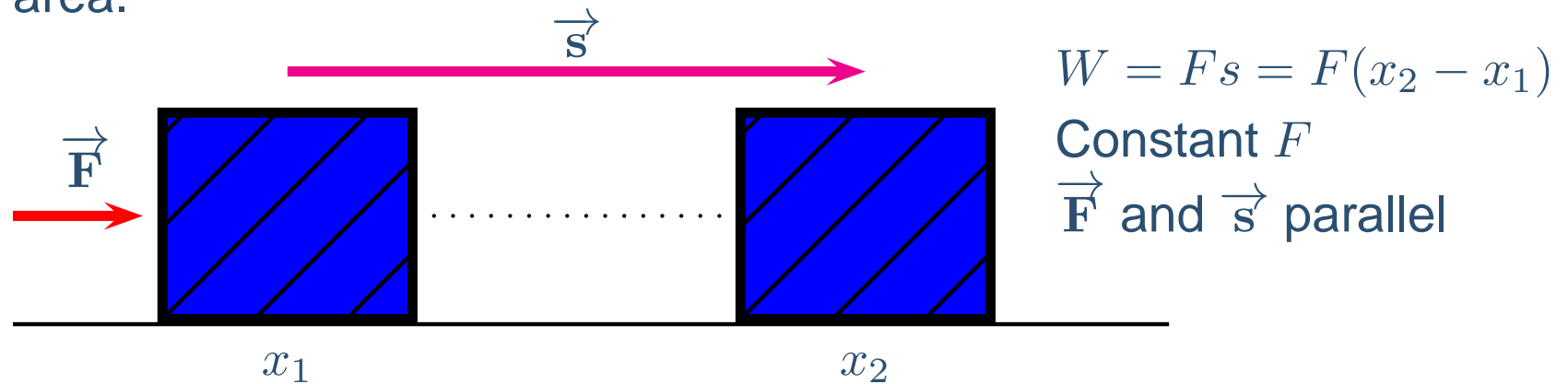


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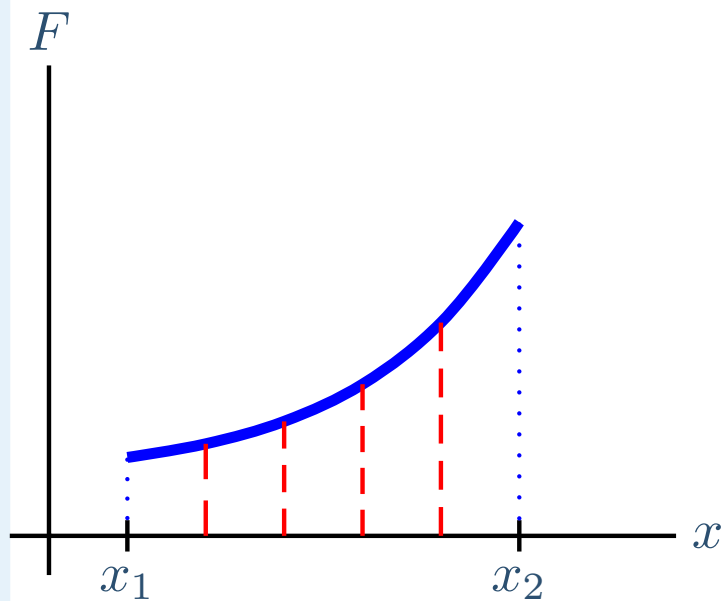
Work is the area under this curve

Split region into many small rectangles.
Find area of each rectangle and add.

Take a limit to find the exact area.

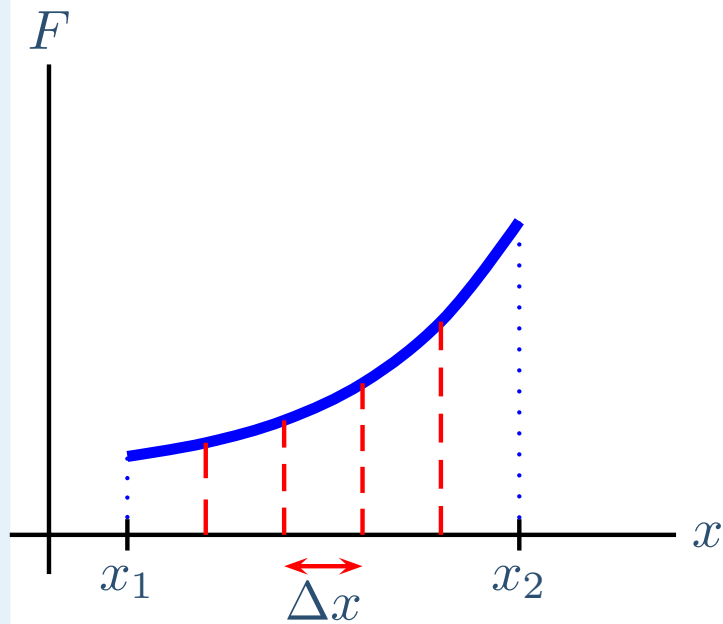
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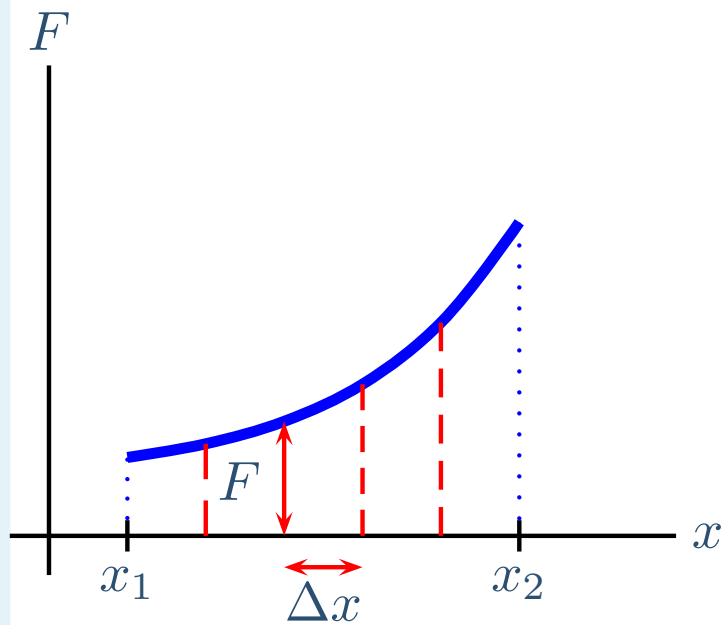
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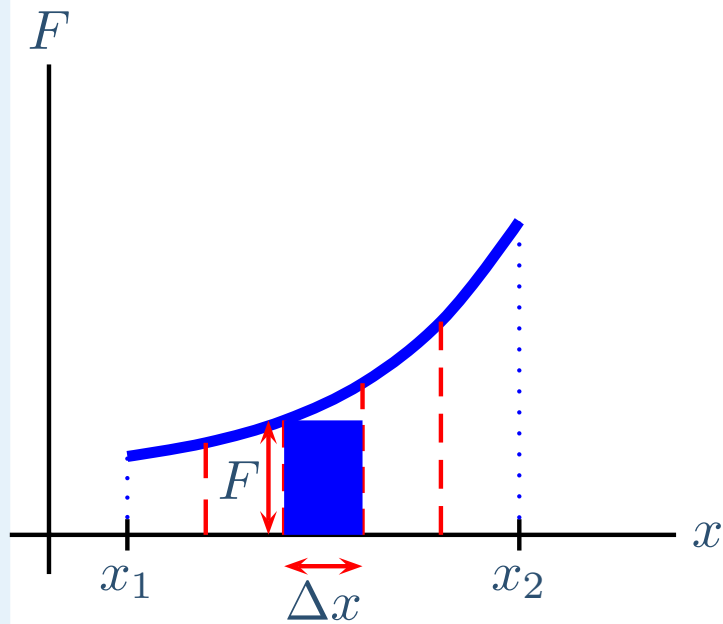
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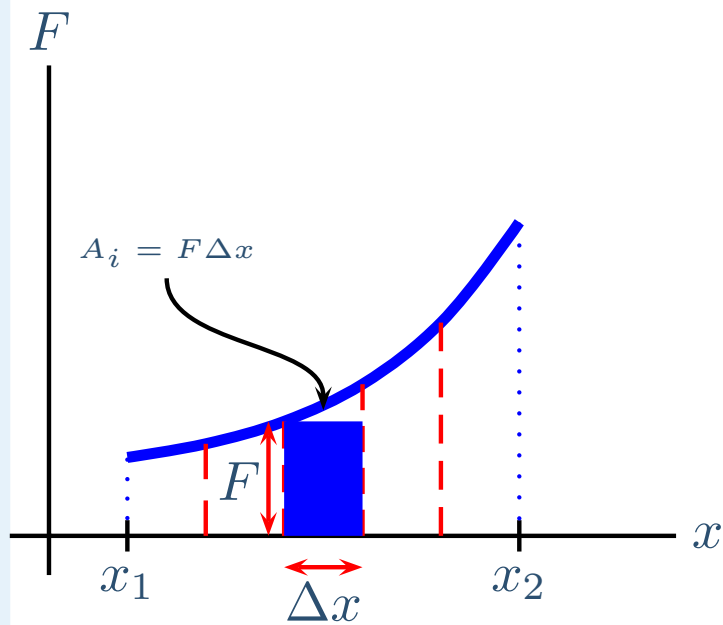
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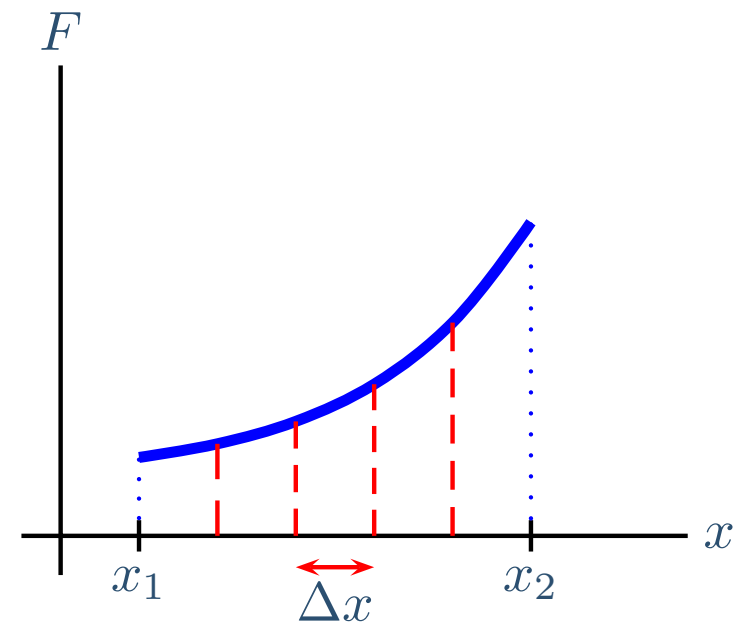
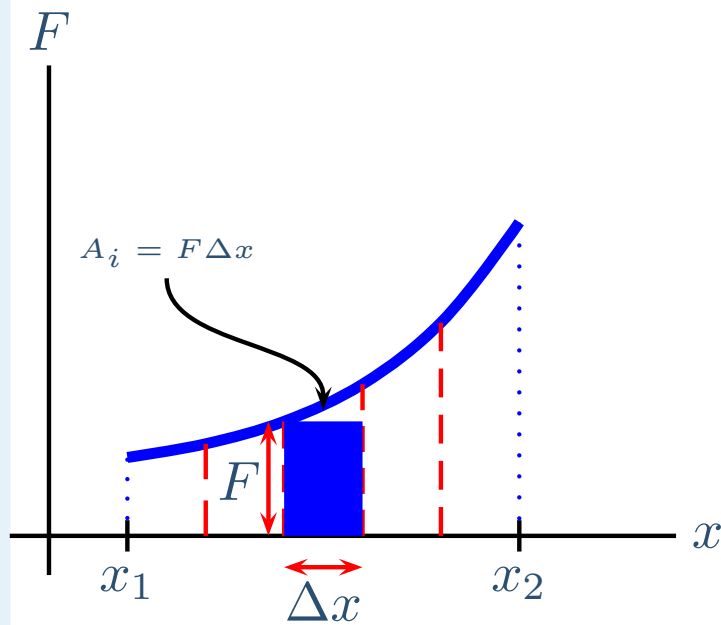
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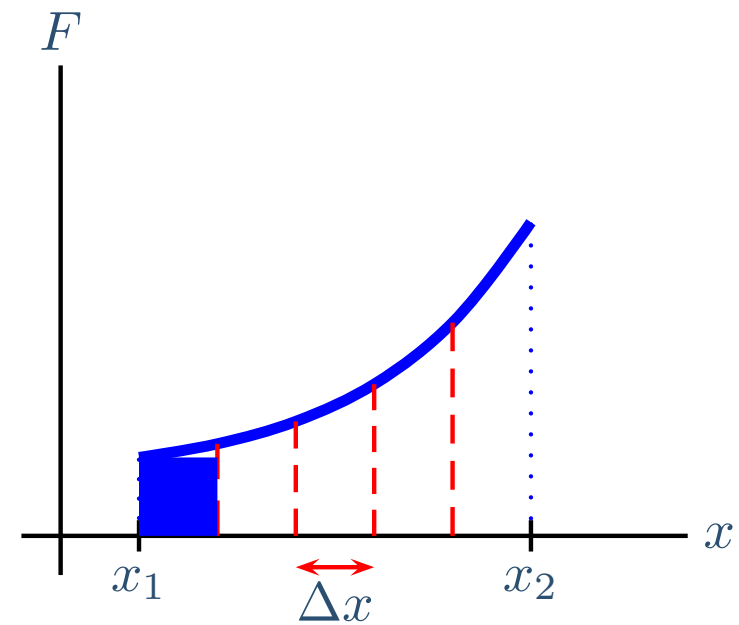
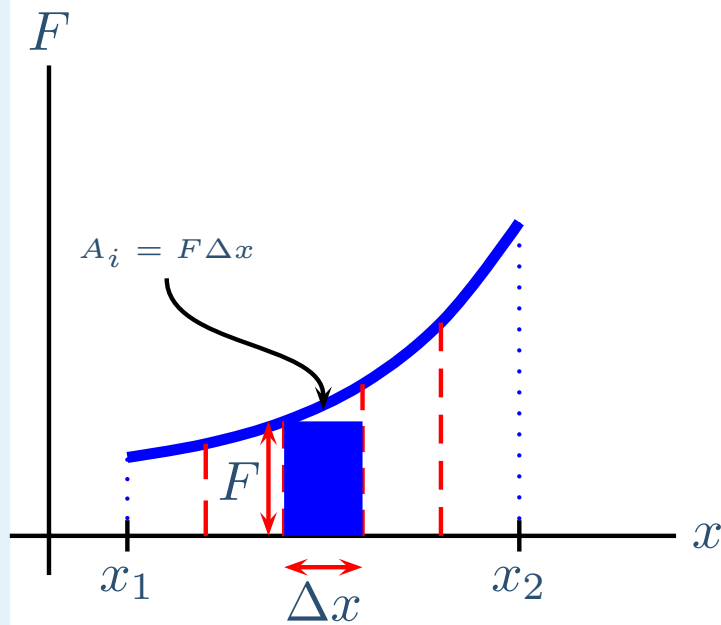
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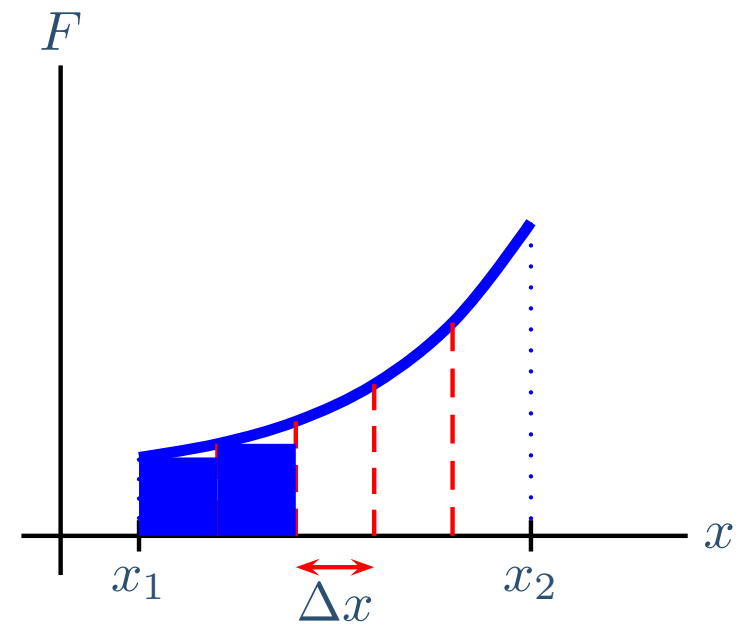
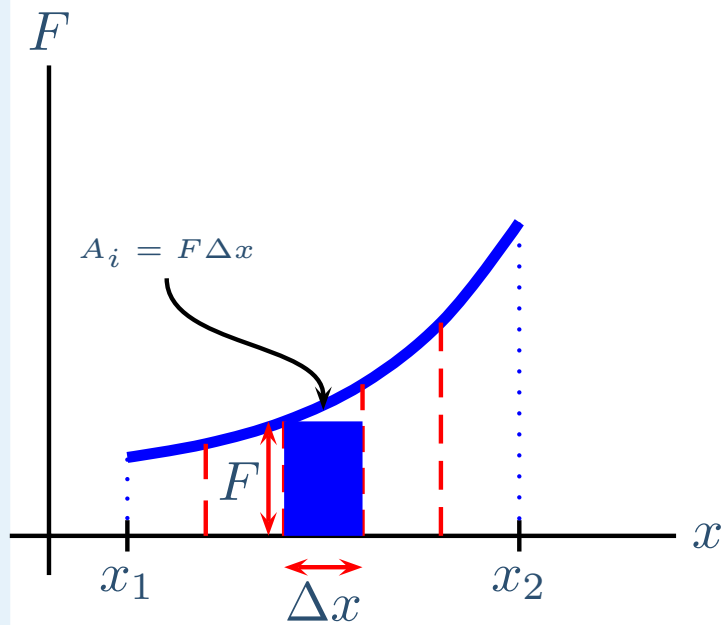
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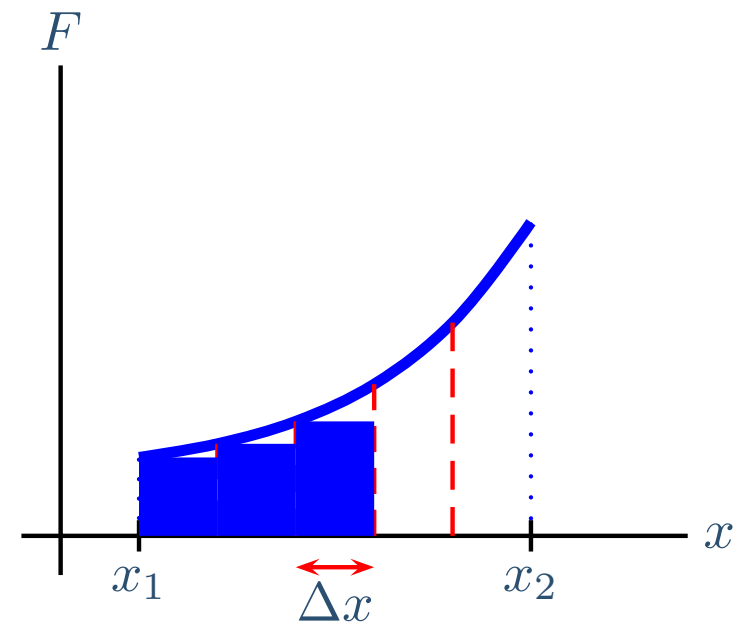
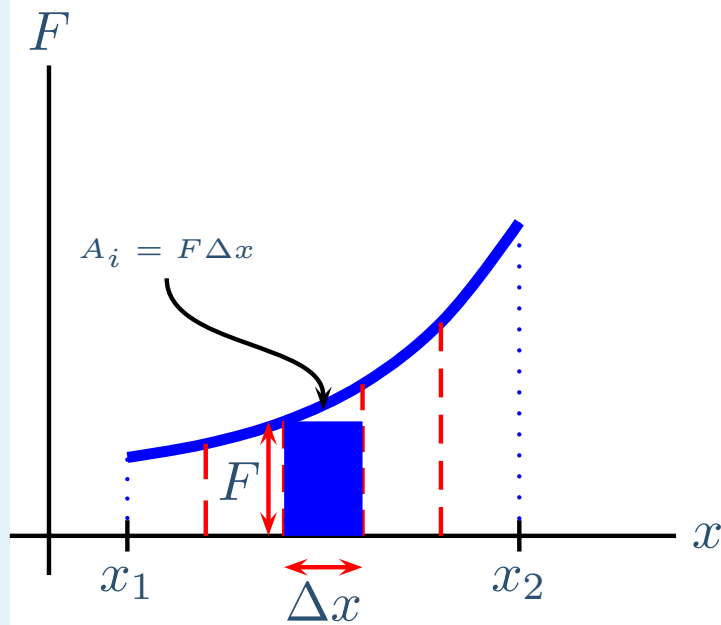
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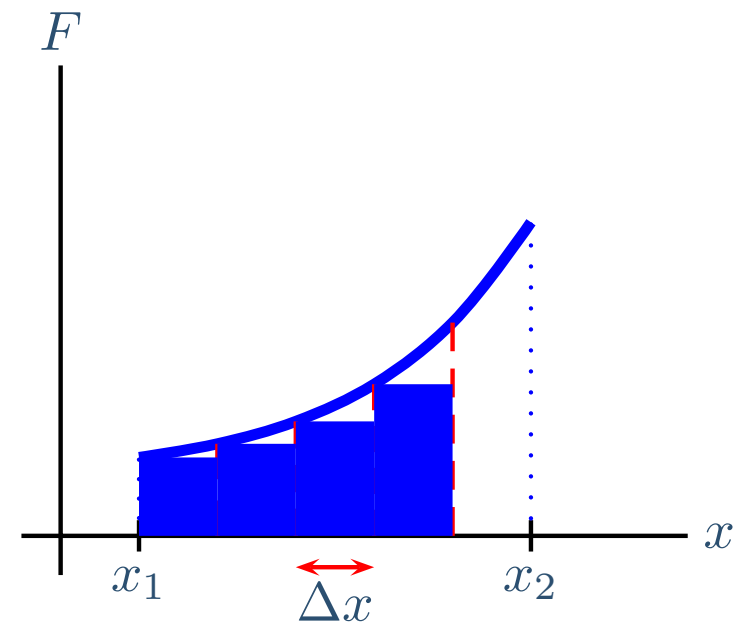
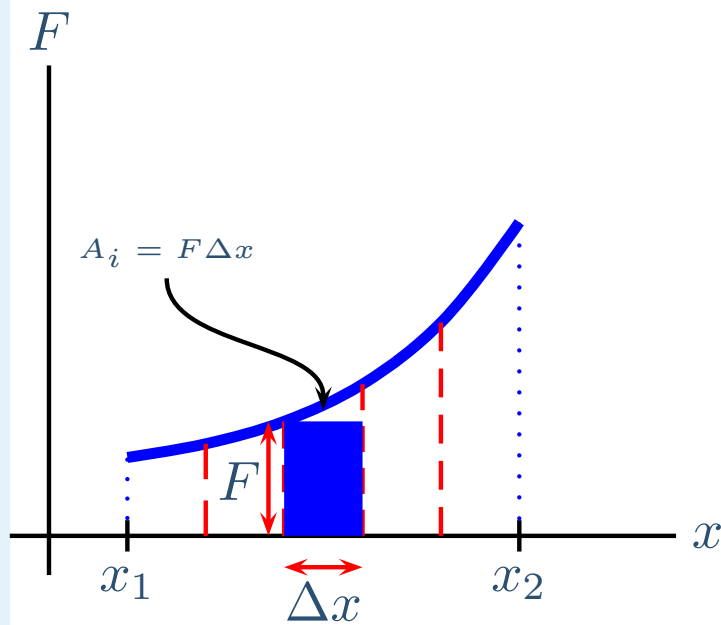
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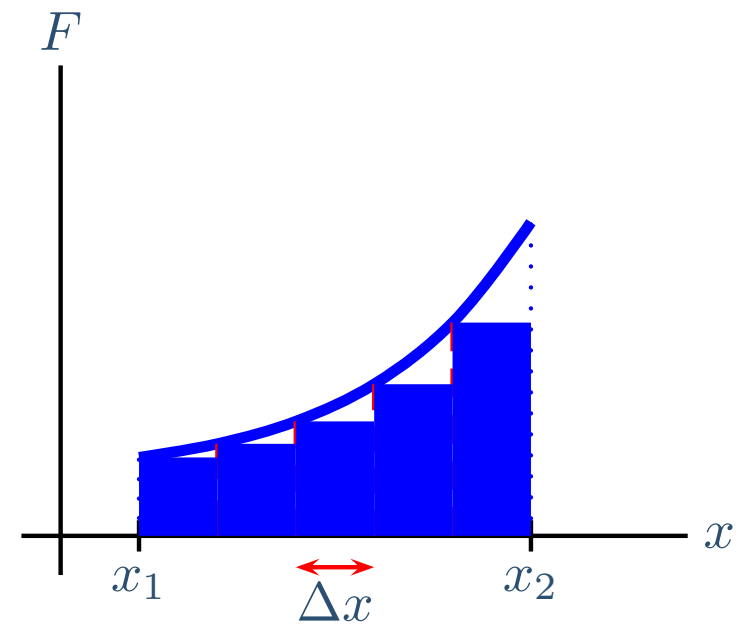
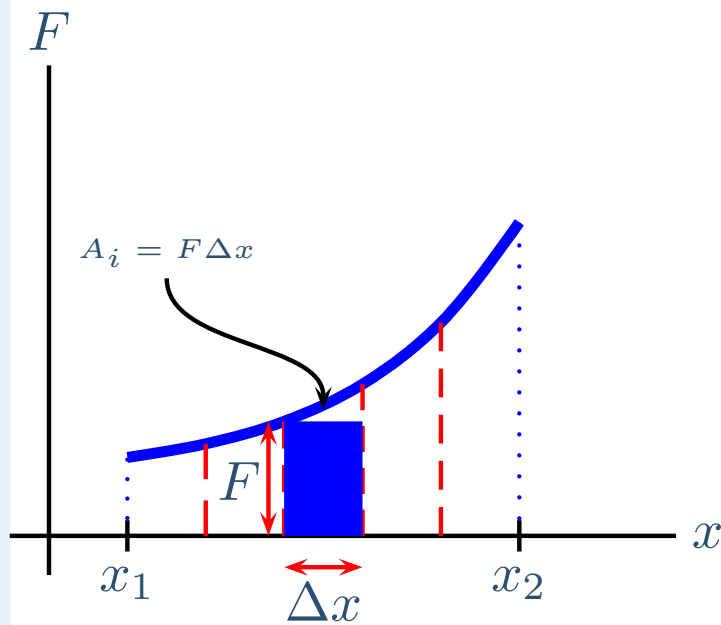
Variable Forces III

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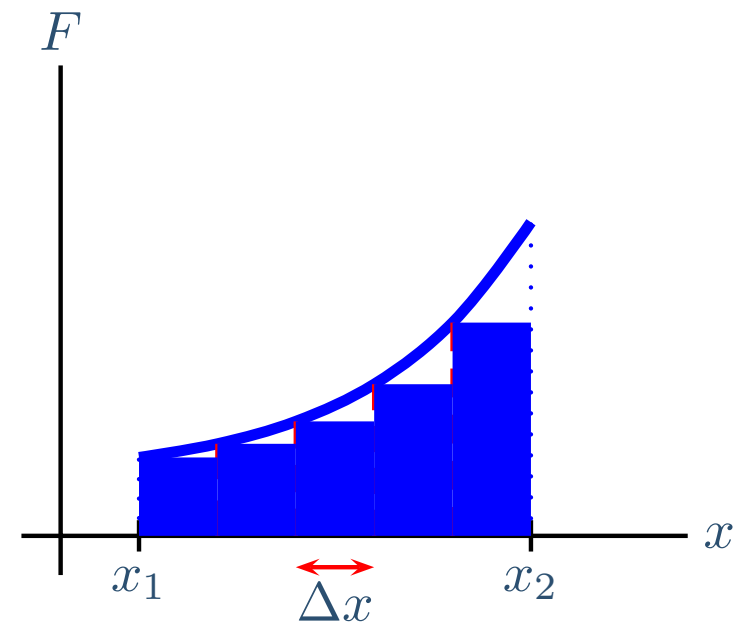
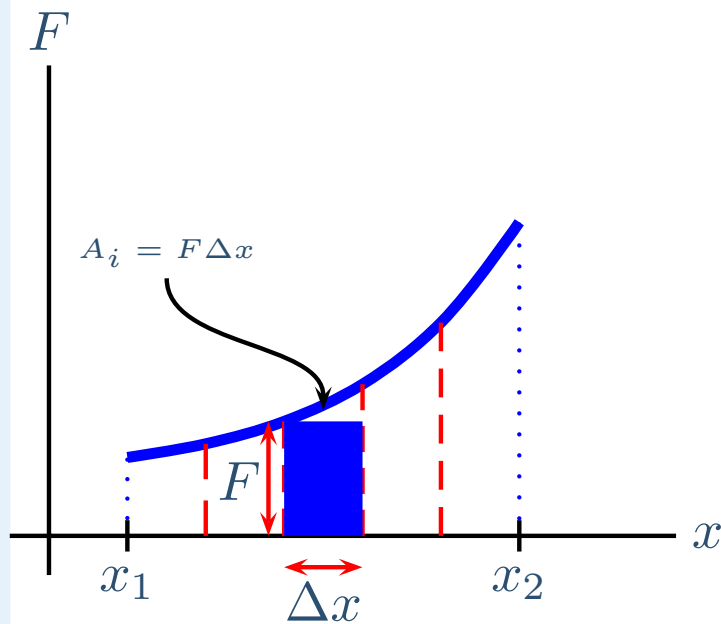
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Variable Forces III

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$$W \approx \sum_i A_i = \sum_i F \Delta x$$

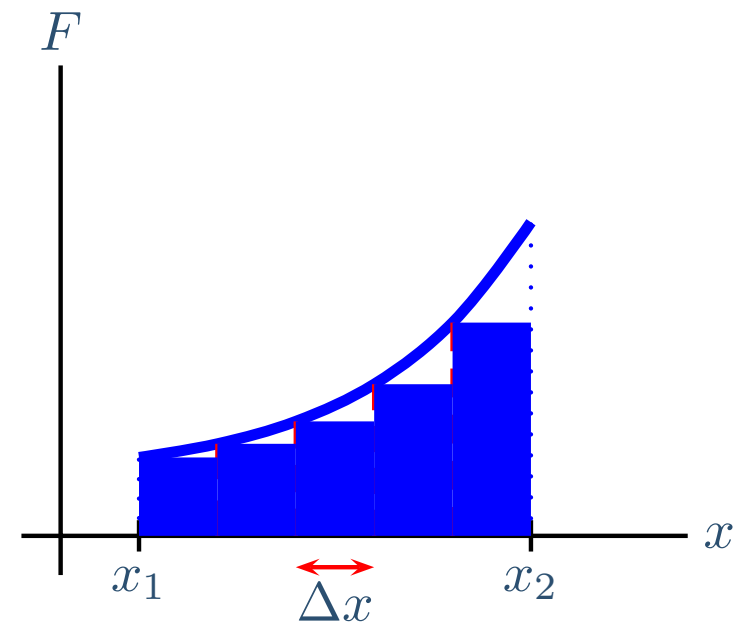
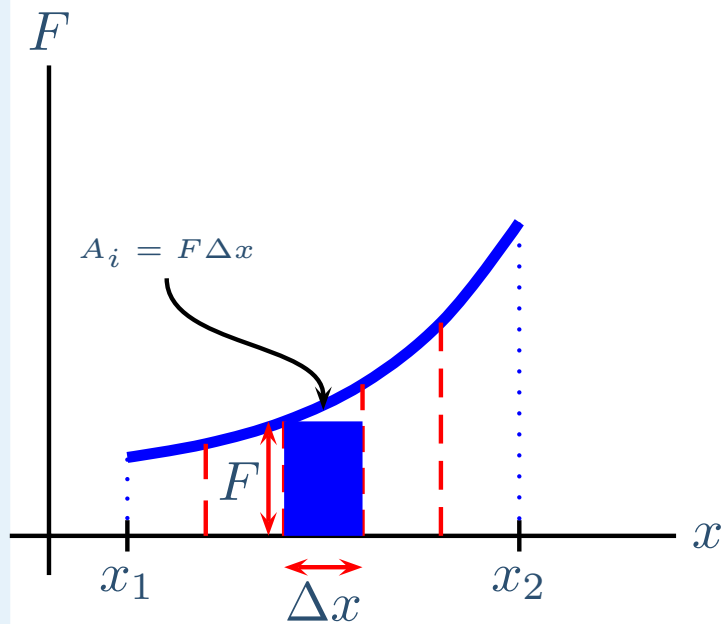


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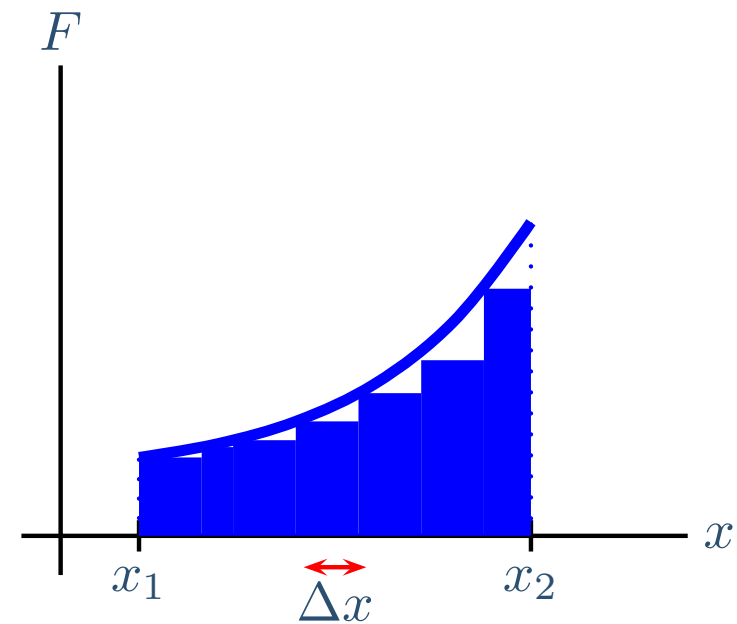
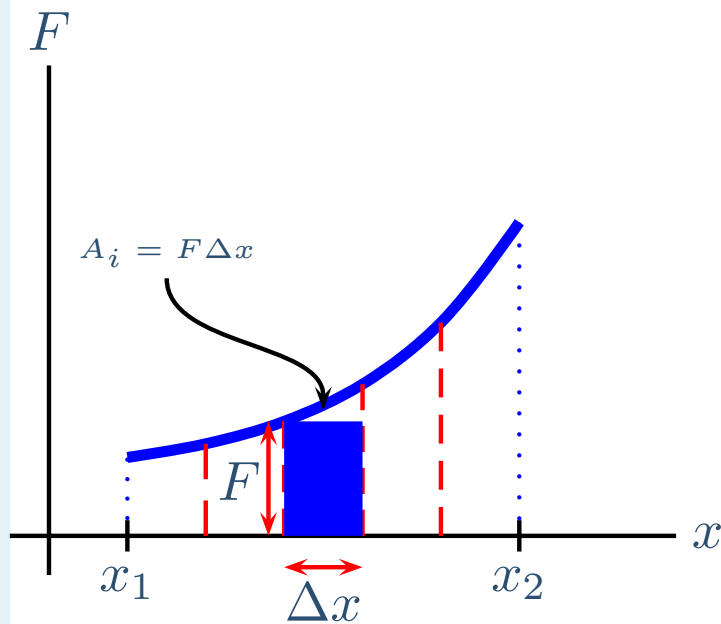


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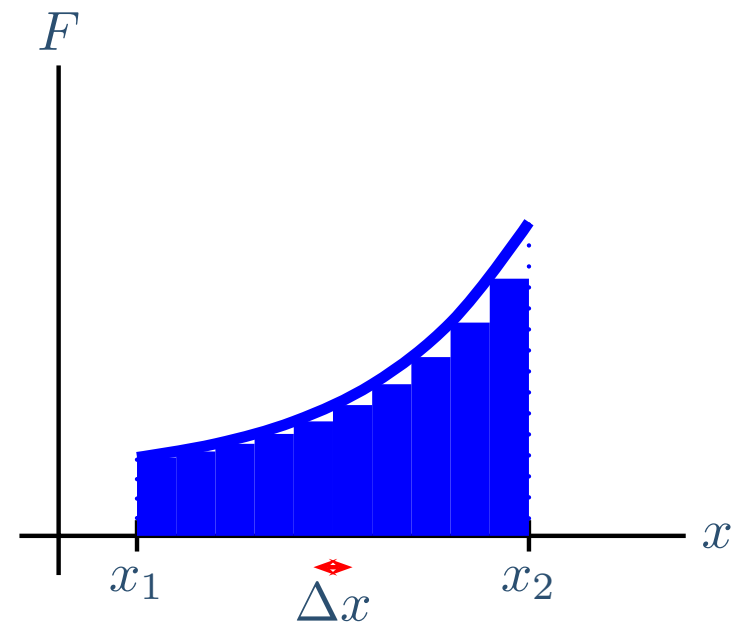
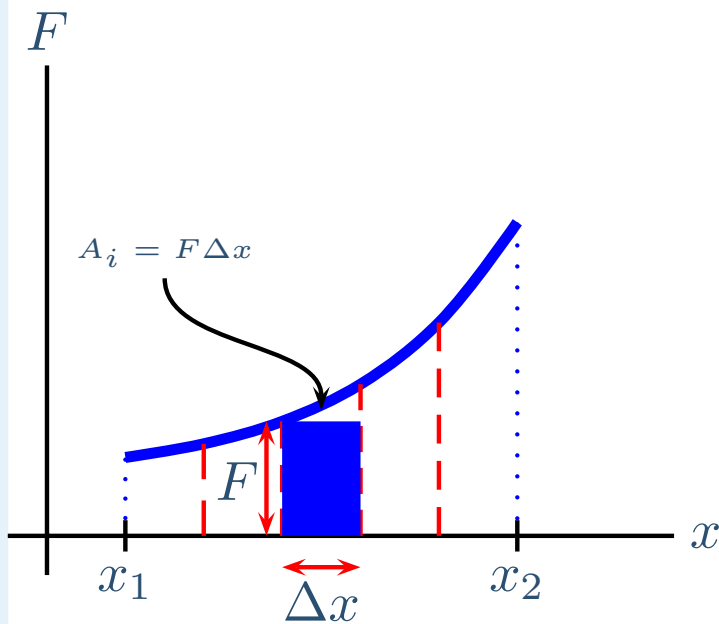


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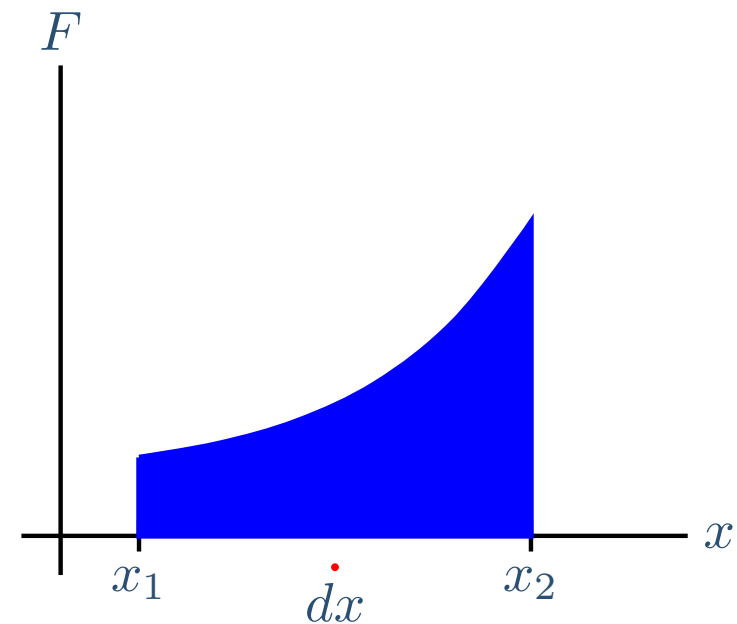
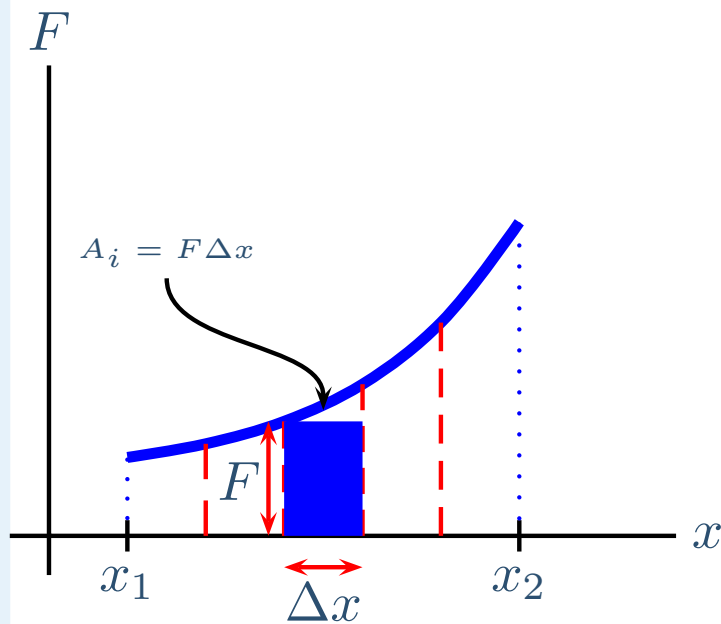


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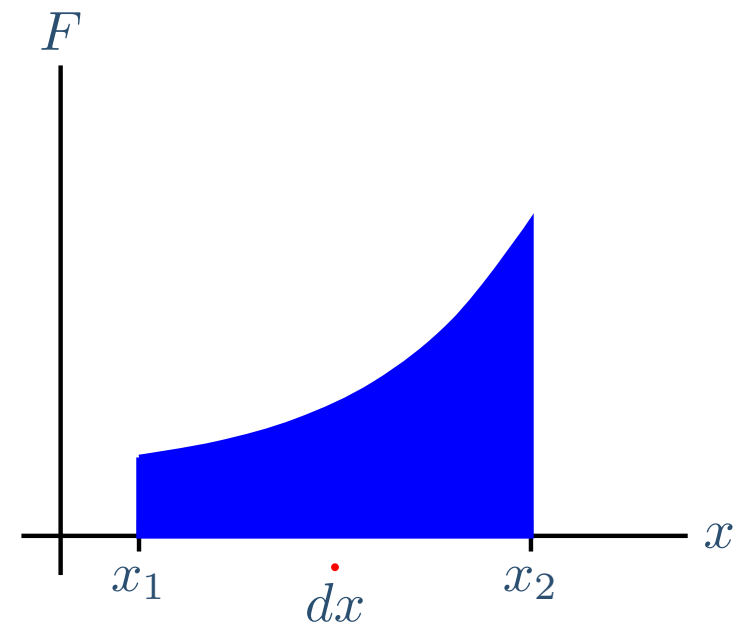
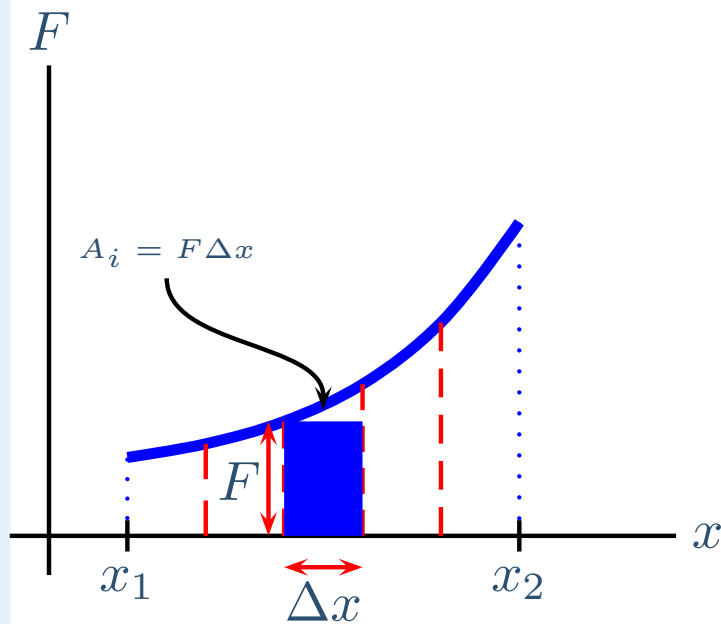


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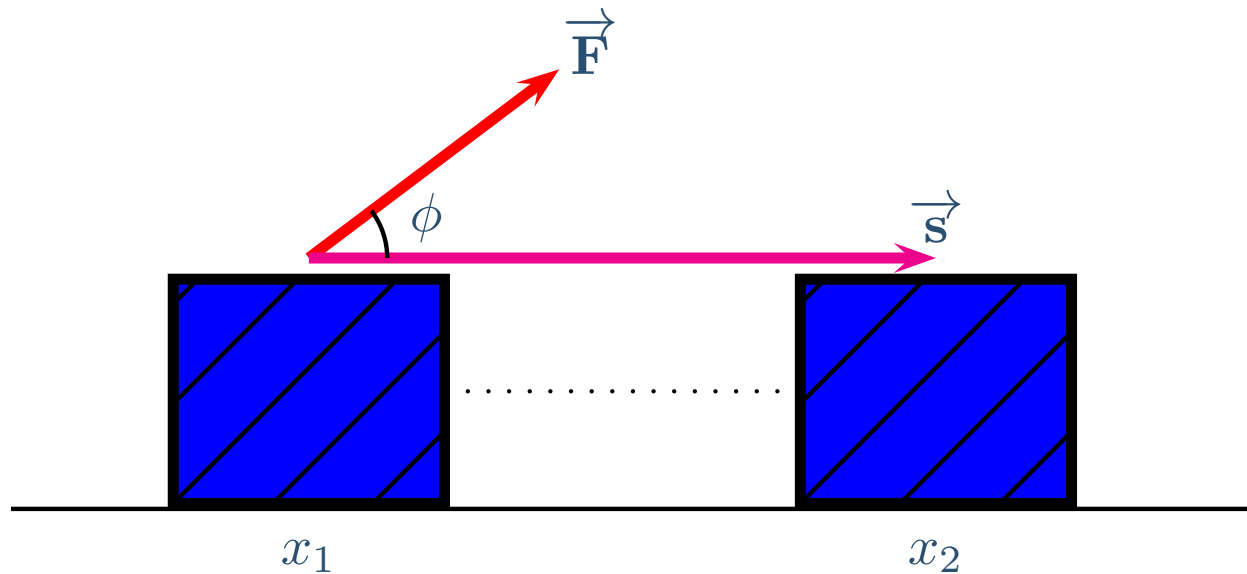
$$W = \lim_{\Delta x \rightarrow 0} \sum F \Delta x = \int_{x_1}^{x_2} F dx$$



Variable Force Arbitrary Direction

Still only the component of the force parallel to the displacement does work.

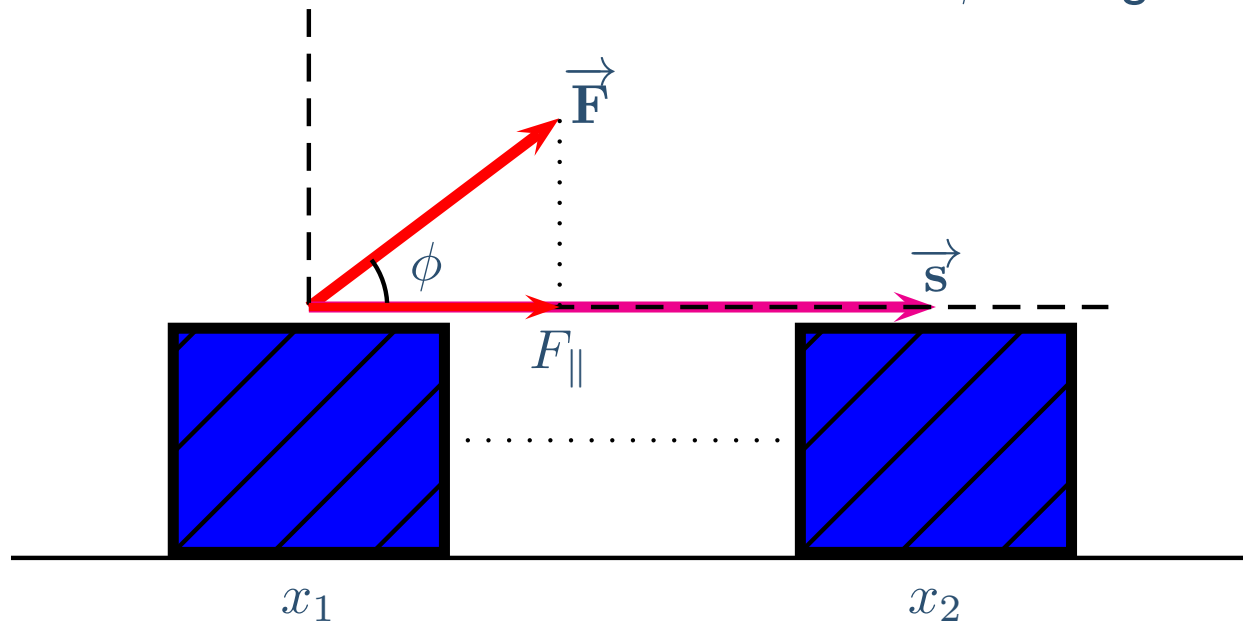
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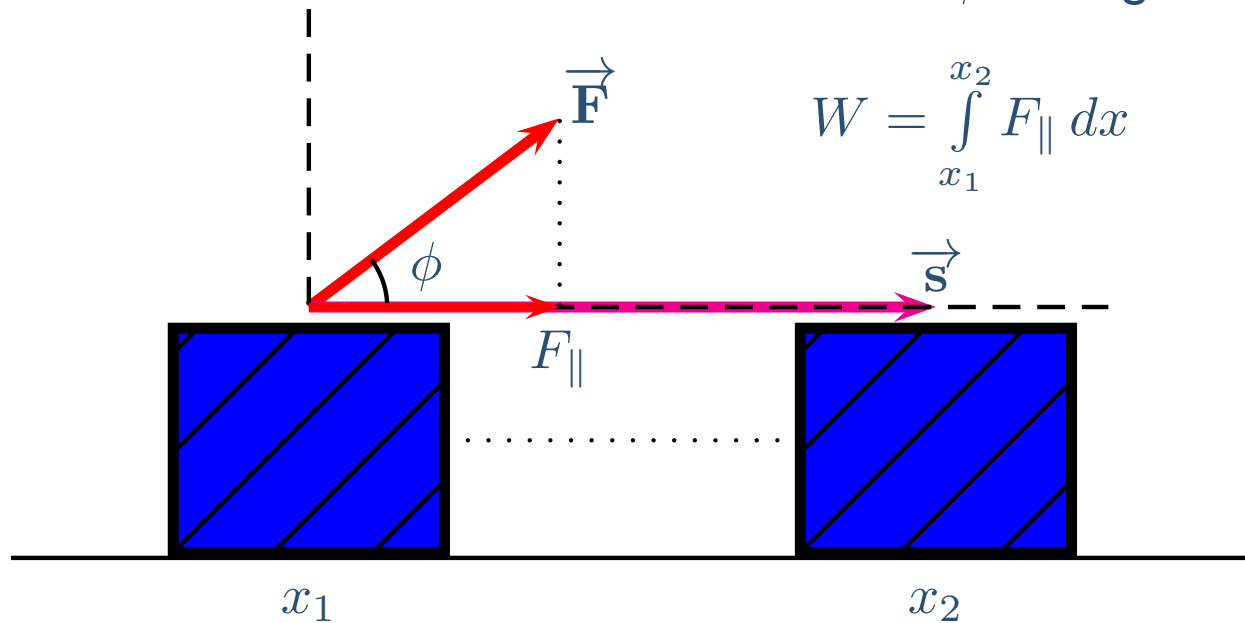


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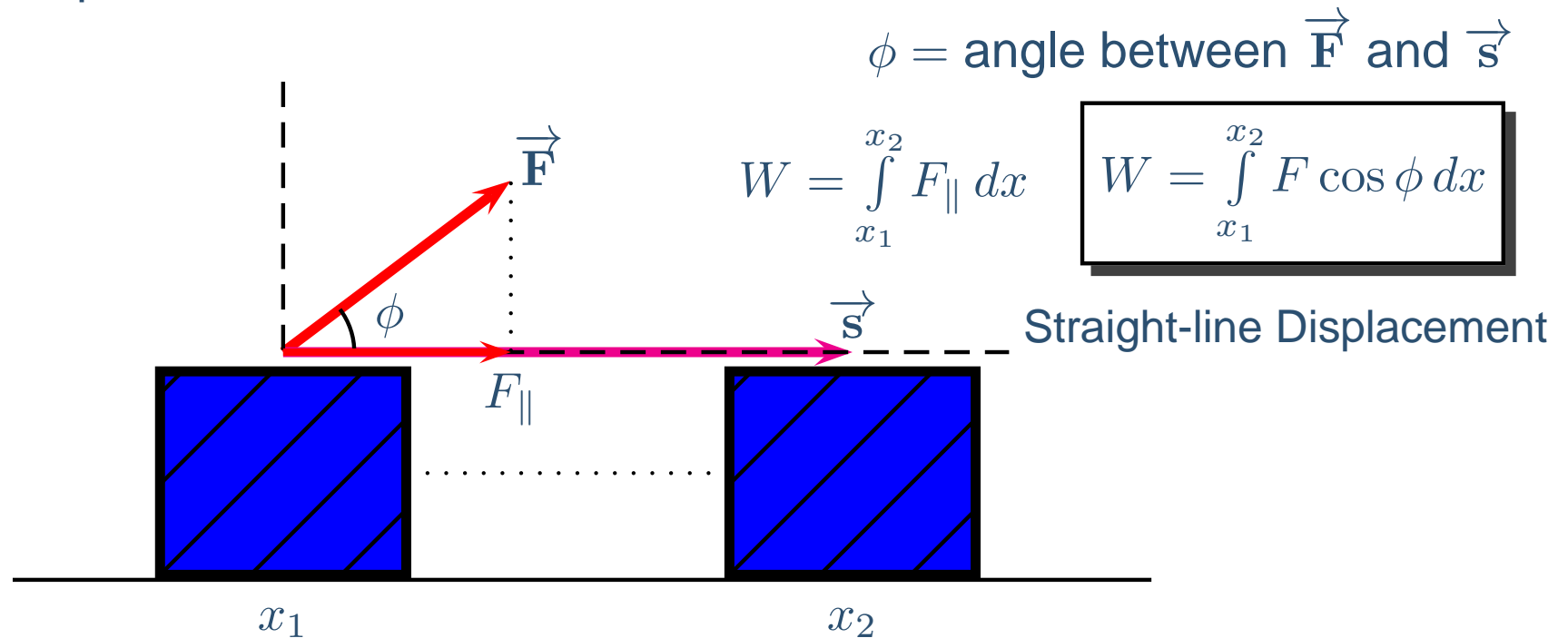
$\phi = \text{angle between } \vec{F} \text{ and } \vec{s}$

$$W = \int_{x_1}^{x_2} F_{\parallel} dx$$



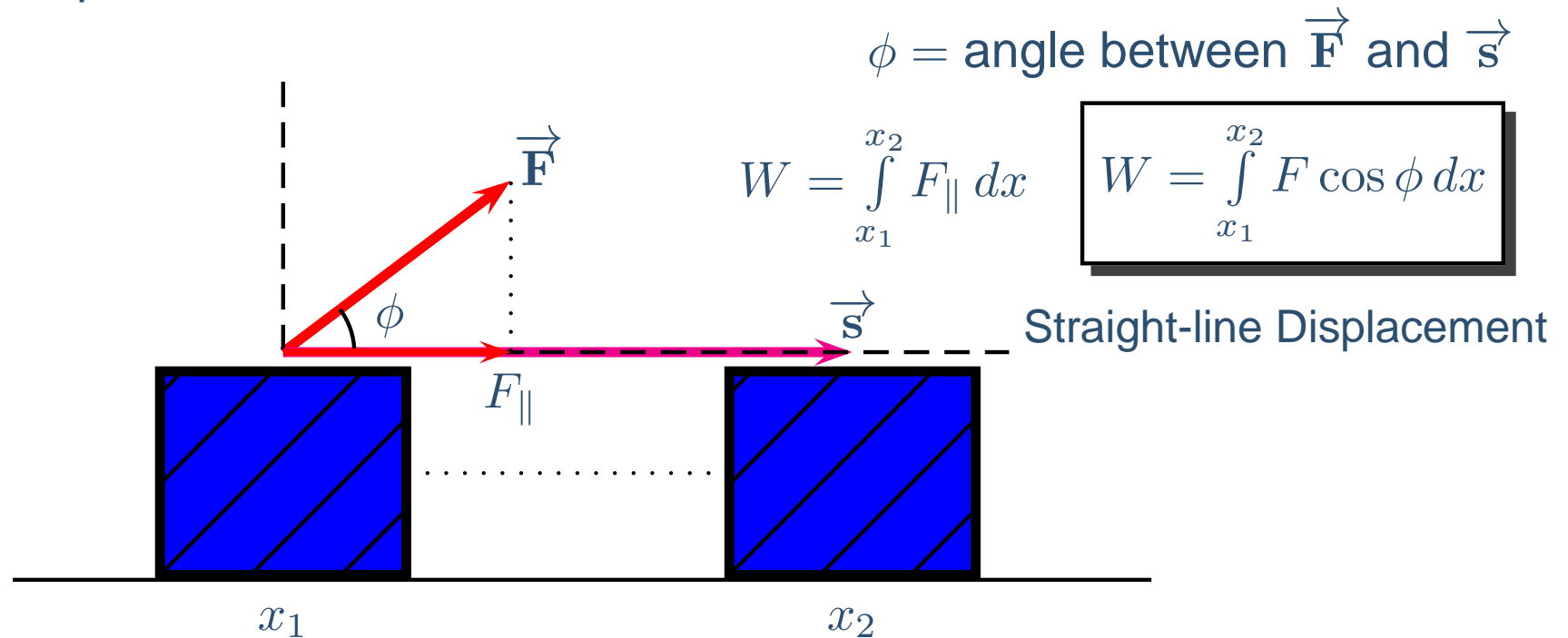
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For variable forces, it can be shown that the work-energy theorem

holds! $W_{total} = \frac{1}{2}mv_2^2 - \frac{1}{2}mv_1^2$