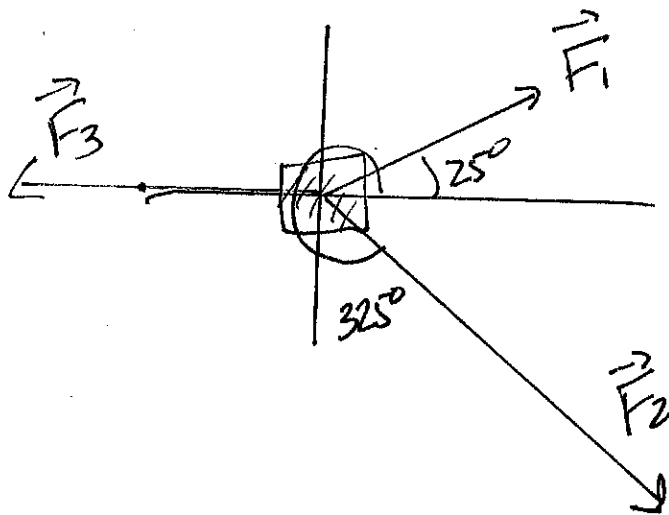


Physics 160, HW #5

TEN Mastering Physics From Chapter 4 & 5

Written: 5.74

# MOTION OF A BLOCK WITH 3 FORCES



$$F_1 = 4\text{N}$$

$$F_2 = 6\text{N}$$

$$F_3 = 8\text{N}$$

A: Calculate Magnitude of  $\vec{F}_R = \sum \vec{F}$

$$\vec{F}_R = \vec{F}_1 + \vec{F}_2 + \vec{F}_3$$

$$\Rightarrow F_{R,x} = F_{1,x} + F_{2,x} + F_{3,x} = 4\text{N} \cos 25^\circ + 6\text{N} \cos 325^\circ - 8\text{N}$$

to left

(STANDARD ANGLES  $\Rightarrow$  COSINE)  $\Rightarrow F_{R,x} = 0.54\text{N}$

$$F_{R,y} = F_{1,y} + F_{2,y} + F_{3,y} = 4\text{N} \sin 25^\circ + 6\text{N} \sin 325^\circ + 0$$

$$= 1.69\text{N} - 3.44\text{N} = -1.75\text{N}$$

WE COULD ALSO USE  $360^\circ - 325^\circ = 35^\circ$

AND PUT THE NEGATIVE IN BY HAND

$$4\text{N} \sin 25^\circ - 6\text{N} \sin 35^\circ = -1.75\text{N}$$

$$F_R = \sqrt{F_{R,x}^2 + F_{R,y}^2} = \sqrt{(0.54\text{N})^2 + (1.75\text{N})^2} = 1.83\text{N}$$

PART B: WHAT ANGLE  $F_{R,x} > 0$ ,  $F_{R,y} < 0 \Rightarrow$  4th QUADRANT, SO CALCULATOR CORRECT

$$\theta = \tan^{-1}\left(\frac{F_{R,y}}{F_{R,x}}\right) = \tan^{-1}\left(\frac{-1.75}{0.54}\right) = -72.9^\circ = -73^\circ$$

PART C: WHAT IS MAGNITUDE OF  $\vec{a}$ ?

$\sum \vec{F} = M\vec{a}$  DOES MEAN THAT  $|\sum \vec{F}| = M a$  <sup>MAGNITUDE</sup>

$$\text{OR IN THIS CASE } F_R = M a \Rightarrow a = \frac{F_R}{M} = \frac{1.83\text{N}}{2\text{kg}}$$

$$= 0.915\text{m/s}^2 \\ = 0.92\text{m/s}^2$$

Part D: Direction of  $\vec{a}$ ,  $\sum \vec{F} = M\vec{a}$

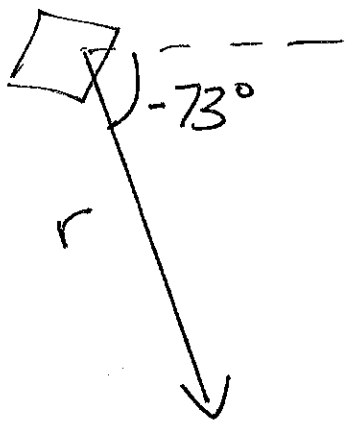
$\Rightarrow$  SAME DIRECTION SO  $-73^\circ$

Part E: How far? SINCE MASS STARTS FROM

REST, IT WILL MOVE IN DIRECTION OF  $\vec{F}_R = \sum \vec{F}$

$\vec{F}_R$  CONSTANT  $\Rightarrow$  STRAIGHT LINE MOTION WITH

CONSTANT ACCELERATION. TO AVOID CONFUSION WITH X,  
CALL DISTANCE COVERED  $r$ . (NOTE, THIS ALSO ANSWERS G  
SINCE MOVING AT  $-73^\circ$ )



$$r = r_0 + v_0 t + \frac{1}{2} a t^2$$

$$r_0 = 0, v_0 = 0$$

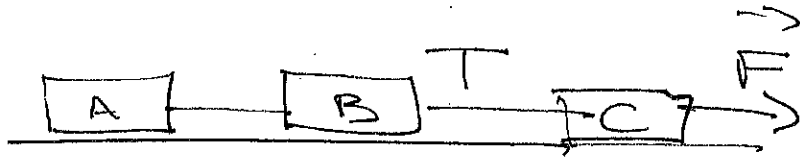
$$\Rightarrow r = \frac{1}{2} a t^2 = \frac{1}{2} (9.2 \text{ m/s}^2) (5 \text{ s})^2$$

$$= 11.5 \text{ m} = 12 \text{ m}$$

Part F:  $v = ?$  at 5s?  $v = v_0 + a t$  FOR SAME

REASONS  $\Rightarrow v = 0 + (9.2 \text{ m/s}^2) (5 \text{ s}) = 4.6 \text{ m/s}$

# Pulling 3 Blocks



$$T = 3\text{N}$$

$$m_A = m_B = m_C = .4\text{kg}$$

Part A: What is magnitude of  $F$ ?

All 3 masses must have SAME Acceleration

Magnitude AND Direction  $\Rightarrow a_{A,x} = a_{B,x} = a_{C,x}$   
 $= a$

Forces on A:  $\vec{T}_{AB}$  to right,  $\vec{n}_A$  <sup>up</sup>,  $\vec{w}_A$  Horizontal Surface

Forces on B:  $\vec{T}_{BA}$  to left,  $\vec{T}$  to right,  $\vec{n}_B$  <sup>up</sup>,  $\vec{w}_B$

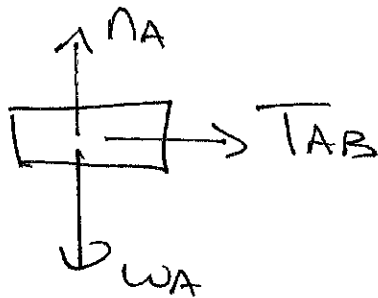
↑  
Massless

Rope  $\Rightarrow$  EQUAL tension

Forces on C:  $\vec{F}$  to right,  $\vec{T}$  to left,  $\vec{n}_C$  up,  $\vec{w}_C$

# Free-Body Diagrams

$M_A$ :



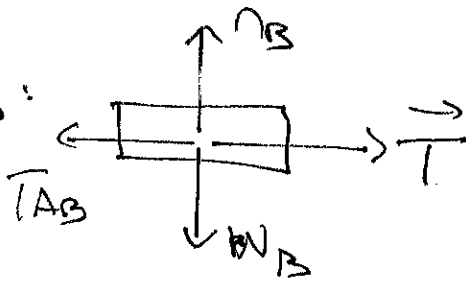
$$\sum F_{A,x} = M_A a_{A,x}$$

$$\Rightarrow T_{AB} = (.4 \text{ kg}) a \quad (1)$$

$$\sum F_{A,y} = 0 \text{ since } a_{A,y} = 0$$

$$\Rightarrow N_A = W_A$$

$M_B$ :

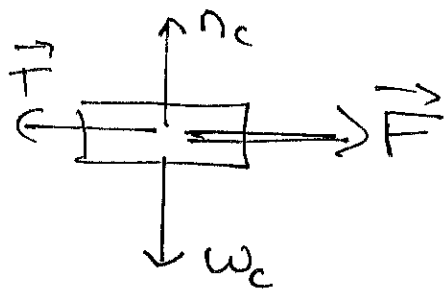


$$\sum F_{B,x} = M_B a_{B,x}$$

$$\Rightarrow T - T_{AB} = (.4 \text{ kg}) a \quad (2)$$

$$\sum F_{B,y} = 0 \Rightarrow N_B = W_B$$

$M_C$ :



$$\sum F_{C,x} = M_C a_{C,x}$$

$$\Rightarrow F - T = (.4 \text{ kg}) a \quad (3)$$

$$\sum F_{C,y} = 0 \Rightarrow N_C = W_C$$

(1)  $\Rightarrow T_{AB} = (.4 \text{ kg}) a$  so substitute into (2)

$$\Rightarrow T - (.4 \text{ kg}) a = (.4 \text{ kg}) a \Rightarrow T = (.8 \text{ kg}) a$$

$$\Rightarrow a = \frac{T}{.8 \text{ kg}} = \frac{3 \text{ N}}{.8 \text{ kg}} = 3.75 \text{ m/s}^2$$

So (3) BECOMES :

$$F - T = (.4 \text{ kg})a \Rightarrow F = T + (.4 \text{ kg})a$$

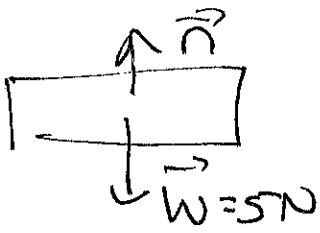
$$\Rightarrow F = 3 \text{ N} + (.4 \text{ kg})(3.75 \text{ m/s}^2) = 3 \text{ N} + 1.5 \text{ N} \\ = 4.5 \text{ N}$$

PART B: What is  $T_{AB}$ ?

$$(1) \Rightarrow T_{AB} = (.4 \text{ kg})a = (.4 \text{ kg})(3.75 \text{ m/s}^2) = 1.5 \text{ N}$$

## BOOK ON TABLE

A: DOWNWARD FORCE ON BOOK = GRAVITY

B:   $\vec{n}$  = UPWARD FORCE ON BOOK  
EXERTED BY TABLE

$$\sum F_y = 0 \Rightarrow n - w = 0 \Rightarrow n = w = 5N$$

C:  $\vec{n}$  AND  $\vec{w}$  ARE NOT 3<sup>RD</sup> LAW PAIRS BECAUSE  
THEY ARE EXERTED ON THE SAME OBJECT.

D: THE REACTION TO GRAVITY: IF THE EARTH  
PULLS DOWN ON THE BOOK, THE BOOK PULLS  
UP ON THE EARTH.

E: REACTION TO NORMAL: IF THE TABLE PUSHES  
UP ON THE BOOK, THE BOOK PUSHES DOWN  
ON THE TABLE.



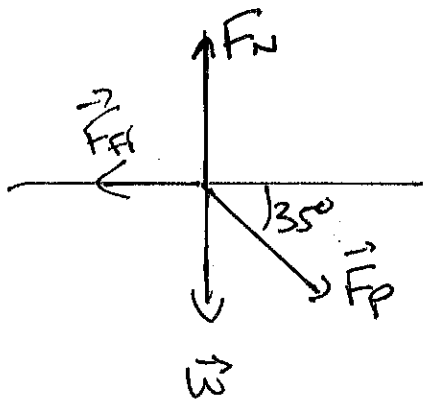
F: As shown Above  $\sum F_y = M a_y$

Shows  $\uparrow = W \Rightarrow 1^{st}$  or  $2^{nd}$  Law

G: Newton's 3<sup>rd</sup> Law tells us Action AND REACTION ARE EQUAL.

# FREE BODY DIAGRAMS AND Newton's Laws

Part A:



$$M = 55 \text{ kg}, \vec{F}_P = 148 \text{ N},$$

35° Below  
Horizontal

So  $\vec{W} = Mg$  -  
Down

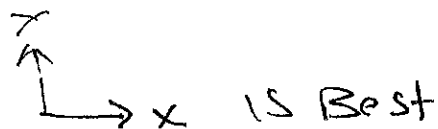
$$W = 539 \text{ N}$$

Friction,  $F_{fr} = 100 \text{ N}$

Friction opposite to velocity  
 $\Rightarrow$  to LEFT

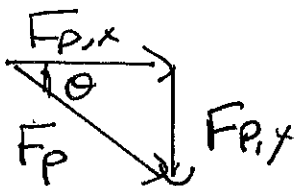
NORMAL,  $F_N$ , HORIZONTAL FLOOR  $\Rightarrow$  upwards

B: Given up, down, left forces usual Cartesian



C:

$$\sum F_x = F_{P,x} - F_{fr} \quad \text{since } F_N, W \text{ ARE BOTH VERTICAL}$$



$$\cos \theta = \frac{F_{P,x}}{F_P} \Rightarrow F_{P,x} = F_P \cos \theta$$

$$\Rightarrow \sum F_x = F_p \cos \theta - F_{fr}$$

Part D:

$\sum F_y = ?$  AS SHOWN ON LAST PAGE  $F_{p,y}$  IS DOWN

~~$\vec{W}$~~  IS DOWN,  $\vec{F}_N$  IS UP

$$\Rightarrow \sum F_y = F_N - W - F_{p,y}$$

From Previous:

$$\sin \theta = \frac{F_{p,y}}{F_p} \Rightarrow F_{p,y} = F_p \sin \theta$$

$$\therefore \sum F_y = F_N - W - F_p \sin \theta \quad \text{OR to use}$$

$$\text{their notation, } \sum F_y = F_N - F_G - F_p \sin \theta$$

Notice, We put Negative sign in by HAND

So we'll set  $\theta = +35^\circ$  AT END OF PROBLEM.

Part E:

$$\Sigma F_x = M a_x, \quad \Sigma F_y = M a_y$$

NO MOTION IN  $y$ -DIRECTION  $\Rightarrow a_y = 0, a_x = a = ?$

$$\Sigma F_x = M a_x \Rightarrow F_p \cos \theta - F_{fr} = M a_x$$

$$\Rightarrow 148 \text{ N} \cos 35^\circ - 106 \text{ N} = 55 \text{ kg } a_x$$

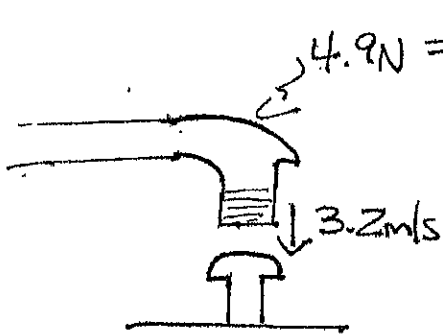
$$\Rightarrow 15.2345 \text{ N} = 55 \text{ kg } a \Rightarrow a = \frac{15.2345 \text{ N}}{55 \text{ kg}} = 0.277 \text{ m/s}^2$$

$$\Sigma F_y = M a_y \Rightarrow F_N - W - F_p \sin \theta = 0$$

$$\Rightarrow F_N = W + F_p \sin \theta = 539 \text{ N} + 148 \text{ N} \sin 35^\circ$$

$$\Rightarrow F_N = 624 \text{ N}$$

4.52



$$4.9\text{ N} = W \rightarrow \vec{W} = 4.9\text{ N, Down}$$

STOPPED IN  $.45\text{ cm} = 4.5 \times 10^{-3}\text{ m}$

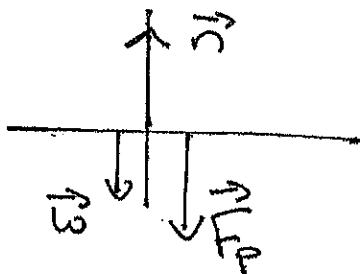
ADDITIONAL 15N DOWNWARD

FORCE APPLIED BY PERSON

$$\Rightarrow \vec{F}_P = 15\text{ N, Down}$$

a) DRAW FBD FOR HAMMER HEAD

FORCES ON HAMMER:  $\vec{W}$ ,  $\vec{F}_P$ , AND NAIL PUSHES UP ON HAMMER, SOLID OBJECTS  $\Rightarrow$  NORMAL FORCE,  $\vec{N}$



1) REACTION FORCES:  $\vec{W} \rightarrow$  EARTH PULLS DOWN ON HAMMER WITH 4.9N  $\Rightarrow$  REACTION = UPWARDS 4.9N pull ON EARTH

$\vec{F}_P \rightarrow$  PERSON PUSHES DOWN ON HAMMER WITH 15N  $\Rightarrow$

REACTION = UPWARDS 15N PUSH ON PERSON

$\vec{n}$   $\rightarrow$  NAIL PUSHES UP ON HAMMER  $\Rightarrow$   
 HAMMER PUSHES DOWN ON NAIL WITH  
 FORCE MAGNITUDE  $n$ .  $\rightarrow$  THIS IS WHAT  
 PUSHES THE NAIL INTO THE BOARD.

b.  $n = ?$        $\Sigma F_y = Ma_y$

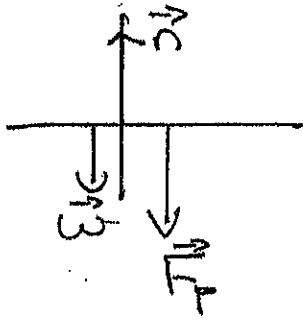
Assuming Constant ACCELERATION  $\Rightarrow V_y^2 = V_{0,y}^2 + 2a_y(y - y_0)$

FOR HAMMER:  $V_y = 0$ ,  $V_{0,y} = -3.2 \text{ m/s}$ ,  $y - y_0 = -4.5 \times 10^{-3} \text{ m}$   
 $\uparrow$  stops       $\nwarrow$  DOWN IS NEGATIVE       $\nwarrow$  HAMMER GOES DOWNWARD while STOPPING

$$\therefore 0 = (-3.2 \text{ m/s})^2 + 2a_y(-4.5 \times 10^{-3} \text{ m})$$

$$\Rightarrow 0 = 10.24 \text{ m}^2/\text{s}^2 + a_y(-9 \times 10^{-3} \text{ m}) \Rightarrow a_y = \frac{-10.24 \text{ m}^2/\text{s}^2}{-9 \times 10^{-3} \text{ m}}$$

$\Rightarrow a_y = +1137.78 \text{ m/s}^2 \leftarrow$  UPWARDS ACCELERATION  
 BECAUSE SLOWING DOWN



$$W = Mg \Rightarrow 4.9\text{N} = M(9.8\text{m/s}^2)$$

$$\Rightarrow M = \frac{4.9\text{N}}{9.8\text{m/s}^2} = 0.5\text{kg}$$

$$\downarrow$$

$$\text{Unit: } \frac{\text{N}}{\text{m/s}^2} = \frac{\text{kg} \cdot \text{m/s}^2}{\text{m/s}^2} = \text{kg}$$

$$\Sigma F_y = Ma_y \Rightarrow n - w - F_p = Ma_y$$

$$\Rightarrow n - 4.9\text{N} - 15\text{N} = 0.5\text{kg}(1137.78\text{m/s}^2) = 568.89\text{N}$$

$$\Rightarrow n = 4.9\text{N} + 15\text{N} + 568.89\text{N} \Rightarrow \boxed{n = 588.7889\text{N}} \\ = 589\text{N}$$

c) IF  $y = -0.12\text{cm} = -1.2 \times 10^{-3}\text{m}$  what is  $n$ ?

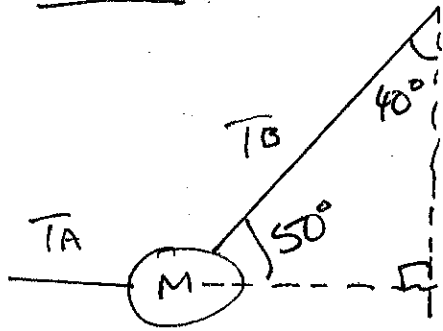
$$a_y = \frac{-(3.2\text{m/s})^2}{2(-1.2 \times 10^{-3}\text{m})} = 4266.67\text{m/s}^2$$

SAME FBD  $\Rightarrow \Sigma F_y = Ma_y \Rightarrow n - w - F_p = Ma_y$

$$\Rightarrow n - 4.9\text{N} - 15\text{N} = 0.5\text{kg}(4266.67\text{m/s}^2)$$

$$\Rightarrow \boxed{n = 2153.2 = 2150\text{N}}$$

5.6 :



$$M = 4090 \text{ kg}$$

Forces on M:  $\vec{T}_A$  to left,

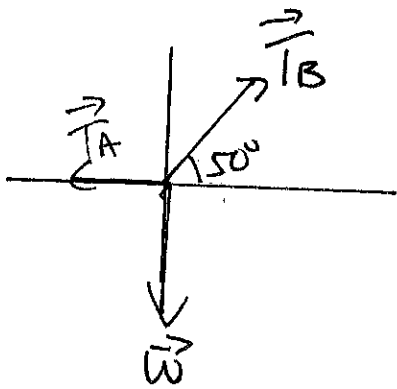
$\vec{T}_B$  at  $50^\circ$

$\vec{W}$  Down.

A: what is  $T_B$ ?

$$W = (4090 \text{ kg})(9.8 \text{ m/s}^2)$$

$$= 40082 \text{ N}$$



$$\sum F_x = M a_x$$

$$\sum F_y = M a_y$$

$a_x = 0, a_y = 0$  since not moving

$$\sum F_y = 0 \Rightarrow T_{B,y} - W = 0. \quad 50^\circ = \text{STANDARD ANGLE}$$

$$\Rightarrow T_B \sin 50^\circ - W = 0 \Rightarrow T_B = \frac{W}{\sin 50^\circ} = \frac{40082 \text{ N}}{\sin 50^\circ} =$$

$$52323 \text{ N} = 52000 \text{ N}$$

Part B :

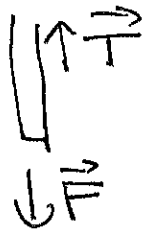
$$\sum F_x = 0 \Rightarrow T_{B,x} - T_A = 0 \Rightarrow T_B \cos 50^\circ - T_A = 0$$

$$\Rightarrow T_A = T_B \cos 50^\circ = 52323 \cos 50^\circ = 33632 \text{ N} = 34000 \text{ N}$$



# THE WINDOW WASHER

First, look AT THE END OF THE MASSLESS ROPE



$$\sum F_y = M_{\text{rope}} a_{\text{rope},y}$$

$$M_{\text{rope}} = 0 \Rightarrow T - F = 0 \Rightarrow F = T$$

$\Rightarrow$  WE REALLY NEED TO FIND TENSION  
IN ROPE.

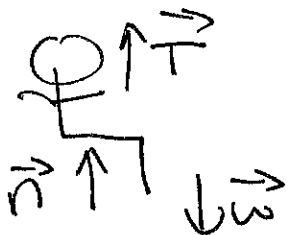
MINIMUM TENSION?

I RECOMMEND taking THIS ONE APART, CONSIDER  
THE MAN AND THE PLATFORM SEPARATELY

ON MAN: ROPE pulls up ON MAN  $\Rightarrow \vec{T}$  up

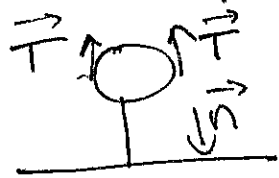
GRAVITY pulls DOWN,  $\Rightarrow \vec{W} = Mg$  DOWN

AND A NORMAL FORCE FROM INCLINE  $\Rightarrow \vec{n}$  up



$$\sum F_y = M a_y \Rightarrow T + n - W = M_{\text{man}} a_{\text{man}}$$

ON THE PLATFORM: (including Pulley)



3RD LAW  $\Rightarrow$  DOWNWARD force

$\vec{n}$  ON platform, ~~REP~~

ROPE IS DOUBLED  $\Rightarrow$  TWO UPWARD

TENSION FORCES  $\vec{T}$  (perfect pulleys

$\Rightarrow$  SAME MAGNITUDE OF TENSION)

NOTE, WE SHOULD ALSO HAVE <sup>weight</sup> ~~MASS~~ OF PLATFORM

SINCE IN REALITY IT WOULD BE QUITE HEAVY.

$$\sum F_y = Mg \Rightarrow T + T - n = M_{\text{platform}} a_{\text{platform}}$$

$$\Rightarrow 2T - n = M_{\text{plat}} a_{\text{plat}}. \quad \text{Notice } T \text{ would get}$$

larger WITH ACCELERATION UPWARDS  $\Rightarrow$  MINIMUM  $T$

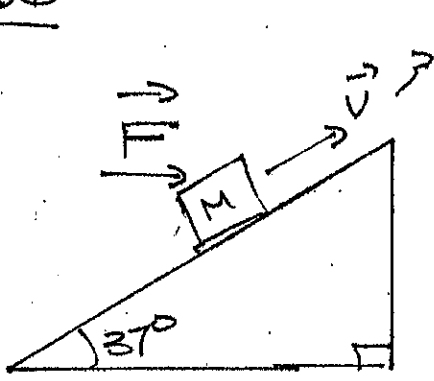
$$\Rightarrow a_{\text{plat}} = 0 \Rightarrow a_{\text{man}} = 0 \text{ too, so}$$

$$2T - n = 0. \quad \text{FROM MAN } T + n - W = 0 \Rightarrow n = W - T$$

$$\text{so substitute: } 2T - (W - T) = 0 \Rightarrow 2T - W + T = 0$$

$$\Rightarrow 3T = W \Rightarrow T = \frac{W}{3} = \frac{Mg}{3}$$

5.66



Box moves up incline  
 $M = 6 \text{ Kg}$   
 $\mu_k = 0.3$

$F = ?$  so mass accelerates at  $4.2 \text{ m/s}^2$

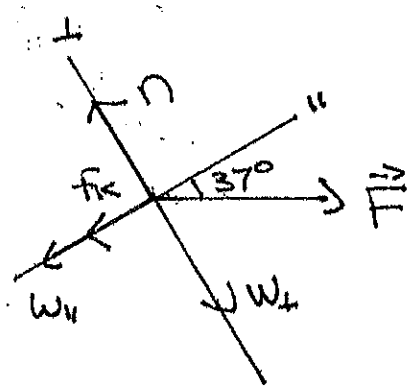
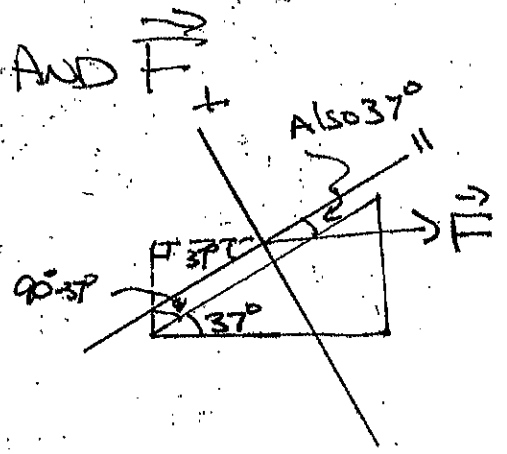
Mass must move parallel to incline  $\Rightarrow a_{||} = 4.2 \text{ m/s}^2$ ,  $a_{\perp} = 0$  still

Forces on mass, incline  $\Rightarrow W_{||} = mg \sin \alpha = (6 \text{ kg})(9.8 \text{ m/s}^2) \sin 37^\circ$   
 $\Rightarrow W_{||} = 35.39 \text{ N}$ ,  $\leftarrow$

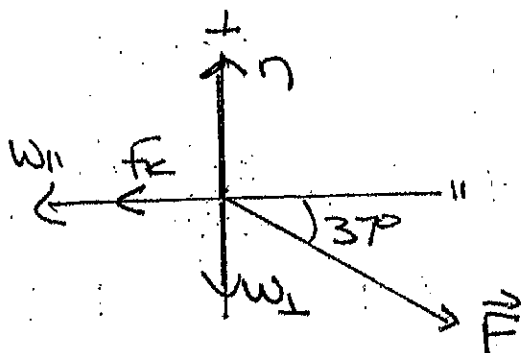
$W_{\perp} = Mg \cos \alpha = (6 \text{ kg})(9.8 \text{ m/s}^2) \cos 37^\circ = 46.96 \text{ N}$ ,  $\searrow$

Normal force,  $\vec{n}$ , at  $90^\circ \Rightarrow \nearrow$

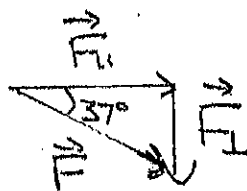
KINETIC friction,  $\vec{f}_k$  at  $\nwarrow$  since mass going up incline



WITHOUT STRAINING NECK:



$$a_{||} = 4.2 \text{ m/s}^2, a_{\perp} = 0$$



$$\sin 37^\circ = \frac{F_{\perp}}{F}$$

$$\Rightarrow F_{\perp} = F \sin 37^\circ$$

$$\cos 37^\circ = \frac{F_{||}}{F} \Rightarrow F_{||} = F \cos 37^\circ$$

$$\sum F_{\perp} = Ma_{\perp} \Rightarrow N - W_{\perp} - F_{\perp} = 0 \Rightarrow N = W_{\perp} + F_{\perp}$$

POINTS  
DOWN

$$\therefore N = 46.96 \text{ N} + F \sin 37^\circ = 46.96 \text{ N} + F(0.602)$$

$$\text{KINETIC FRICTION} \Rightarrow f_k = \mu_k N = 0.3 [46.96 \text{ N} + F(0.602)] \\ = 14.088 \text{ N} + 0.1806 F$$

$$\text{Finally, } \sum F_{||} = Ma_{||} \Rightarrow F_{||} - W_{||} - f_k = Ma_{||}$$

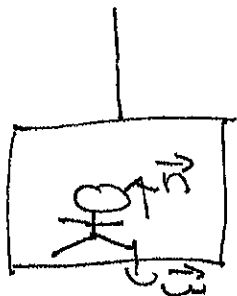
$$\Rightarrow F \cos 37^\circ - 35.39 \text{ N} - [14.088 \text{ N} + 0.1806 F] = (6 \text{ kg})(4.2 \text{ m/s}^2)$$

$$\Rightarrow F(0.799) - 35.39 \text{ N} - 14.088 \text{ N} - 0.1806 F = 25.2 \text{ N}$$

$$\Rightarrow F(0.799 - 0.1806) - 49.478 \text{ N} = 25.2 \text{ N} \Rightarrow F(0.6184) = 74.678 \text{ N}$$

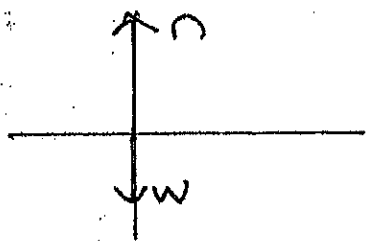
$$\Rightarrow F = \frac{74.678 \text{ N}}{0.6184} = \underline{\underline{120.76 \text{ N} = 121 \text{ N}}}$$

5.78



ACCELERATES OVER 3m  
MAXIMUM SPEED SO THAT  
FORCE EXERTED ON PATIENT  
DOES NOT EXCEED 1.6 THEIR  
WEIGHT.

FORCES ON PATIENT:  $\vec{n}$  UP,  $\vec{w}$  DOWN



$$\sum F_y = Ma_y$$

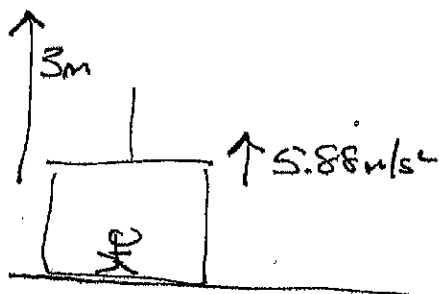
$$\Rightarrow n - w = Ma_y$$

$$\text{at MAX } a_y, n = 1.6w$$

$$\Rightarrow 1.6w - w = Ma_y \Rightarrow (1.6 - 1)w = Ma_y$$

$$\Rightarrow .6w = Ma_y. \quad w = Mg \Rightarrow .6Mg = Ma_y$$

$$\Rightarrow a_y = .6g = .6(9.8 \text{ m/s}^2) = 5.88 \text{ m/s}^2 \leftarrow \text{SAME FOR ALL MASSES!}$$



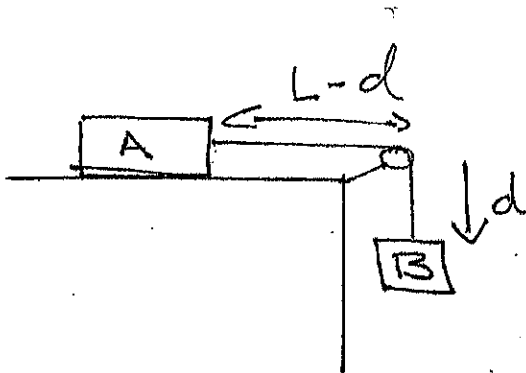
ELEVATOR STARTS FROM REST  $\Rightarrow v_0 = 0$

$$v_y^2 = v_{0y}^2 + 2a_y(y - y_0)$$

$$\Rightarrow v_y^2 = 2(5.88 \text{ m/s}^2)(3\text{m}) = 35.28 \text{ m}^2/\text{s}^2$$

$$\Rightarrow v_y = \sqrt{35.28 \text{ m}^2/\text{s}^2} = 5.94 \text{ m/s} \leftarrow 13 \text{ mi/h}$$

5.83



$M_A, M_B$   
ROPE HAS NON-ZERO  
MASS  $M_{ROPE}$ ,  
TOTAL LENGTH  $L$

0) FIND ACCELERATION WHEN LENGTH  $d$  HANGS VERTICALLY.

TOTAL LENGTH =  $L \Rightarrow (L-d)$  HORIZONTAL TO  
TABLE.

ASSUMING THE ROPE HAS UNIFORM DENSITY  $\Rightarrow$  THE MASS  
OF A LENGTH  $x$  OF THE ROPE WOULD BE  $M = \left(\frac{M_{ROPE}}{L}\right)x$   
S.t. WHEN  $x=L$ ,  $M = M_{ROPE}$  AND  $x=0 \Rightarrow M=0$ .

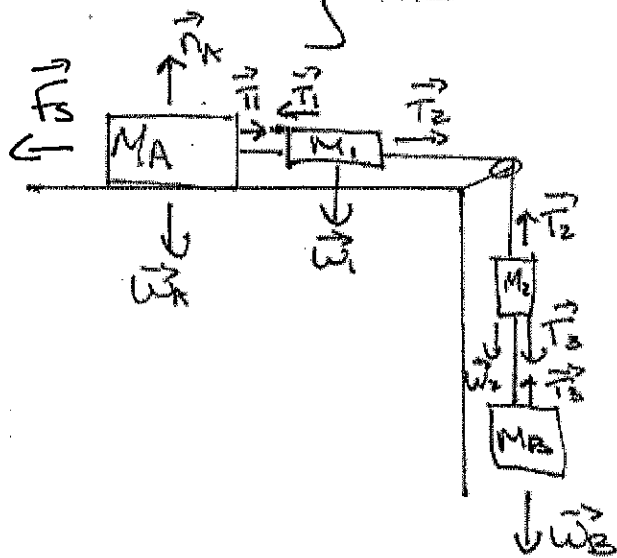
$\therefore$  THE MASS OF THE HORIZONTAL LENGTH IS

$$M_1 = \left(\frac{M_{ROPE}}{L}\right)(L-d) = M_{ROPE} \left(1 - \frac{d}{L}\right)$$

THE MASS OF THE VERTICAL LENGTH IS

$$M_2 = \left(\frac{M_{ROPE}}{L}\right)d = M_{ROPE} \left(\frac{d}{L}\right)$$

IN THE PARTICLE MODEL, WE TREAT  $M_1$  AND  $M_2$  AS DOTS (THOUGH I'LL DRAW THEM AS BOXES TO MAKE THE ANALYSIS EASIER). SO WE'LL HAVE  $M_A$  AND  $M_1$  ON THE TABLE,  $M_2$  AND  $M_B$  HANGING. CONNECTING THEM WILL BE MASSLESS ROPES.



FORCES ON:

$$M_A: \vec{W}_A, \vec{N}_A, \vec{T}_1, \vec{F}_s$$

$$M_1: \vec{T}_1, \vec{W}_1, \vec{T}_2 \rightarrow \text{NOTICE HOW}$$

$\vec{W}_1$  ISN'T BEING CANCELED BY HORIZONTAL  $\vec{T}_1$  AND  $\vec{T}_2$ . THIS IS

WHY IN REALITY THE ROPE WOULD SAG, BUT THAT'S A MUCH HARDER PROBLEM.

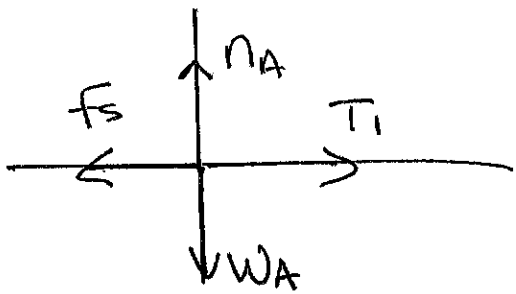
$$M_2: \vec{T}_2, \vec{T}_3, \vec{W}_2$$

$$M_3: \vec{T}_3, \vec{W}_B$$

MINIMUM VALUE OF  $d \Rightarrow F_s = F_{s, \text{MAX}}$  BUT  $a = 0$  STILL

NOTICE FRICTION ONLY ACTING ON  $M_A \Rightarrow F_{s, \text{MAX}} = \mu_s N_A$

$M_A$  Fbd



$$\sum F_{A,x} = M_A a_{A,x}$$

$$\sum F_{A,y} = M_A a_{A,y}$$

$$a_{A,x} = a_{A,y} = 0$$

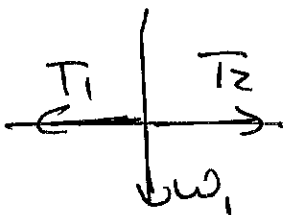
$$\Rightarrow T_1 - F_S = 0 \Rightarrow T_1 = F_S$$

$$n_A - w_A = 0 \Rightarrow n_A = w_A = Mg$$

$$F_S = F_{S,\text{MAX}} = \mu_s n_A \Rightarrow F_S = \mu_s Mg$$

$$T_1 = F_S \Rightarrow T_1 = \mu_s Mg$$

$M_1$  Fbd



AGAIN NOTICE HOW IN REALITY

$\vec{T}_1$  AND  $\vec{T}_2$  WOULD NEED  $y$ -COMPONENTS

TO CANCEL  $w_1$ .

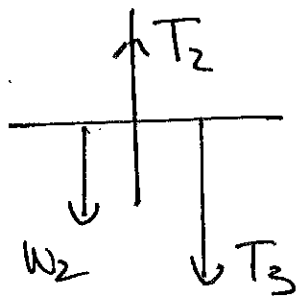
$$\sum F_{1,x} = M_1 a_{1,x} \Rightarrow T_2 - T_1 = 0$$

SINCE  $a_{1,x} = 0$



$$\text{So } T_2 = T_1 = \mu_s M_A g$$

$M_2$  Fbd



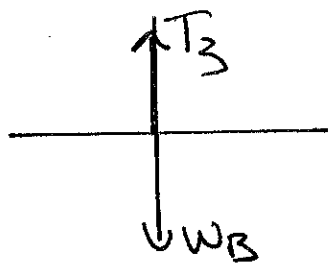
$$\sum F_{2,y} = M_2 a_{2,y} \quad a_{2,y} = 0$$

$$\Rightarrow T_2 - W_2 - T_3 = 0$$

$$\Rightarrow T_3 = T_2 - W_2 = \mu_s M_A g - M_2 g$$

$$= \mu_s M_A g - M_{\text{ROPE}} \left( \frac{d}{L} \right) g$$

Finally on B:



$$\sum F_{B,y} = M_B a_{B,y} \quad a_{B,y} = 0$$

$$\Rightarrow T_3 - W_B = 0$$

$$\Rightarrow \mu_s M_A g - M_{\text{ROPE}} \left( \frac{d}{L} \right) g - M_B g = 0$$

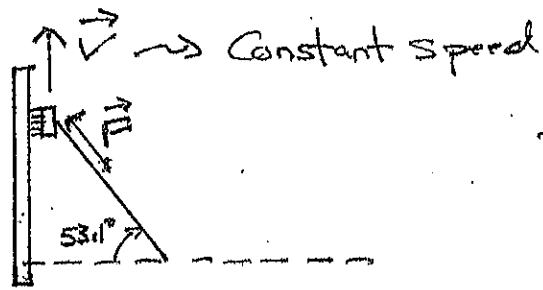
$$\Rightarrow (\mu_s M_A - M_B)g = \frac{M_{\text{ROPE}}}{L} dg$$

$$\Rightarrow d = \frac{(\mu_s M_A - M_B)L}{M_{\text{ROPE}}}$$

My NUMBERS WERE  $\mu_s = .255$ ,  $M_A = 2.07\text{Kg}$   
 $M_B = .35\text{Kg}$ ,  $M_{\text{ROPE}} = .243\text{Kg}$ ,  $L = 1.02\text{m}$

$$d = \frac{(.255 \cdot 2.07 - .35\text{kg})(1.02\text{m})}{.243} = \left(\frac{.17785}{.243}\right)(1.02\text{m})$$
$$= .747\text{m}$$

5.74

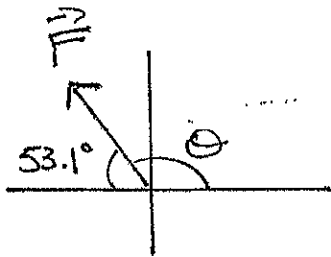


BRUSH WEIGHS 15N

$\mu_k = .15$

- a) FIND MAGNITUDE OF  $F$ , b) FIND NORMAL FORCE,  $n$

FORCES ON BRUSH  $\vec{W}$  DOWN,  $W = 15N$ , KINETIC FRICTION  
 $\vec{f}_k$  DOWNWARD (OPPOSITE TO  $\vec{v}$ ), NORMAL FORCE,  $\vec{n}$ .  
 VERTICAL WALL  $\Rightarrow \vec{n}$  TO RIGHT, APPLIED FORCE  $\vec{F}$ .  
 $\vec{F}$  PARALLEL TO HANDLE  $\Rightarrow$



SO STANDARD  $\theta = 180^\circ - 53.1^\circ = 126.9^\circ$

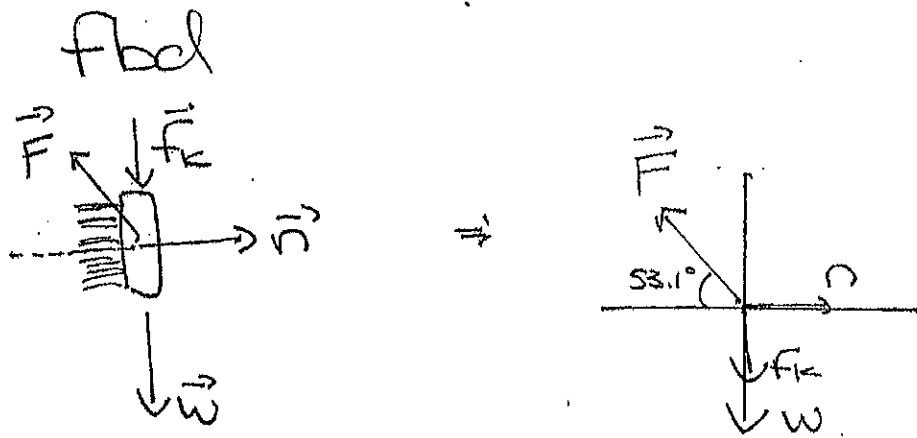
$$\Rightarrow F_x = F \cos 126.9^\circ = -.6F$$

$$F_y = F \sin 126.9^\circ = .8F$$

EQUIVALENTLY, USE  $53.1^\circ$  AND  $\vec{F}$  IN 2<sup>ND</sup> QUADRANT

$$\Rightarrow F_x < 0 \therefore F_x = -F \cos 53.1^\circ = -.6F$$

$$F_y > 0 \therefore F_y = +F \sin 53.1^\circ = .8F$$



$$\sum F_x = Ma_x. \quad \text{No motion in } x \Rightarrow a_x = 0$$

$$\Rightarrow n + F_x = 0 \Rightarrow n - .6F = 0 \quad (1)$$

$$\sum F_y = Ma_y. \quad \text{Constant speed} \Rightarrow a_y = 0$$

$$\Rightarrow F_y - f_k - W = 0 \Rightarrow .8F - f_k - 15N = 0$$

$$\text{Kinetic friction} \Rightarrow f_k = \mu_k n = .15n \therefore .8F - .15n - 15N = 0$$

$$\Rightarrow .8F - .15n = 15N$$

$$(1) \Rightarrow n = .6F \Rightarrow .8F - .15(.6F) = 15N$$

$$\Rightarrow .8F - .09F = 15N \Rightarrow .71F = 15N \Rightarrow \boxed{F = \frac{15N}{.71} = 21.1N}$$

$$\boxed{n = .6F = .6(21.1N) = 12.7N}$$