

April 20, Week 13

Today: Chapter 10, Angular Momentum

Homework #10 - Due April 23 at 11:59pm

Mastering Physics: 7 questions from chapter 10.

Written Question: 10.86

Exam #5, Friday, April 27

On Chapters 9 and 10

Review Session: Thursday, April 26, 7:30PM, Room 114 of Regener Hall.

Review

Angular Momentum:

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Angular Momentum:

Point Particle:

Review

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Point Particle: $\vec{\mathbf{L}} = \vec{\mathbf{r}} \times \vec{\mathbf{p}}$

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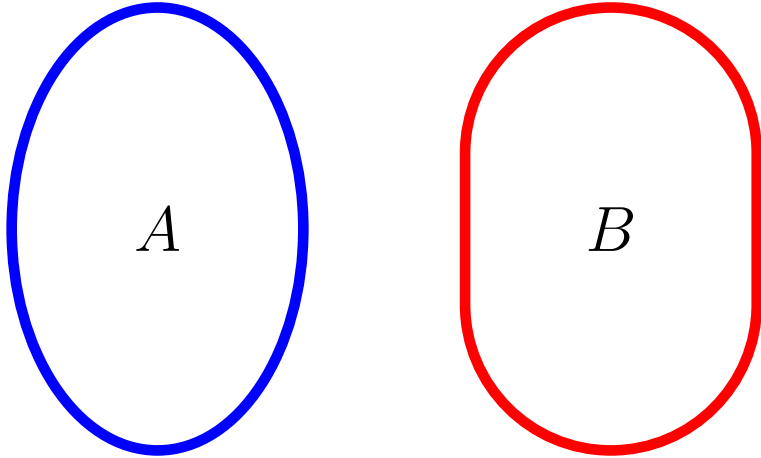
For either: $\vec{\boldsymbol{\tau}} = \frac{d\vec{\mathbf{L}}}{dt}$

Conservation of Angular Momentum

In the absence of external torques, the total angular momentum of a system cannot change.

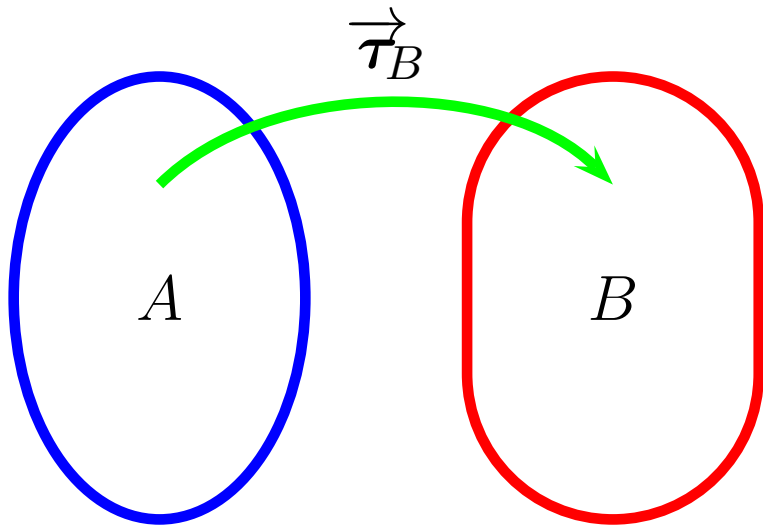
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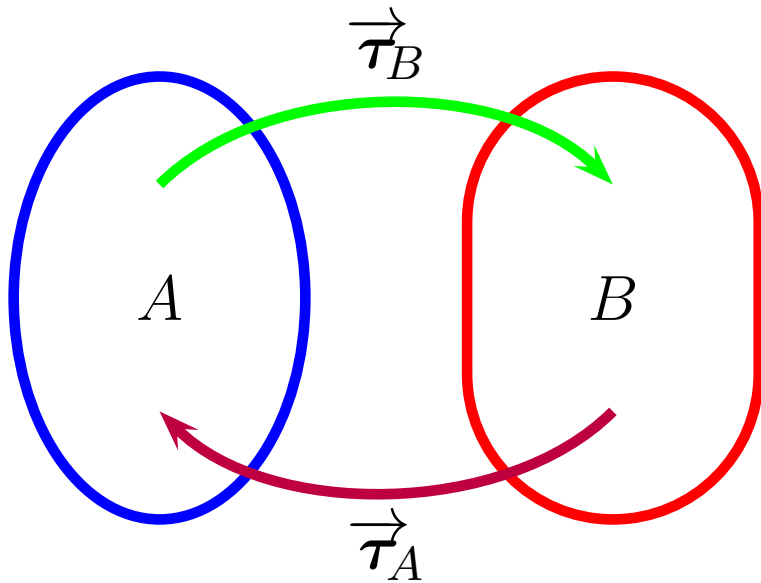
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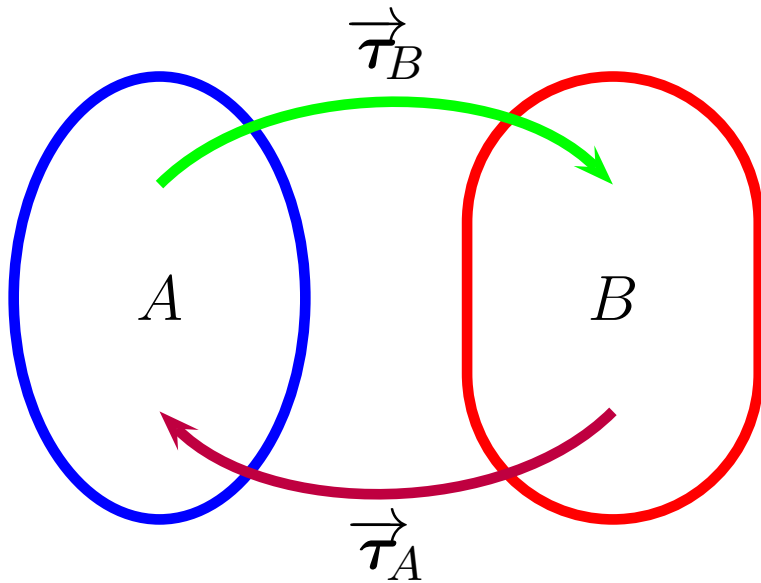


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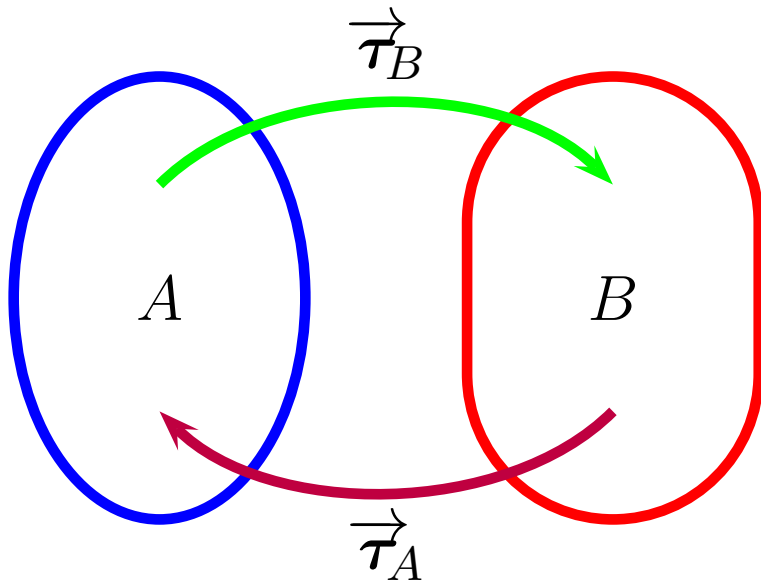
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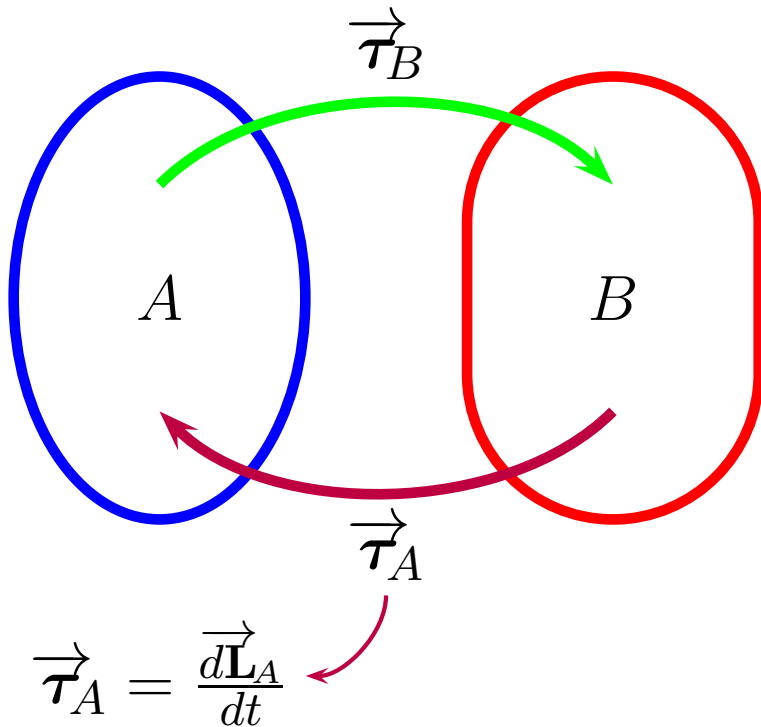
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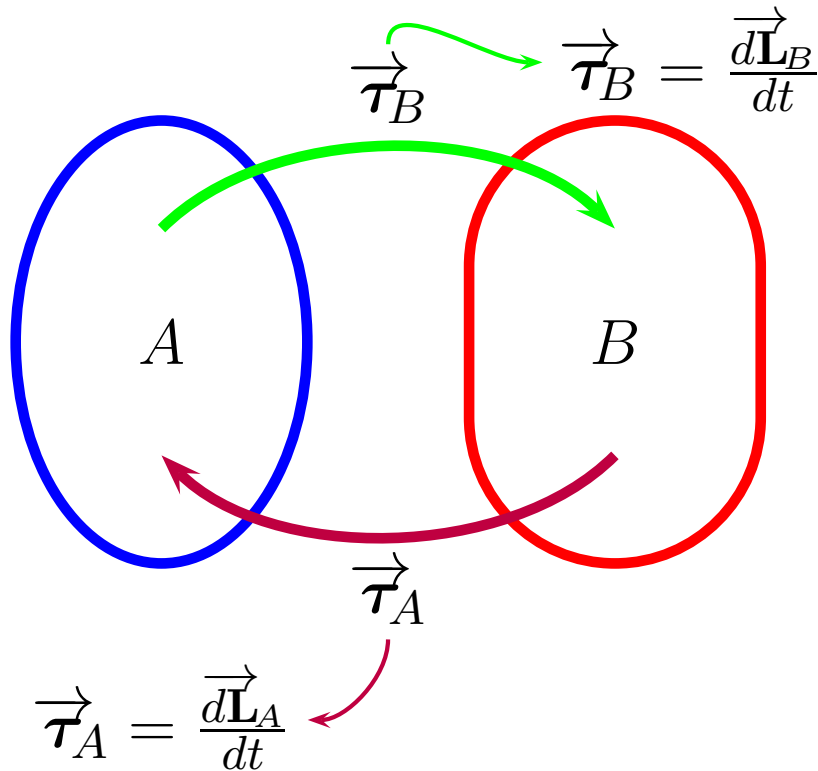
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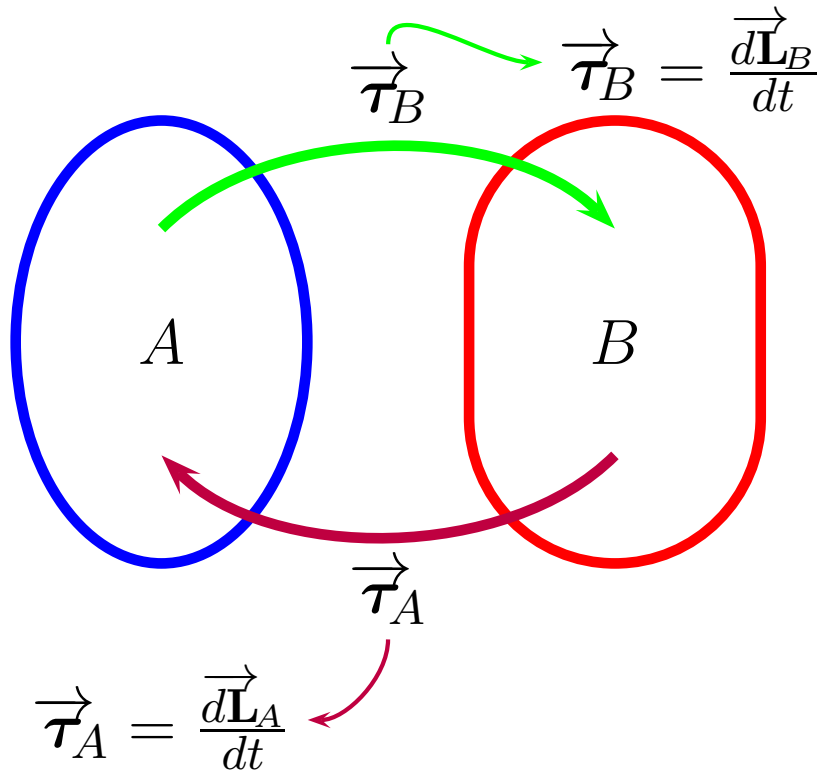
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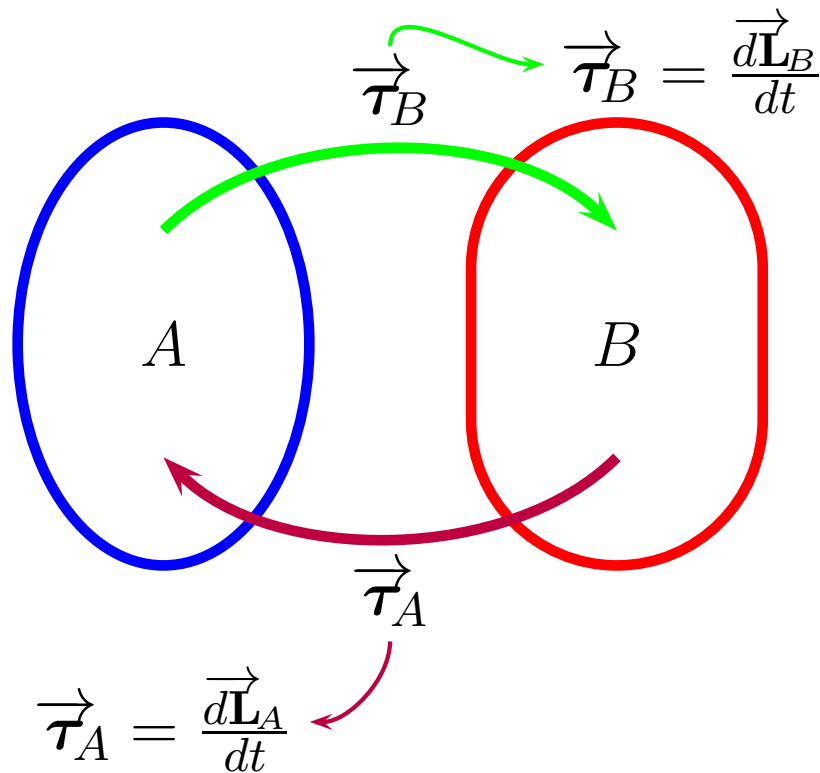
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$$\vec{L}_A + \vec{L}_B = \text{constant}$$

Example II

Conservation of Angular Momentum:

$$\vec{\mathbf{L}}_{A1} + \vec{\mathbf{L}}_{B1} = \vec{\mathbf{L}}_{A2} + \vec{\mathbf{L}}_{B2}$$

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Example: A 60-kg man runs at 3.4 m/s alongside a 155-kg , 2.6-m radius merry-go-round that is rotating at 4 rad/s . If the both the man and the merry-go-round are circling counter-clockwise (as viewed from above), how fast will the merry-go-round be going after the man jumps onto its edge?

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Clicker Quiz

An olympic diver launches himself from the 20-m platform with angular speed 2 rad/s . By tucking himself into a ball, he increases his angular speed to 6 rad/s . By what factor did the diver change his moment of inertia by tucking himself into a ball?

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The magnitude of this force is given by:

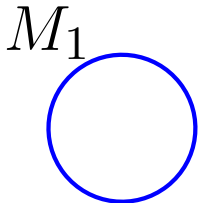
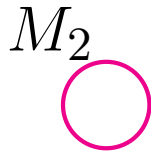
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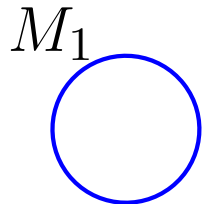
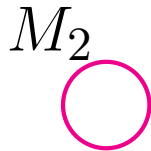
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$$F_g = \frac{M_1 M_2}{r^2}$$

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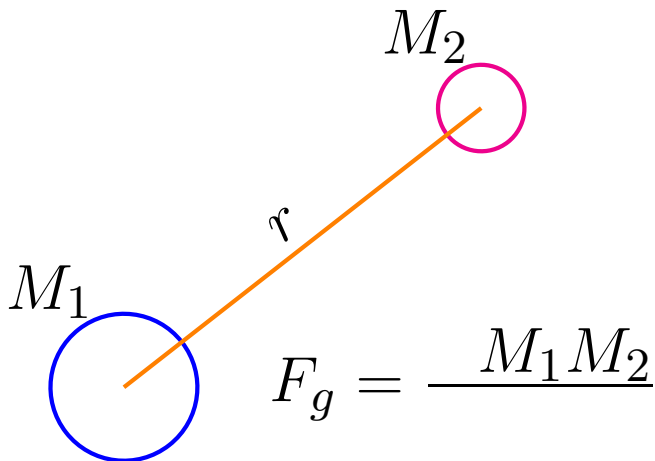
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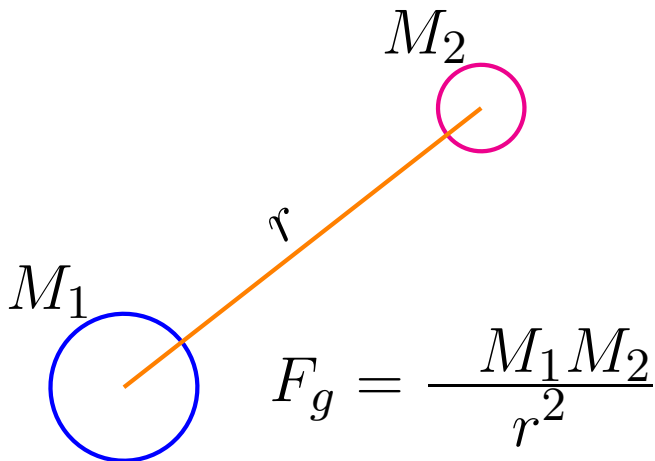
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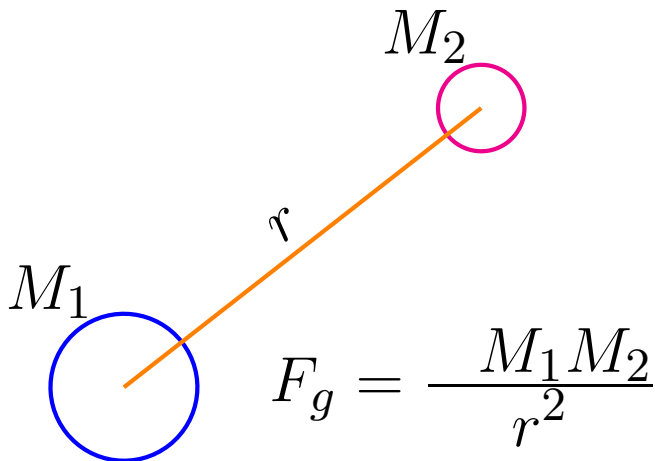
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Inverse square law

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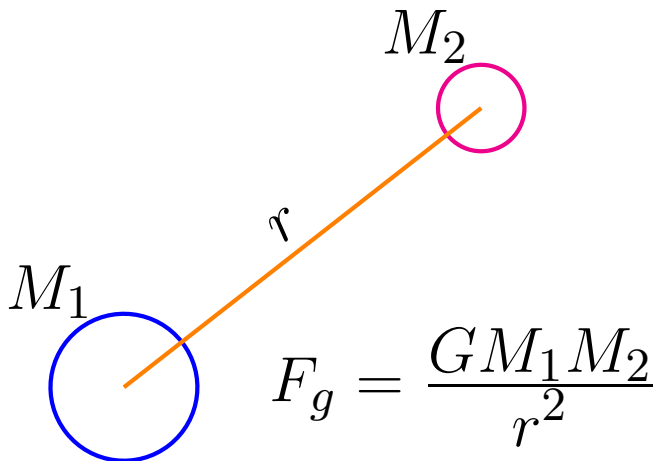
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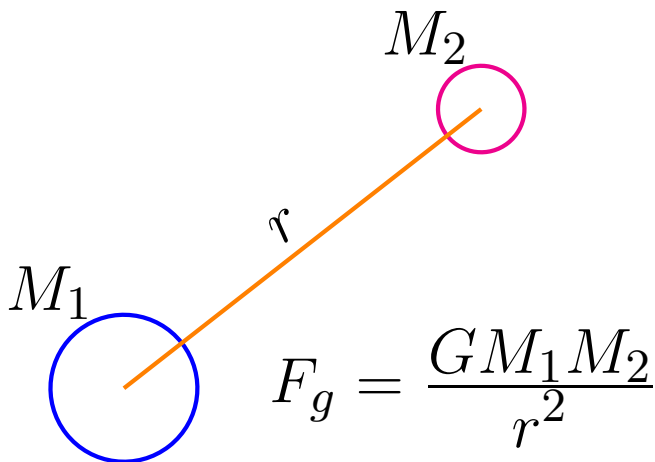
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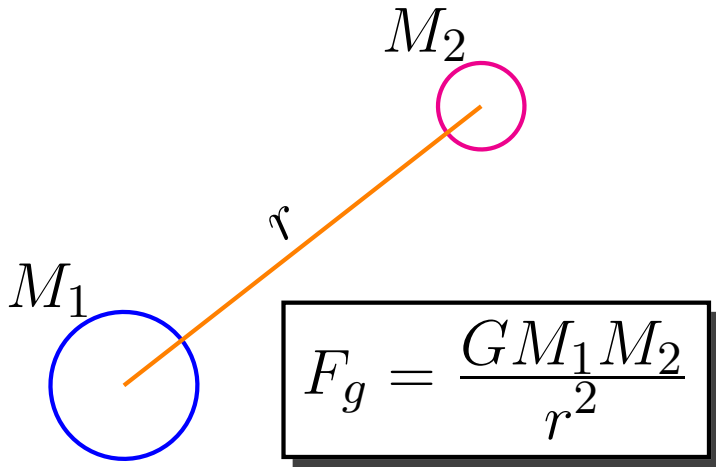
Universal Gravitational Constant:

$$G = 6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2 / \text{kg}^2$$



Inverse square law

Example



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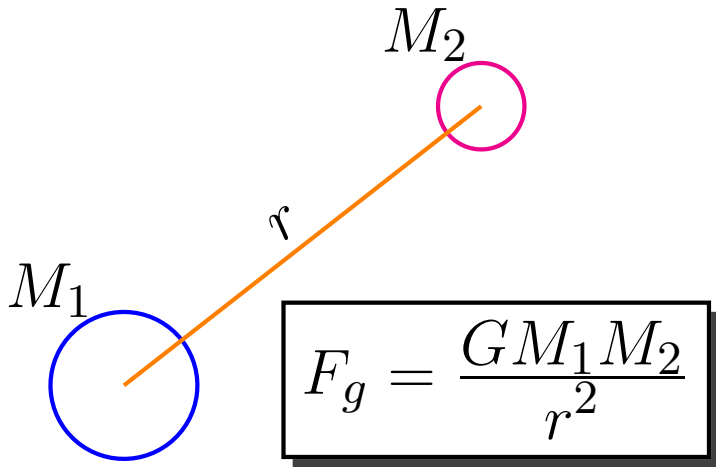
M_2 - Mass of second object

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Example: Find the gravitational force that the earth exerts on the moon.