

# March 23, Week 9

Today: Chapter 7, Elastic Energy

Homework #7:

Mastering Physics: 6 problems from chapter 7

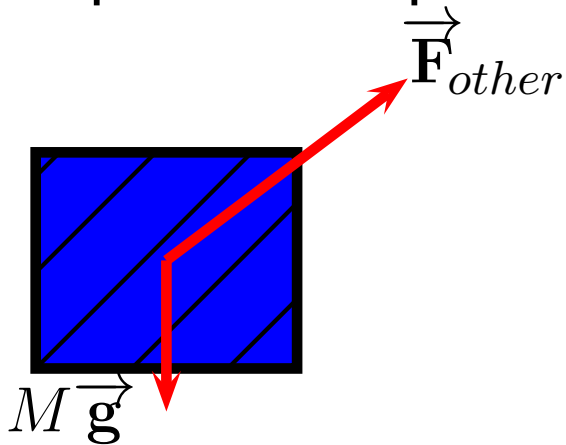
Written Question: 7.60

Due Monday, March 26 at 11:59pm

Makeup Questions now in mailboxes. The score on them is your percentage increase.

# Review

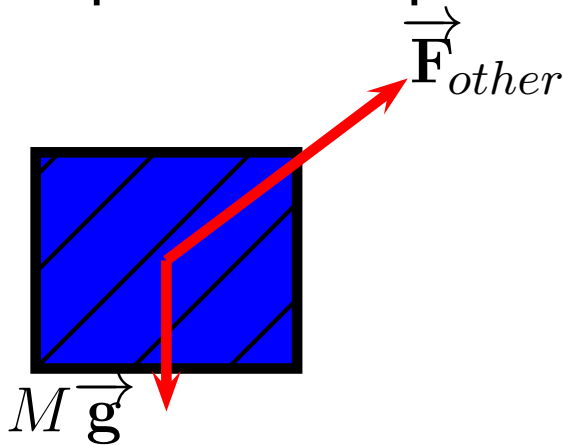
When other forces do work on an object (e.g. friction), while energy may not be conserved, we can still use the energy equations to predict characteristics of the motion.



$$\frac{1}{2}Mv_1^2 + Mgy_1 + W_{other} = \frac{1}{2}Mv_2^2 + Mgy_2$$

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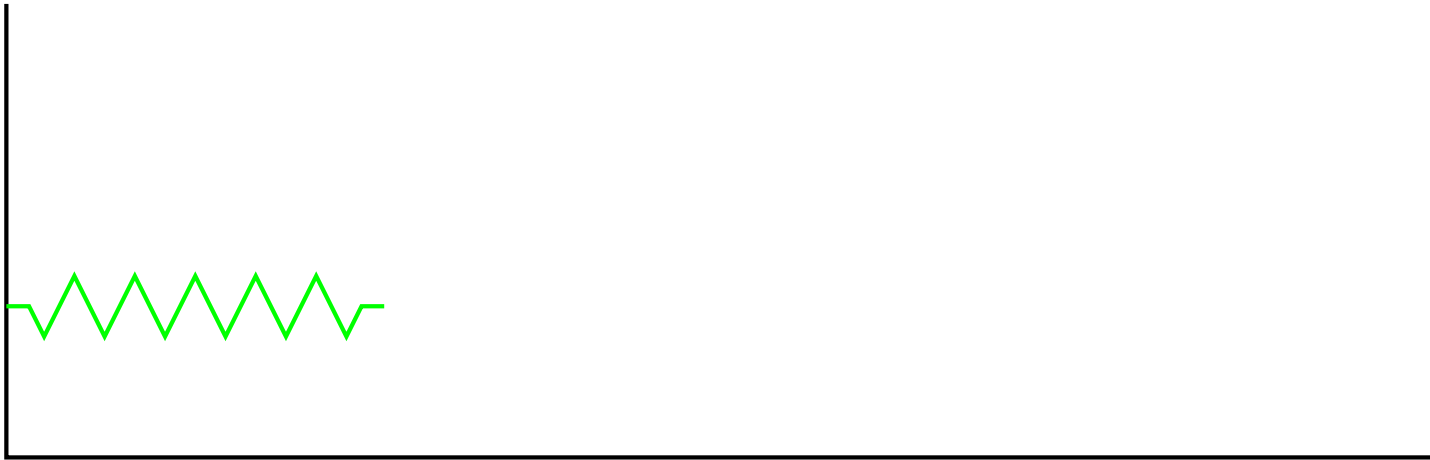
Example: A mass slides down a  $23^\circ$ ,  $2\text{-m}$  long incline. If it starts with speed  $5\text{ m/s}$  and  $\mu_k = 0.6$ , what is its speed at the bottom?

# Elastic Potential Energy

Elastic Potential energy - Potential energy due to a spring.

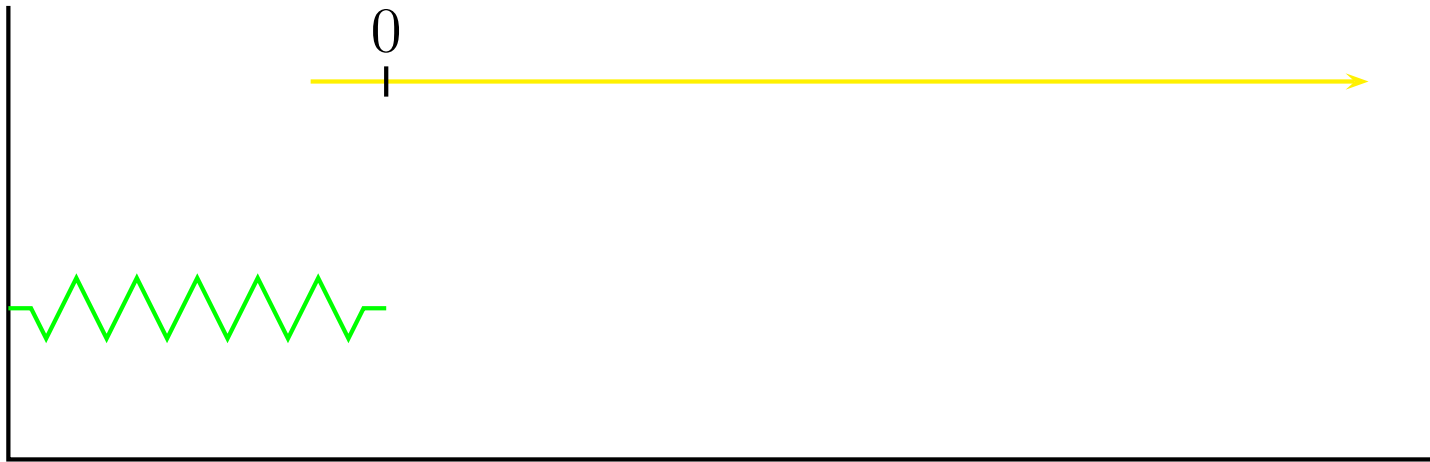
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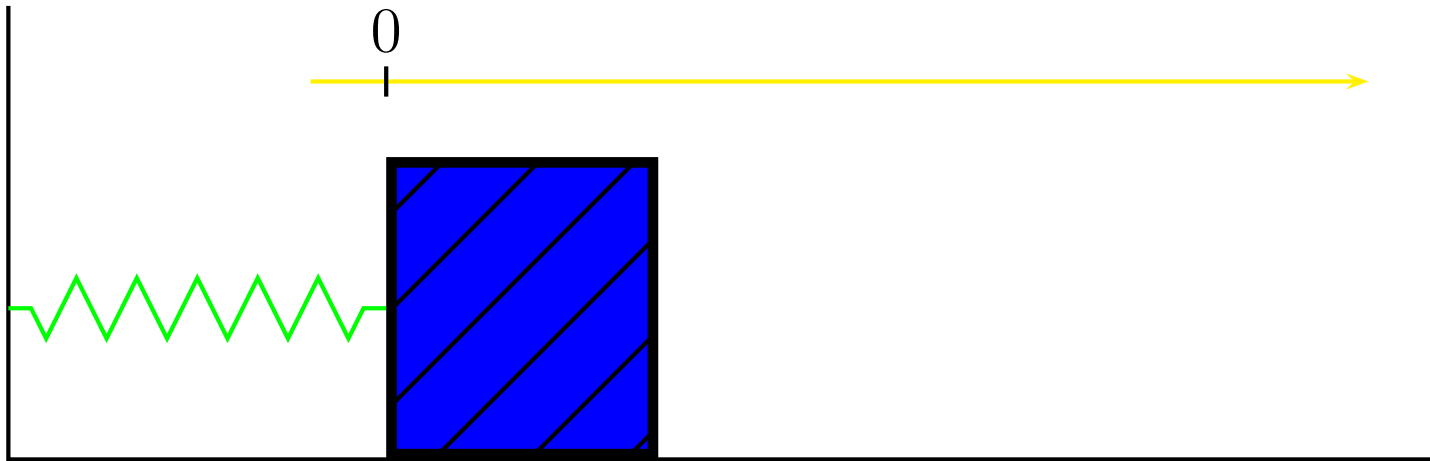
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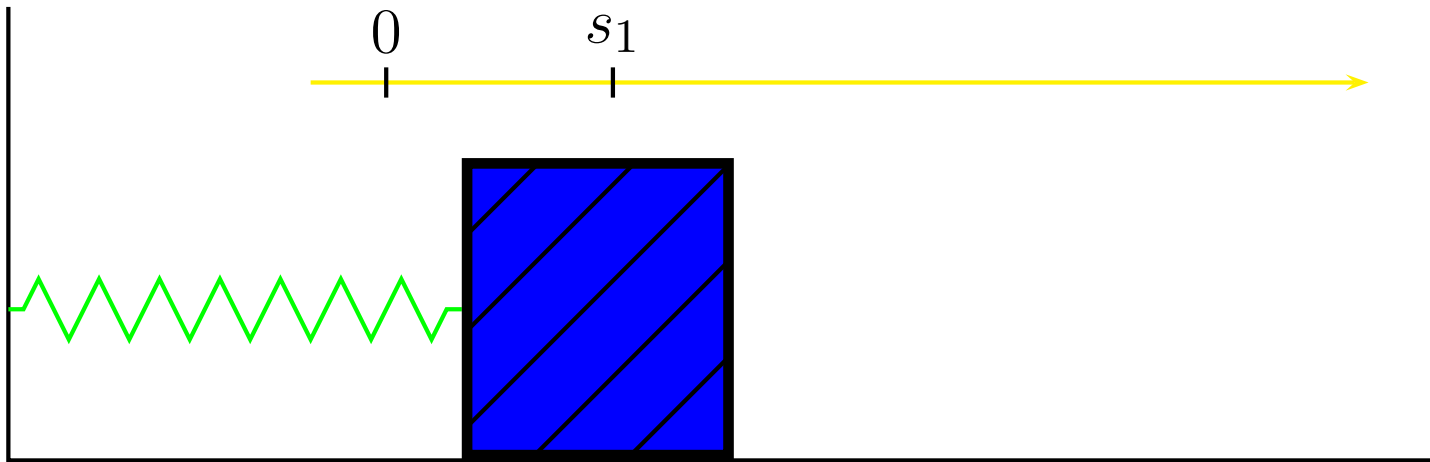
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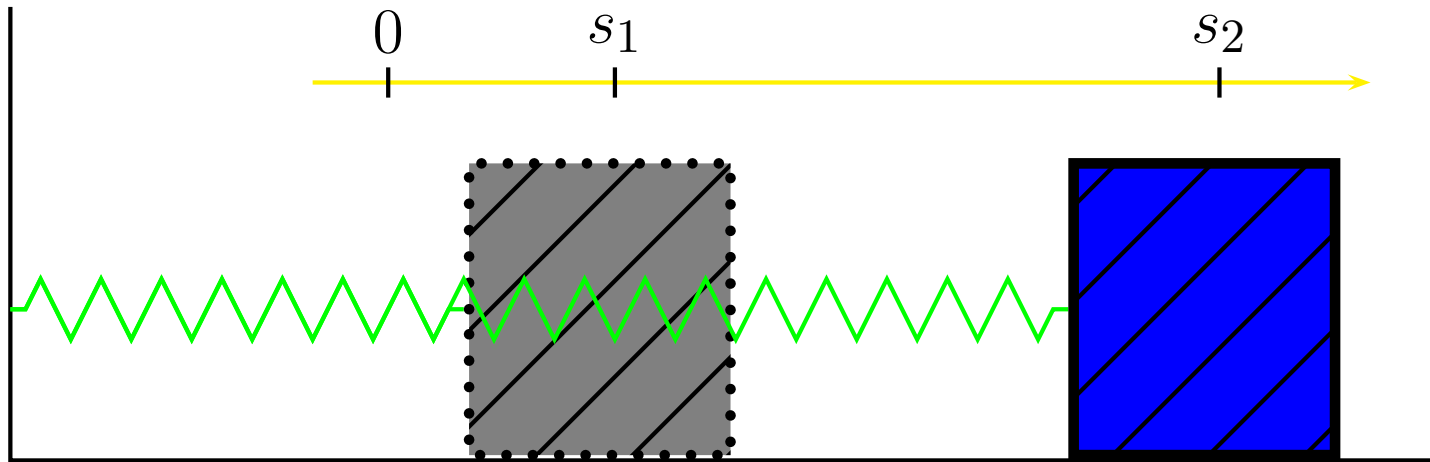
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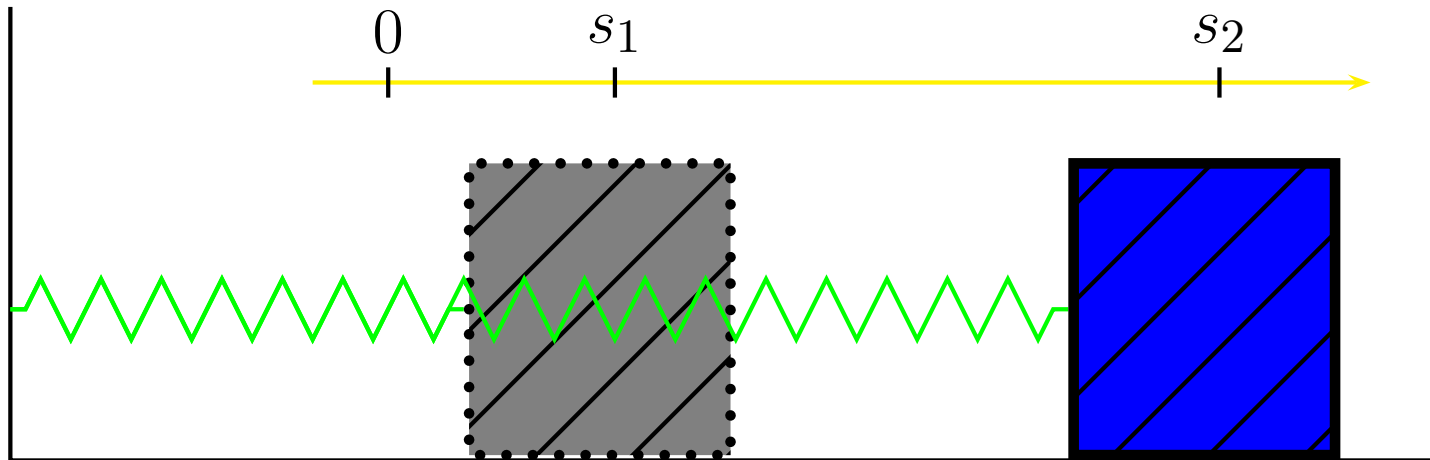
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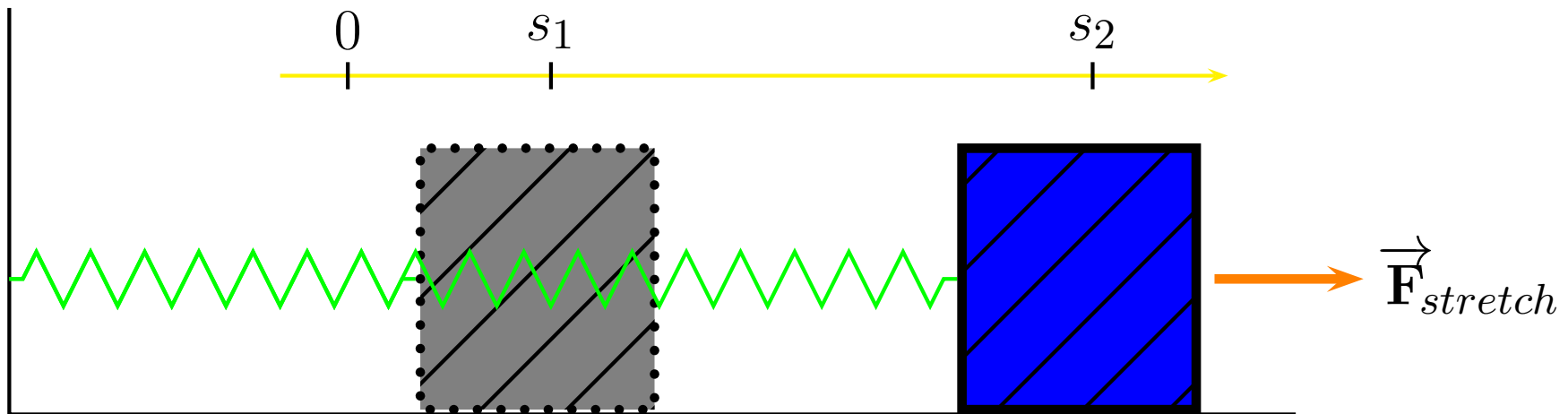
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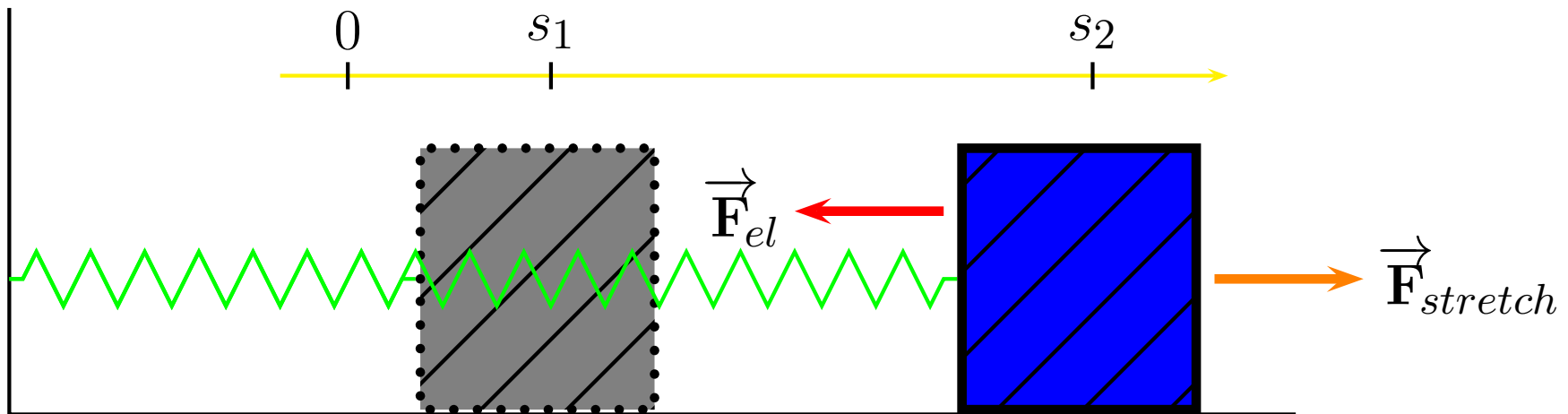
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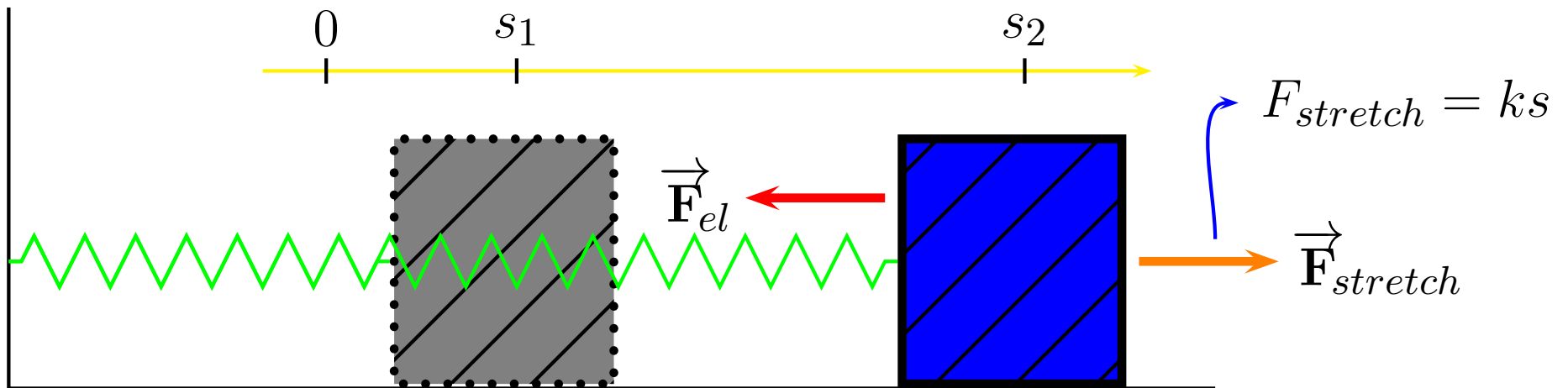
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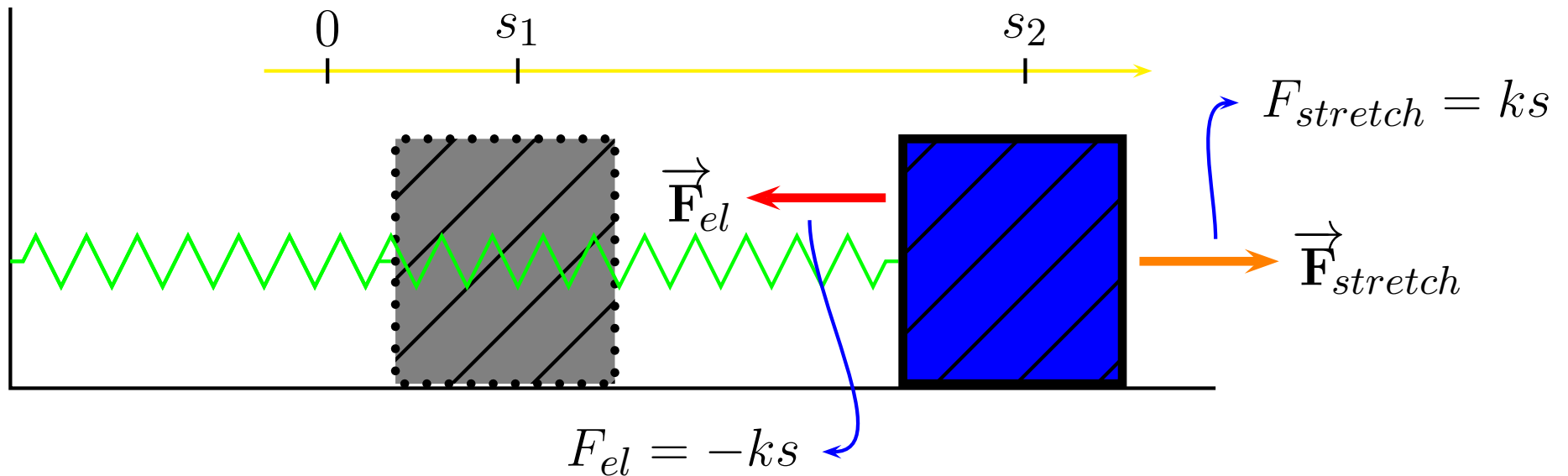
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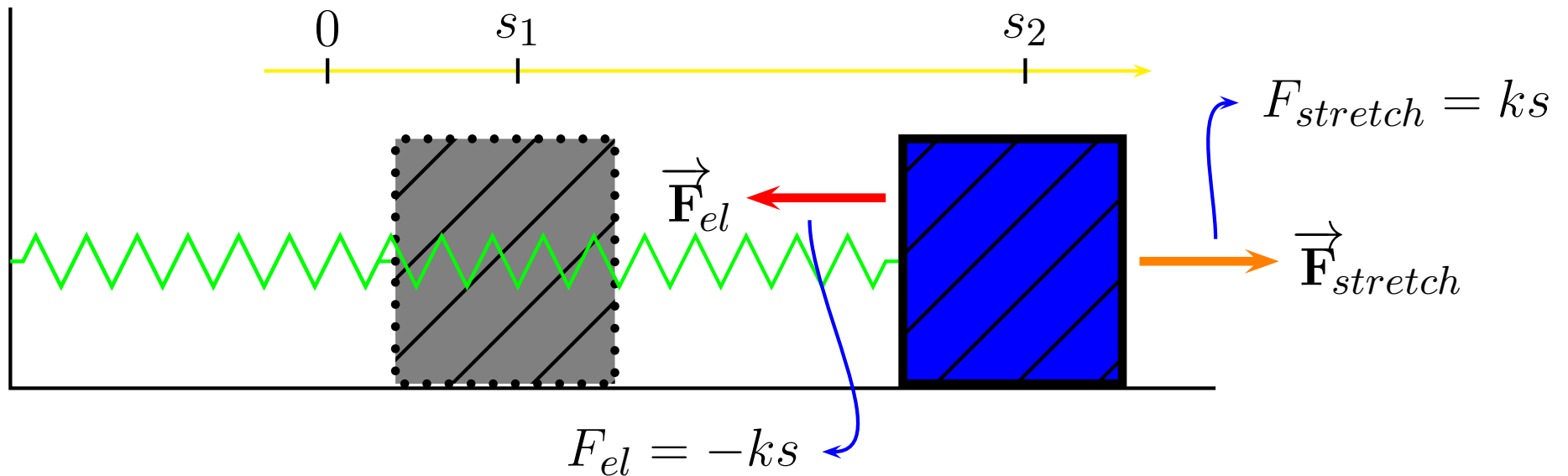
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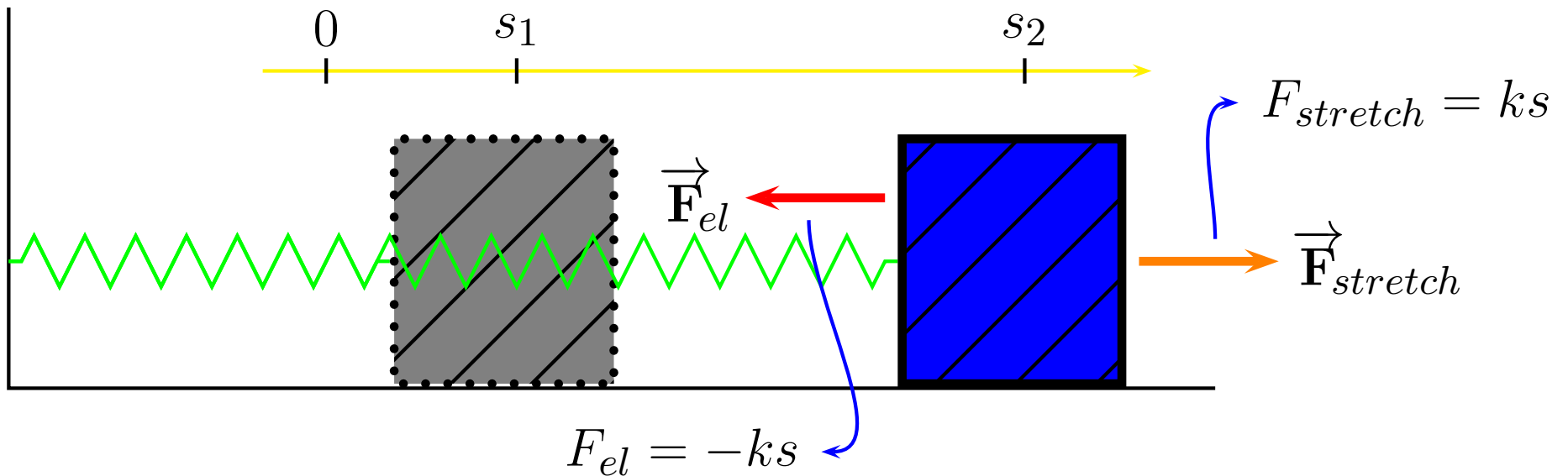


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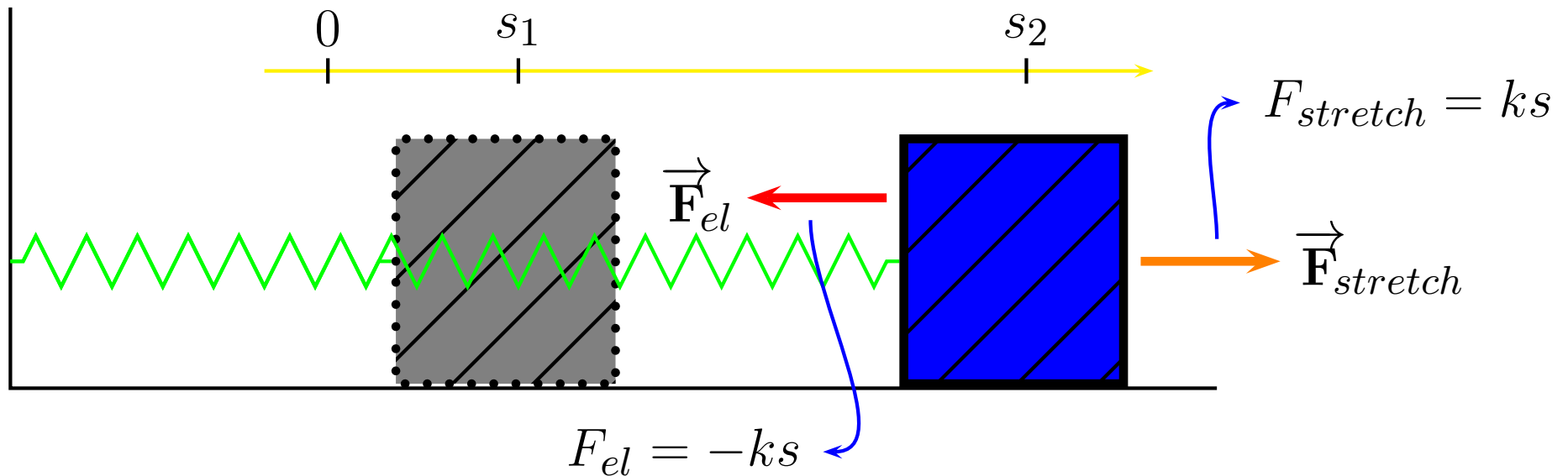
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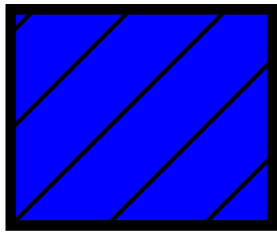
Example: A 2-kg block is attached to a  $k = 200 \text{ N/m}$  spring. If the block is given an initial 5-m/s speed from the spring's unstretched position, without friction how far does it go before stopping?

# Other Forces

When other forces do work on an object (*e.g.* friction), while energy may not be conserved, we can still use the energy equations to predict characteristics of the motion.

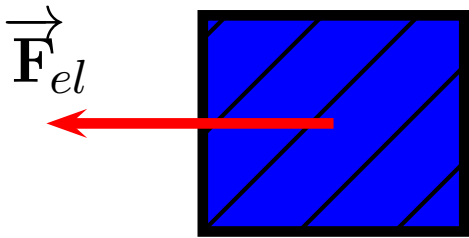
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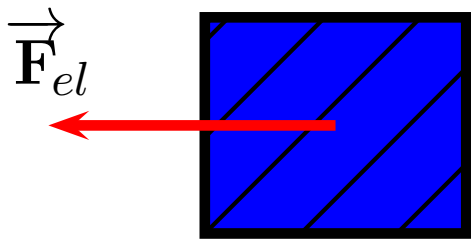
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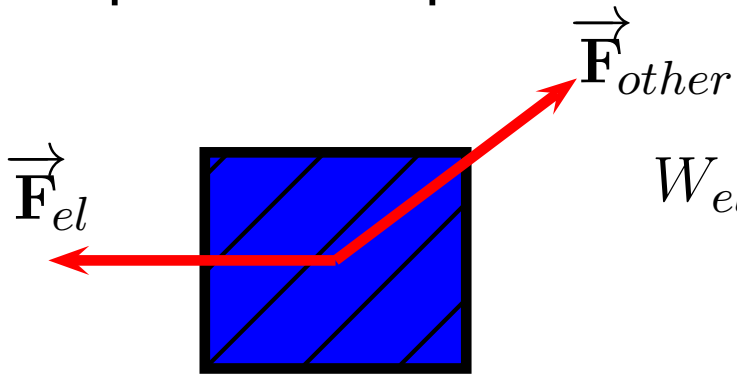
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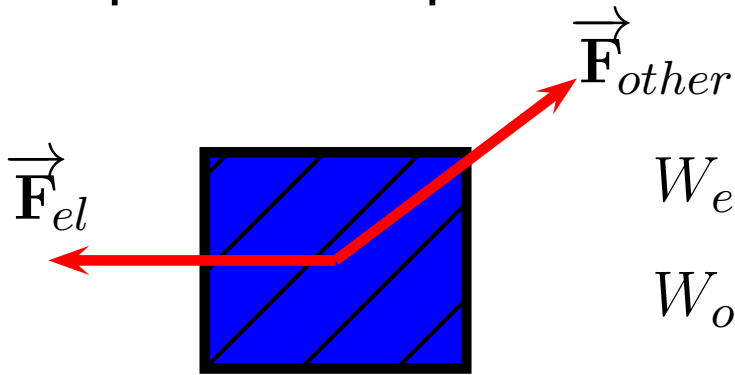
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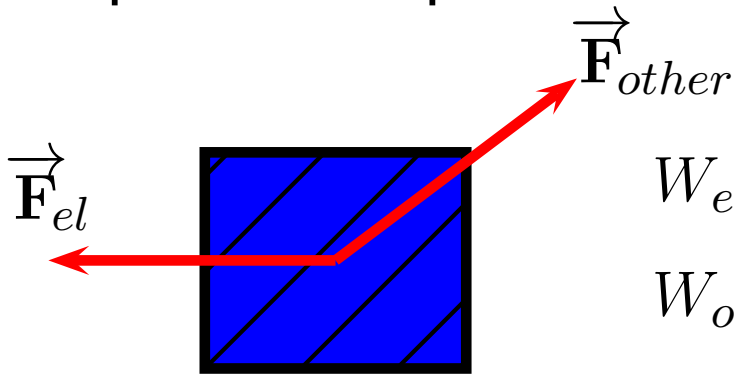


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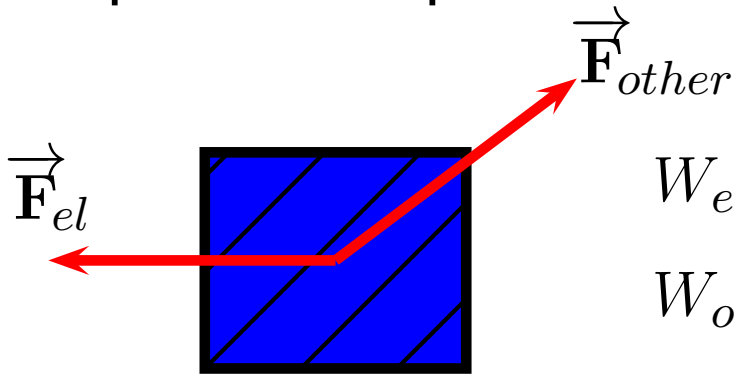
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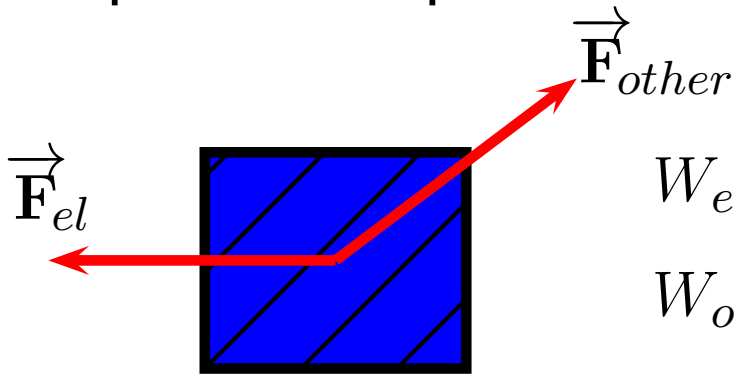
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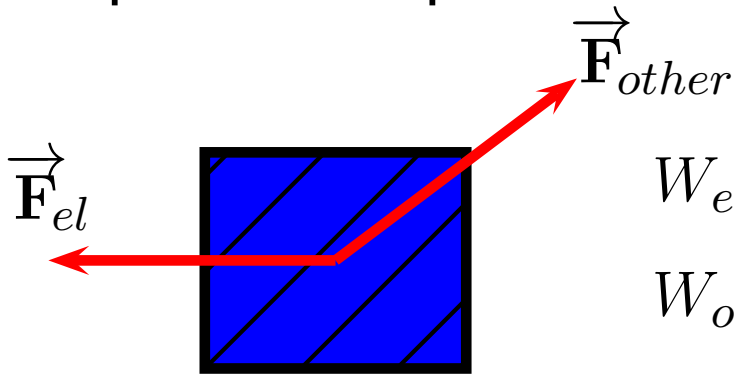
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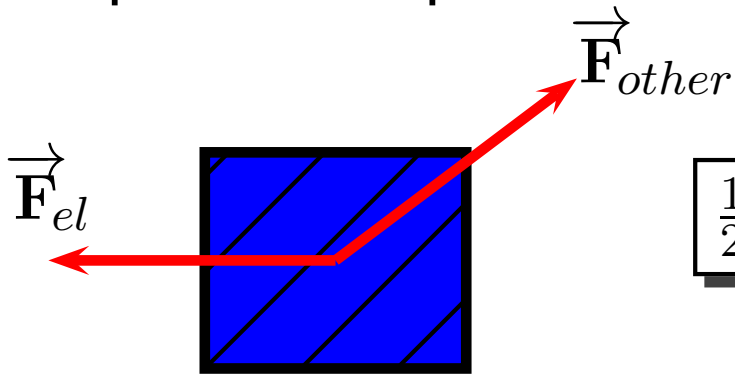
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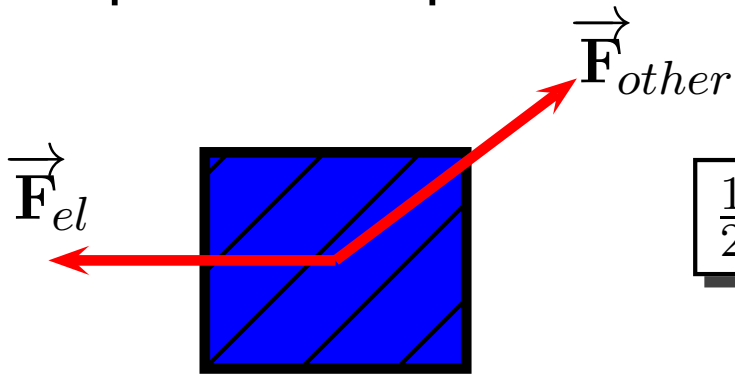


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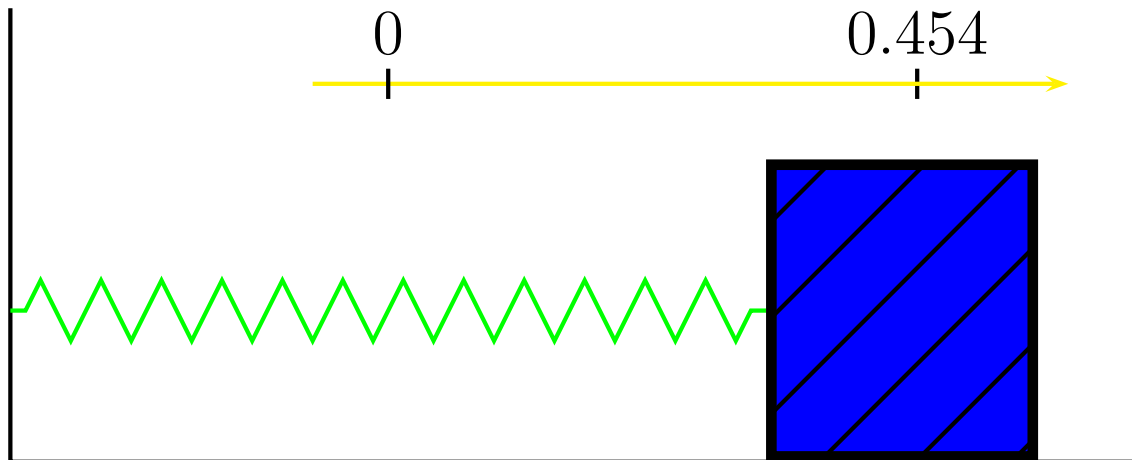


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Example: A 2-kg block is attached to a  $k = 200 \text{ N/m}$  spring. If the block is given an initial 5-m/s speed from the spring's unstretched position and  $\mu_k = 0.5$ , how far does it go before stopping?

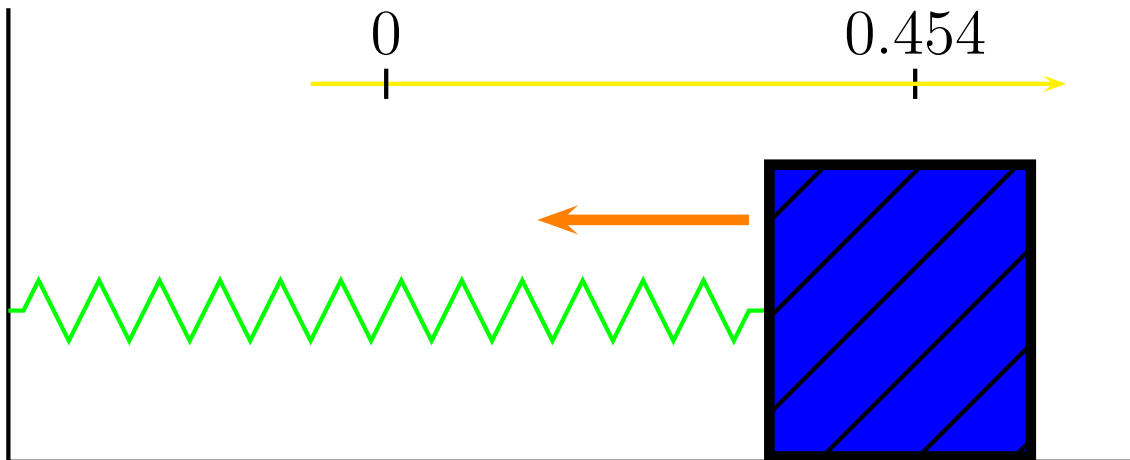
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If the  $2\text{-kg}$  block attached to a  $k = 200\text{ N/m}$  spring with  $\mu_k = 0.5$  slides back from its  $s_2 = 0.454\text{ m}$  position, which of the following choices is a possible stretching distance for the spring,  $s_3$ , when it stops again?



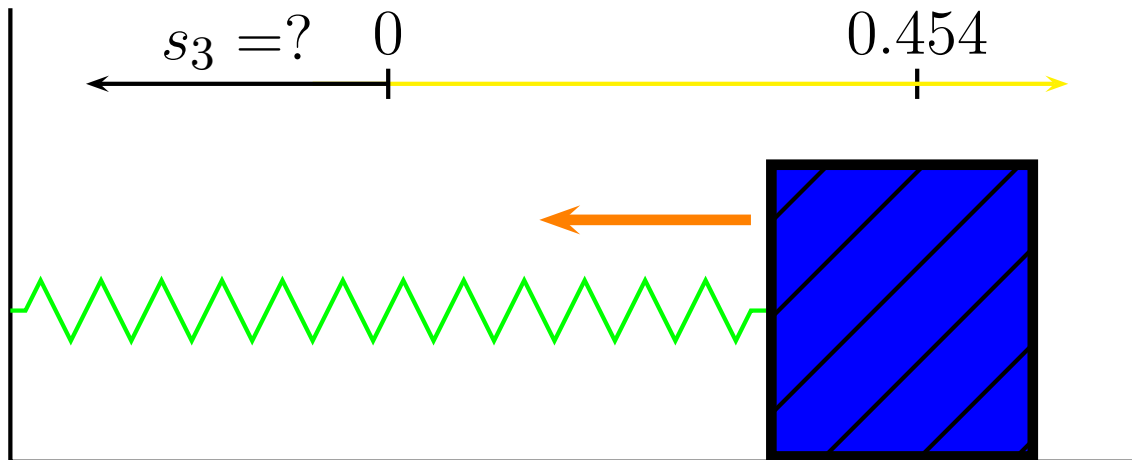
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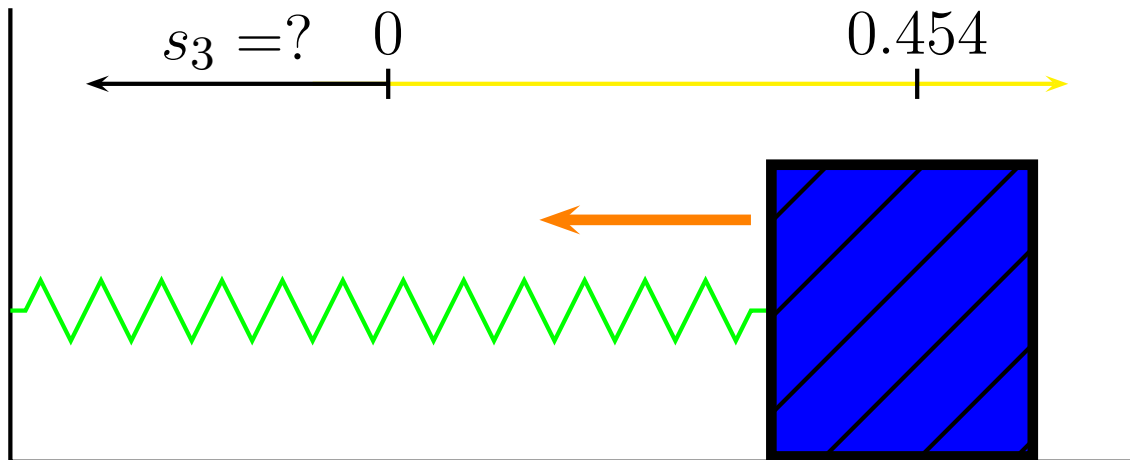
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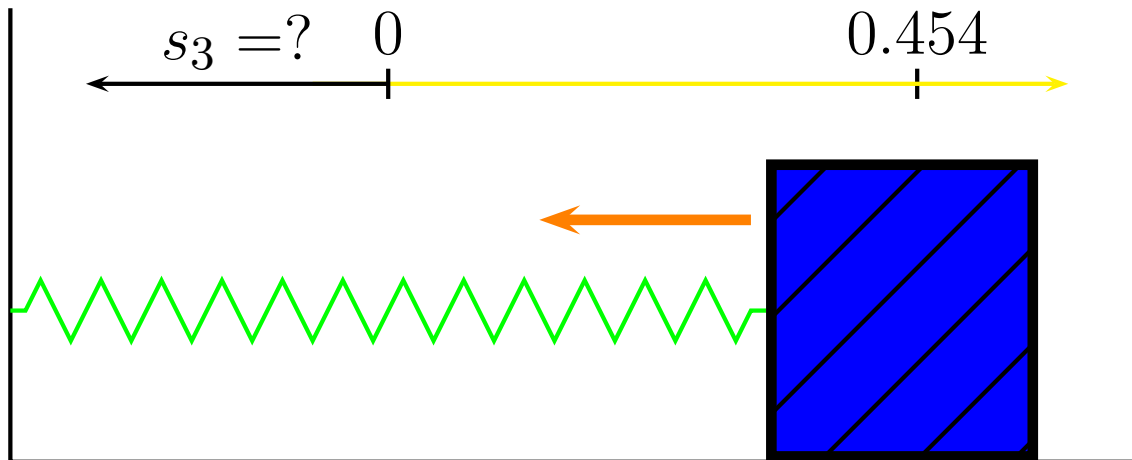


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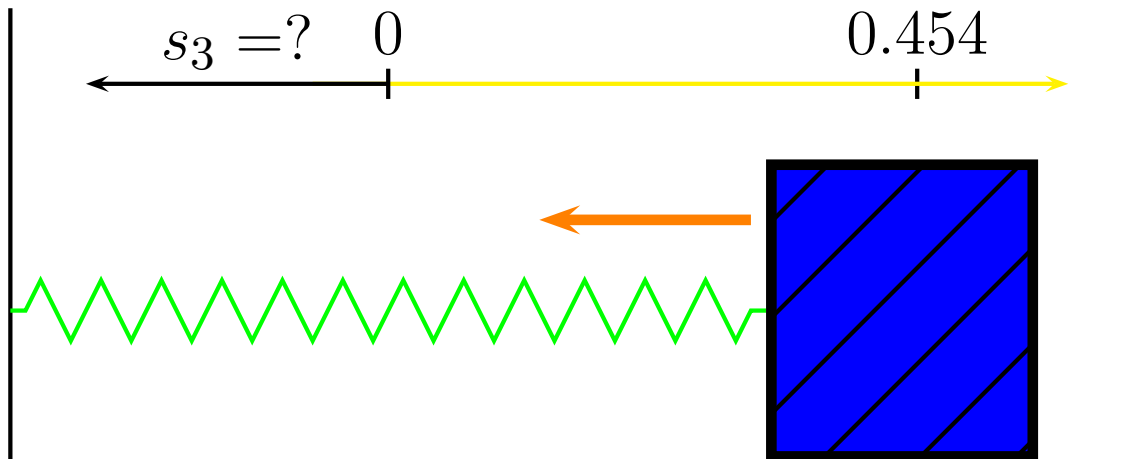
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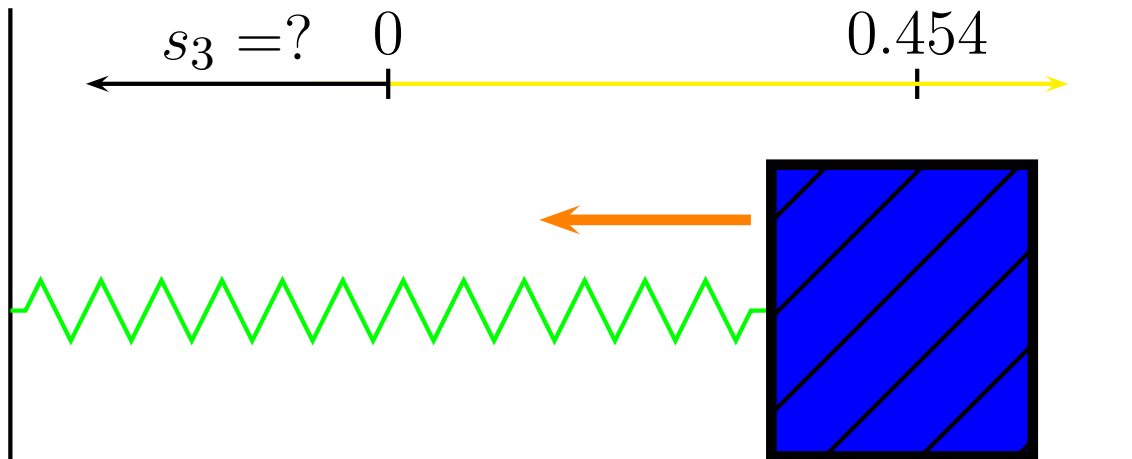
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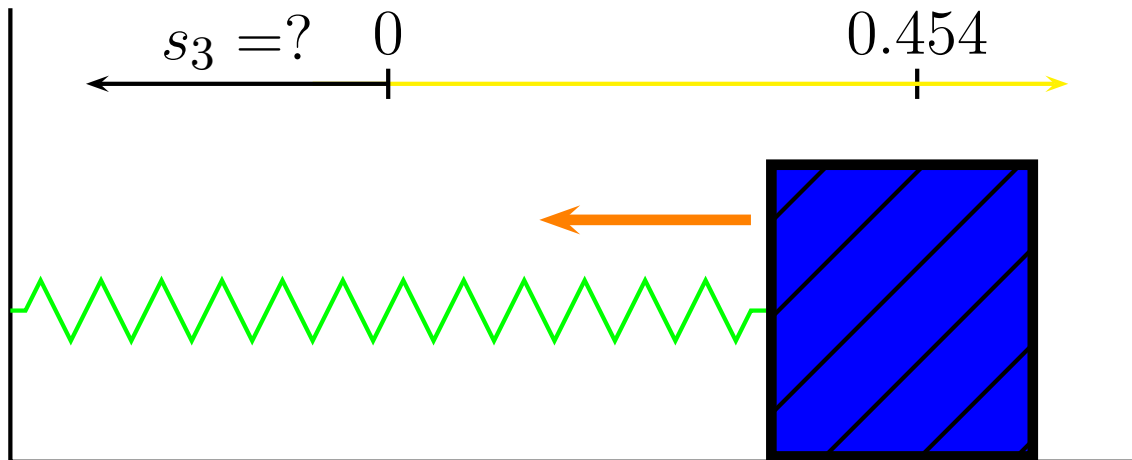


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The most general problems (this term) involve gravity, springs, and other forces all doing work.

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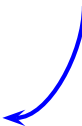
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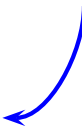

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A diagram illustrating energy conservation. The equation  $W_{total} = W_g + W_{el} + W_{other}$  is shown at the top. Below it, three terms are listed:  $\Delta K$ ,  $-\Delta U_g$ , and  $-\Delta U_{el}$ . A blue arrow points from  $W_{total}$  to  $\Delta K$ . A red arrow points from  $W_g$  to  $-\Delta U_g$ . A green arrow points from  $W_{el}$  to  $-\Delta U_{el}$ .

$$\frac{1}{2}Mv_1^2 + Mgy_1 + \frac{1}{2}ks_1^2 + W_{other} = \frac{1}{2}Mv_2^2 + Mgy_2 + \frac{1}{2}ks_2^2$$