

Physics (S), HW # 2

7 Mastering Physics from chapters 1 & 2

Written: 1.39, 1.44

52 SHANNON's SPEED = 70 mph = 70 mi/h.

MILE MARKERS 1.00 mile Apart in 54s.

Is SPEEDOMETER ACCURATE?


$$V = \frac{\Delta X}{\Delta t}$$

CALCULATE ACTUAL V USING  $\Delta X = 1.00\text{mi}$

$$\Delta t = 54\text{s} \times \frac{1\text{h}}{3600\text{s}} = 0.015\text{h}$$

$$V_{\text{ACTUAL}} = \frac{1.00\text{mi}}{0.015\text{h}} = 66.7\text{mph} \leftarrow \text{SPEEDOMETER READING}$$

too high

56.



E. coli

2  $\mu\text{m}$  long cylinder

1  $\mu\text{m}$  diameter

$1 \times 10^{-12}$  g MASS

DNA 700  $\times$  longer THAN LENGTH

20  $\mu\text{m/s}$  SPEED

FIND IN S.I. USING PROPER SIG-FIG

a) LENGTH:  $1 \mu\text{m} = 1 \times 10^{-6} \text{ m} \Rightarrow 2 \mu\text{m} \times \frac{1 \times 10^{-6} \text{ m}}{1 \mu\text{m}} = \underline{\underline{2 \times 10^{-6} \text{ m}}}$

b) DIAMETER:  $1 \mu\text{m} = \underline{\underline{1 \times 10^{-6} \text{ m}}}$

c) MASS:  $1 \text{ Kg} = 1000 \text{ g} \Rightarrow 1 \times 10^{-12} \text{ g} \times \frac{1 \text{ Kg}}{1000 \text{ g}} = \underline{\underline{1 \times 10^{-15} \text{ Kg}}}$

d) DNA LENGTH IN millIMETERS:

LENGTH:  $\ell = 700 \times 2 \mu\text{m} = 1400 \mu\text{m} \times \frac{1 \times 10^{-6} \text{ m}}{1 \mu\text{m}} = .0014 \text{ m}$

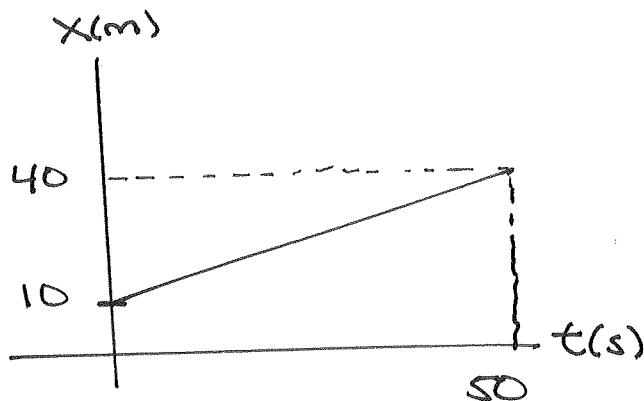
1 mm = .001 m  $\Rightarrow .0014 \text{ m} \times \frac{1 \text{ mm}}{.001 \text{ m}} = 1.4 \text{ mm} = 1 \text{ mm}$  to 1 sig fig

e) How many Meters in A DAY:  $V = \frac{\Delta X}{\Delta t} \cdot V = \frac{20 \mu\text{m}}{5} \times \frac{1 \times 10^{-6} \text{ m}}{\mu\text{m}} = 2 \times 10^{-5} \text{ m/s}$

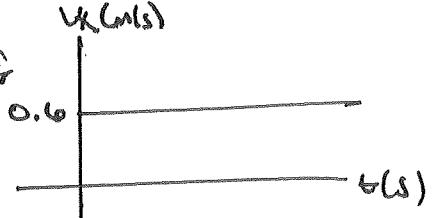
$$\Delta t = 1 \text{ day} \times \frac{24 \text{ h}}{\text{day}} \times \frac{3600 \text{ s}}{\text{h}} = 86400 \text{ s} \Rightarrow 2 \times 10^{-5} \text{ m/s} = \frac{\Delta X}{86400 \text{ s}} \Rightarrow \Delta X = (2 \times 10^{-5} \text{ m/s})(86400 \text{ s}) = 1.728 \text{ m} = \underline{\underline{2 \text{ m}}}$$

1 sig fig

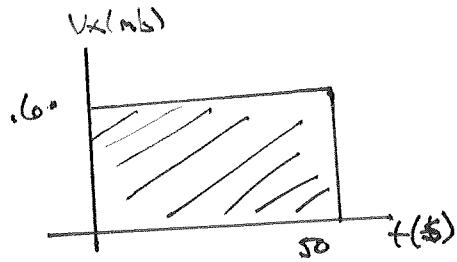
## WHAT $x$ vs. $t$ Graphs Can Tell you:



- a) WHAT IS TOTAL distance?  $\Delta x = x_f - x_i$ . JUST READ OFF VALUES  
 at  $t_f = 50\text{s}$ ,  $x_f = 40\text{m}$ , at  $t_i = 0$ ,  $x_i = 10\text{m}$   
 $\Rightarrow \Delta x = 40\text{m} - 10\text{m} = 30\text{m}$
- b) WHAT IS  $V_{AV}$  FOR  $\Delta t = 50\text{s}$ ?  $V_{AV} = \frac{\Delta x}{\Delta t}$ . ALREADY have  $\Delta x = 30\text{m}$   
 $\Rightarrow V_{AV} = \frac{30\text{m}}{50\text{s}} = 0.6\text{m/s}$
- c) WHAT IS  $V_x$  AT  $t = 10\text{s}$ .  $x$  vs.  $t$  is straight line  $\Rightarrow$  UNIFORM MOTION  
 $\Rightarrow$  Constant Velocity. So  $V_{AV} = V_x$  AT ALL TIMES  $\Rightarrow V_x = 0.6\text{m/s}$  TOO
- d) CORRECT  $V_x$  GRAPH?  $\rightarrow$  AGAIN, UNIFORM MOTION  $\Rightarrow$  Constant  $V_x$   
 $\Rightarrow$  HORIZONTAL  $V_x$  VS.  $t$  GRAPH.  $V_x = 0.6\text{m/s} \Rightarrow$



Part E.  $\rightarrow$  e)



$$\text{Area} = .60 \text{ m/s} (50 \text{ s})$$

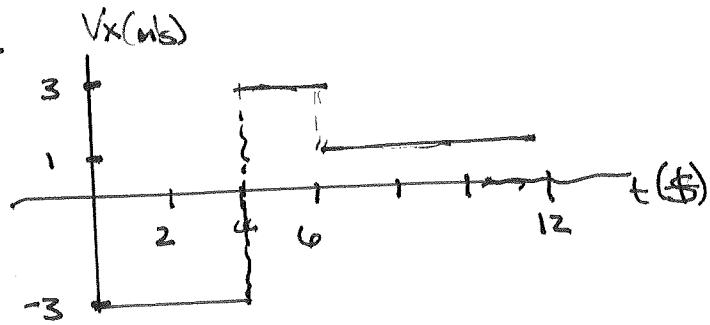
$$= 30 \text{ m}$$

3

just verifying

that AREA UNDER  
Vx plot is EQUAL to  
 $\Delta x$

2.8



DRAW Corresponding X vs t. Assume  $x=0$  at  $t=0$

First: Notice that  $V_x$  consists of 3 horizontal line segments  
 $\Rightarrow$  3 UNIFORM MOTIONS combined together  $\Rightarrow$  3 line segments for  $x$  vs.  $t$

To find distances travelled use  $V_x = \frac{\Delta x}{\Delta t} \Rightarrow \Delta x = V_x \Delta t$  OR EQUIVALENTLY

FIND AREA ON GRAPH. THEN TO FIND POSITION USE  $\Delta x = x_f - x_i \Rightarrow x_f = x_i + \Delta x$

$$V_x = 3 \text{ m/s}$$

For  $0 < t < 4 \text{ s}$   $\Delta t = 4 \text{ s} - 0 = 4 \text{ s} \Rightarrow \Delta x = (-3 \text{ m/s})(4 \text{ s}) = -12 \text{ m}$

~~At  $t=0, x=0 \Rightarrow x_i=0 \Rightarrow x_f = -12 \text{ m}$~~

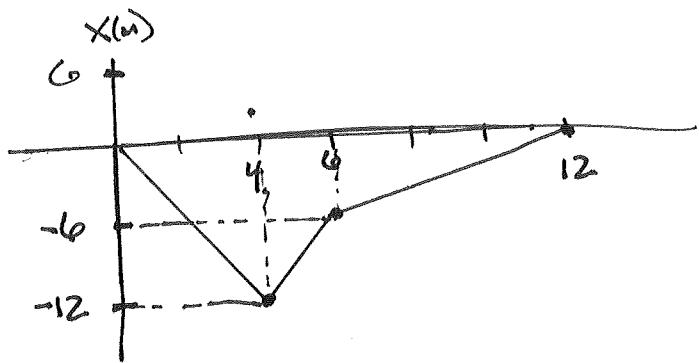
For  $4 \text{ s} < t < 6 \text{ s}$   $\Delta t = 6 \text{ s} - 4 \text{ s} = 2 \text{ s}, V_x = +3 \text{ m/s} \Rightarrow \Delta x = (3 \text{ m/s})(2 \text{ s}) = 6 \text{ m}$

but now  $t_i = 4 \text{ s} \Rightarrow x_i = x \text{ at } 4 \text{ s} = -12 \text{ m} \Rightarrow x_f = -12 \text{ m} + 6 \text{ m} = -6 \text{ m}$

For  $6 \text{ s} < t < 12 \text{ s}, \Delta t = 12 \text{ s} - 6 \text{ s} = 6 \text{ s}, V_x = +1 \text{ m/s} \Rightarrow \Delta x = (1 \text{ m/s})(6 \text{ s}) = 6 \text{ m}$

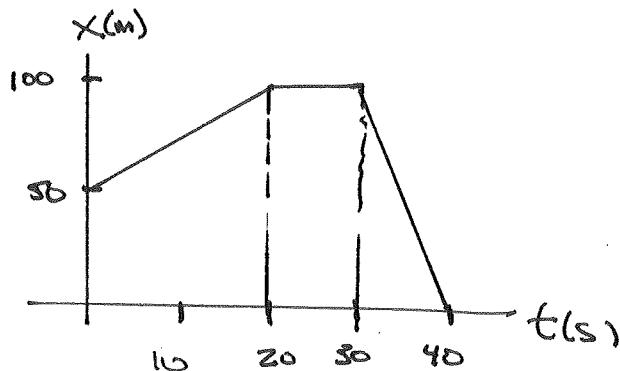
Here  $t_i = 6 \text{ s} \Rightarrow x_i = -6 \text{ m} \Rightarrow x_f = -6 \text{ m} + 6 \text{ m} = 0$

Putting this all together:



Part B: What is  $x$  at  $t=12s$ ?  $x = 0m$

2.9



Notice: 3 straight line  
Segments  $\Rightarrow$  3 UNIFORM  
Motions

a) What is velocity at  $t=10s$

This is  $x$  vs  $t \Rightarrow v_x = \text{slope}$ .  $t=10s$  is during first line segment

$\Rightarrow$  use  ~~$x$~~   $t_i = 0, t_f = 20s, x_i = 50m, x_f = 100m$

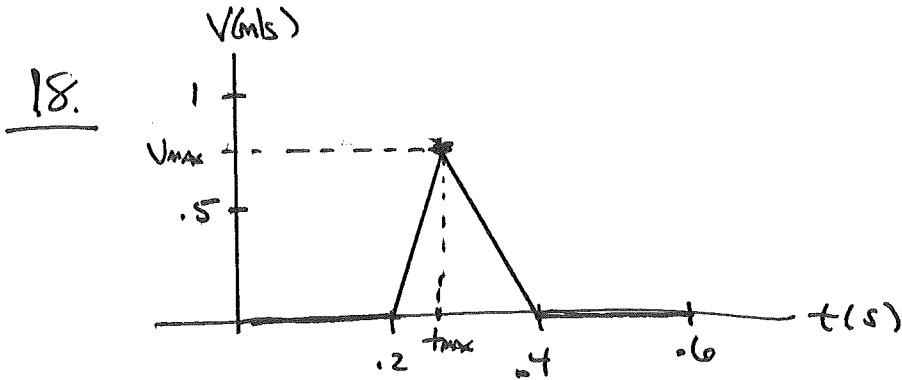
$\Rightarrow v_x = \frac{\Delta x}{\Delta t} \leftarrow$  gives instantaneous velocity Because this is uniform motion

$$v_x = \frac{(100m - 50m)}{(20s - 0)} = \frac{50m}{20s} = 2.5 \text{ m/s}$$

b) What is velocity at  $t=25s$   $\leftarrow$  during 2<sup>nd</sup> segment which is HORIZONTAL  $\Rightarrow v_x = 0$ . OR, EQUIVALENTLY,  $x_i = x_f = 100m$  for 2<sup>nd</sup> segment  $\Rightarrow \Delta x = 0 \Rightarrow v_x = 0$

c)  $v_x$  at  $t=35s$ ? 3<sup>rd</sup> segment has  $t_i = 30s, t_f = 40s \Rightarrow x_i = 100m, x_f = 0$

$$\Rightarrow v_x = \frac{(0 - 100m)}{(40s - 30s)} = \frac{-100m}{10s} = -10 \text{ m/s}$$

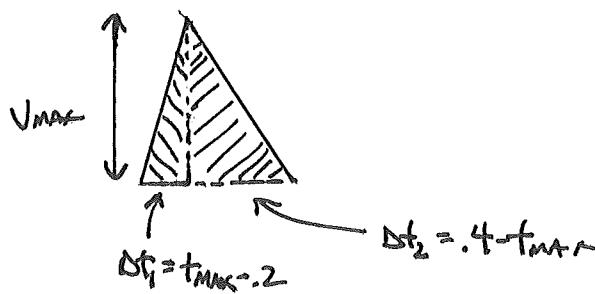


TO MEASURE  
the MAX velocity  
to be HALF WAY  
Between .5 AND 1  
while  $t_{\text{MAX}}$  is About  $\frac{1}{3}$   
of the way Between  
.2 AND .4 s .

You MAY HAVE SLIGHTLY DIFFERENT VALUES.

- a) Approximately how far does blood go during ONE BEAT.

How far  $\Rightarrow$  AREA



$$V_{\text{MAX}} = .75 \text{ m/s} \leftarrow \text{HALFWAY}$$

$$t_{\text{MAX}} = .2 + \frac{1}{3}(.4 - .2)$$

$$= .2 + \frac{1}{3}(.2) = .2667 \text{ s}$$

$$\Rightarrow \Delta t_1 = .0667 \text{ s} \quad \Delta t_2 = .1333 \text{ s}$$

$$\text{Two Triangles} \Rightarrow \Delta X = \frac{1}{2} \Delta t_1 V_{\text{MAX}} + \frac{1}{2} \Delta t_2 V_{\text{MAX}}$$

$$\Delta X = \frac{1}{2} (.0667 \text{ s}) (.75 \text{ m/s}) + \frac{1}{2} (.1333 \text{ s}) (.75 \text{ m/s}) = \frac{1}{2} (.2 \text{ s}) (.75 \text{ m})$$

$$\Rightarrow \boxed{\Delta X = .075 \text{ m} \times \frac{100 \text{ cm}}{\text{m}} = 7.5 \text{ cm}}$$

b) Estimate how many beats from heart to brain.

I (think) its about  $\frac{1}{4}$  meter from brain to heart

$$1\text{m} = .25\text{m} = 25\text{cm}$$

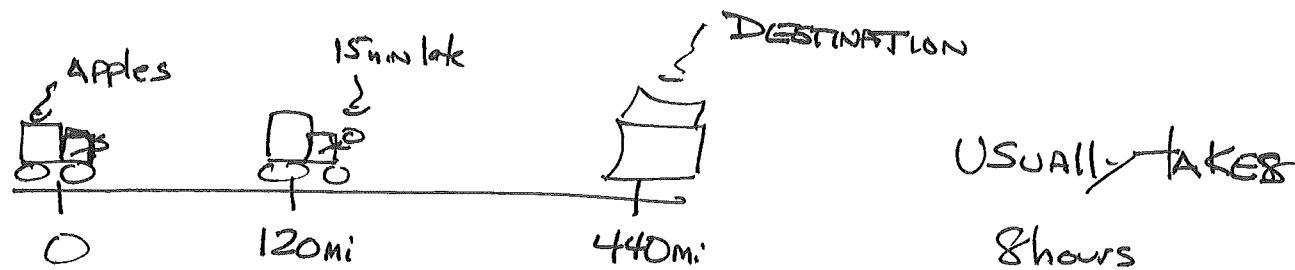
Blood travels 7.5cm/beat

$$\therefore \# \text{ beats} = \frac{25\text{cm}}{7.5\text{cm/beat}} = 3.33 \approx 3 \text{ beats}$$

Note: the original book problem had you estimate your own height. In mastering, they just tell you to use 30cm.

$$\text{For } 30\text{cm, } \# \text{ beats} = \frac{30\text{cm}}{7.5\text{cm/beat}} = 4$$

49



WHAT SPEED FOR REMAINING DISTANCE to make up time.

SPLIT TRIP INTO TWO PIECES : (1) AND (2)  $\rightarrow$  (1) = First 120 mi.  
(2) = REST

$$V_1 = \frac{\Delta X_1}{\Delta t_1} . \quad \Delta X_1 = 120 \text{ mi}, \quad \Delta t_1 = ?, \quad V_1 = ?$$

$$V_2 = \frac{\Delta X_2}{\Delta t_2} . \quad \Delta X_2 = 440 \text{ mi} - 120 \text{ mi} = 320 \text{ mi}, \quad \Delta t_2 = ?$$

$V_2 = ?$  AND  $V_2$  IS FINAL ANSWER.

WE <sup>KNOW</sup>  $\Delta t_1 + \Delta t_2 = 8 \text{ h}$   $\rightarrow$  IF WE FIND  $\Delta t_1$ , WE CAN SOLVE  
FOR  $\Delta t_2$ .

USE THE 15min LATER THAN USUAL;  $\Delta t_1 = \Delta t_{1,\text{USUAL}} + 15 \text{ min}$

$\Delta t_{1,\text{USUAL}}$  = USUAL time to travel  $\Delta X_1 = 120 \text{ mi}$

$$V_{\text{USUAL}} = \frac{440 \text{ mi}}{8 \text{ h}} = 55 \text{ mi/h}$$

$$V_{\text{USUAL}} = \frac{\Delta x_1}{\Delta t_{1,\text{USUAL}}} \Rightarrow 55 \text{ mi/h} = \frac{120 \text{ mi}}{\Delta t_{1,\text{USUAL}}} \Rightarrow \Delta t_{1,\text{USUAL}} = \frac{120 \text{ mi}}{55 \text{ mi/h}}$$

$\approx 2.181818 \text{ h}$

↳ UNIT:  
mi/h = h

$$\Delta t_1 = \Delta t_{1,\text{USUAL}} + 15 \text{ min.} \quad 15 \text{ min} \times \frac{1 \text{ h}}{60 \text{ min}} = .25 \text{ h}$$

$$\Rightarrow \Delta t_1 = 2.431818 \text{ h}$$

$$\Delta t_1 + \Delta t_2 = 8 \text{ h} \Rightarrow \Delta t_2 = 8 \text{ h} - 2.431818 \text{ h} \approx 5.568181 \text{ h}$$

$$\therefore V_2 = \frac{\Delta x_2}{\Delta t_2} = \frac{320 \text{ mi}}{5.568181 \text{ h}} = 57.469 \text{ mi/h} = 57.5 \text{ mi/h}$$

$= 57 \text{ mi/h} \underline{\underline{\text{to 2sg fig}}}$

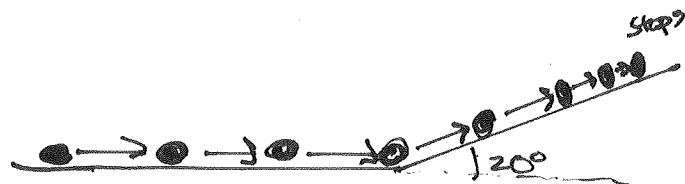
1.39 DRAW Motion Diagram For Ball rolling on Smooth,

Horizontal floor which rolls up a  $20^\circ$  Ramp, AND stops, ~~then~~ (AND then rolls back down)

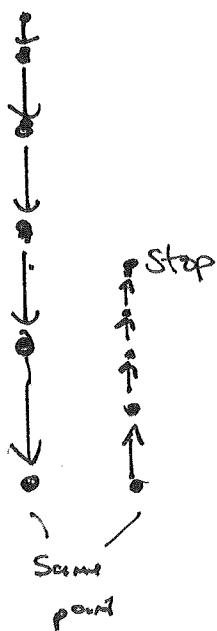
ON ~~Floor~~ ball has constant speed (Hence the word smooth)

⇒ EQUAL SPACING OF dots.

UP RAMP, the ball is slowing down since its speed has changed from 10m/s to zero ⇒ Dots getting closer together.



1.44.



Be Creative!

Jack drops his phone off at the top of his roof of his apartment building. (He was foolishly sunbathing up there) The phone falls with increasing speed. Luckily, Jack has the new "protect-a-phone" app that inflates a small balloon around the phone just before impact. This allows it to bounce back up (but with smaller speed). It flies into the air with decreasing speed and is caught by his roommate Sally, just at the top of its motion.