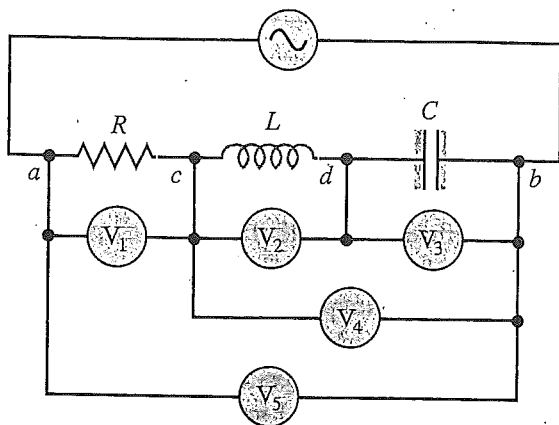


**31.42.** Five infinite-impedance voltmeters, calibrated to read rms values, are connected as shown in Fig 31.25. Let  $R = 200 \Omega$ ,  $L = 0.400 \text{ H}$ ,  $C = 6.00 \mu\text{F}$ , and  $V = 30.0 \text{ V}$ . What is the reading of each voltmeter if (a)  $\omega = 200 \text{ rad/s}$ ; and (b)  $\omega = 1000 \text{ rad/s}$ ?

Figure 31.25 Problem 31.42.



- **31.51.** An  $L$ - $R$ - $C$  series circuit is connected to an ac source of constant voltage amplitude  $V$  and variable angular frequency  $\omega$ . (a) Show that the current amplitude, as a function of  $\omega$ , is

$$I = \frac{V}{\sqrt{R^2 + (\omega L - 1/\omega C)^2}}$$

- (b) Show that the average power dissipated in the resistor is

$$P = \frac{V^2 R / 2}{R^2 + (\omega L - 1/\omega C)^2}$$

- (c) Show that  $I$  and  $P$  are both maximum when  $\omega = 1/\sqrt{LC}$ ; that is, when the source frequency equals the resonance frequency of the circuit. (d) Graph  $P$  as a function of  $\omega$  for  $V = 100 \text{ V}$ ,  $R = 200 \Omega$ ,  $L = 2.0 \text{ H}$ , and  $C = 0.50 \mu\text{F}$ . Compare to the light purple curve in Fig. 31.19. Discuss the behavior of  $I$  and  $P$  in the limits  $\omega = 0$  and  $\omega \rightarrow \infty$ .

- **31.54. The  $L$ - $R$ - $C$  Parallel Circuit.** A resistor, inductor, and capacitor are connected in parallel to an ac source with voltage amplitude  $V$  and angular frequency  $\omega$ . Let the source voltage be given by  $v = V \cos \omega t$ . (a) Show that the instantaneous voltages  $v_R$ ,  $v_L$ , and  $v_C$  at any instant are each equal to  $v$  and that  $i = i_R + i_L + i_C$ , where  $i$  is the current through the source and  $i_R$ ,  $i_L$ , and  $i_C$  are the currents through the resistor, the inductor, and the capacitor, respectively. (b) What are the phases of  $i_R$ ,  $i_L$ , and  $i_C$  with respect to  $v$ ? Use current phasors to represent  $i$ ,  $i_R$ ,  $i_L$ , and  $i_C$ . In a phasor diagram, show the phases of these four currents with respect to  $v$ . (c) Use the phasor diagram of part (b) to show that the current amplitude  $I$  for the current  $i$  through the source is given by  $I = \sqrt{I_R^2 + (I_C - I_L)^2}$ . (d) Show that the result of part (c) can be written as  $I = V/Z$ , with  $1/Z = \sqrt{1/R^2 + (\omega C - 1/\omega L)^2}$ .