

$$T(^{\circ}C) = \frac{5}{9}(T(^{\circ}F) - 32)$$

$$T(K) = T(^{\circ}C) + 273.15$$

$$\Delta L = \alpha L_0 \Delta T$$

$$\Delta V = \beta V_0 \Delta T$$

$$Q = mc\Delta T = nC\Delta T$$

$$Q_{F/V} = \pm mL_{F/V}$$

$$H = \frac{dQ}{dt} = k \frac{A}{L} (T_H - T_C)$$

$$pV = nRT$$

$$K_{tr} = \frac{3}{2} nRT$$

$$C_v = \frac{3}{2} R \quad \text{ideal monatomic gas}$$

$$C_v = \frac{5}{2} R \quad \text{ideal diatomic gas w/o vibration}$$

$$W = \int_{V_1}^{V_2} p dV$$

$$\Delta U = Q - W$$

$$e = \frac{W}{Q_H} = 1 - \left| \frac{Q_C}{Q_H} \right|$$

$$e_{Carnot} = 1 - \left| \frac{T_C}{T_H} \right|$$

$$\Delta S = \int_1^2 \frac{dQ}{T}$$

$$S = k \ln w$$

$$R = 8.314 \text{ J/mol} \cdot \text{K}$$

$$N_A = 6.02 \times 10^{23} \text{ molecules/mole}$$

$$1 \text{ atm} = 101325 \text{ N/m}^2$$

$$1/4\pi\epsilon_0 = 8.99 \times 10^9 \text{ Nm}^2/\text{C}^2$$

$$e = -1.602 \times 10^{-19} \text{ C}$$

$$\vec{F}_E = q\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{qQ}{r^2} \hat{r}$$

$$\Phi_E = \oint \vec{E} \cdot d\vec{A} = \frac{q_{enc}}{\epsilon_0}$$

$$V_b - V_a = - \int_a^b \vec{E} \cdot d\vec{l}$$

$$\Delta U = q\Delta V$$

$$\vec{E} = - \left( \hat{i} \frac{\partial V}{\partial x} + \hat{j} \frac{\partial V}{\partial y} + \hat{k} \frac{\partial V}{\partial z} \right)$$

$$Q = CV$$

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots \quad \text{series}$$

$$C_{eq} = C_1 + C_2 + C_3 + \dots \quad \text{parallel}$$

$$U = \frac{1}{2} CV^2$$

$$u_E = \frac{1}{2} \epsilon_0 E^2$$

$$E = \frac{E_0}{K}$$

$$I = \frac{dq}{dt}$$

$$\vec{J} = nq\vec{v}_d$$

$$\rho = \frac{E}{J}$$

$$V = IR$$

$$P = VI$$

$$R_{eq} = R_1 + R_2 + R_3 + \dots \quad \text{series}$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots \quad \text{parallel}$$

$$q = C\mathcal{E} \left( 1 - e^{-t/RC} \right) \quad \text{charging}$$

$$q = Q_0 e^{-t/RC} \quad \text{discharging}$$

$$\vec{F} = q\vec{v} \times \vec{B}$$

$$\Phi_B = \int \vec{B} \cdot d\vec{A}$$

$$d\vec{F} = Id\vec{l} \times \vec{B}$$

$$\vec{\tau} = \vec{\mu} \times \vec{B}, \quad \vec{\mu} = NI\vec{A}$$

$$U = -\vec{\mu} \cdot \vec{B}$$

$$\vec{B} = \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \hat{r}}{r^2}$$

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{Id\vec{l} \times \hat{r}}{r^2}$$

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 (i_C + i_D)$$

$$\oint \vec{E} \cdot d\vec{l} = \mathcal{E} = - \frac{d\Phi_B}{dt}$$

$$i_D = \varepsilon \frac{d\Phi_E}{dt}$$

$$\mathcal{E}_2 = -M \frac{di_1}{dt} \text{ and } \mathcal{E}_1 = -M \frac{di_2}{dt}$$

$$M = \frac{N_2 \Phi_{B2}}{i_1} = \frac{N_1 \Phi_{B1}}{i_2}$$

$$\mathcal{E} = -L \frac{di}{dt},$$

$$L = \frac{N\Phi_B}{i}$$

$$U = \frac{1}{2} LI^2, \quad u_E = \frac{1}{2\mu_0} B^2,$$

$$\frac{di}{dt} = \frac{\mathcal{E}}{L} e^{-Rt/L}$$

$$\omega = \frac{1}{\sqrt{LC}}$$

$$I_{RMS} = \frac{1}{\sqrt{2}} I \text{ for } i = I \cos(\omega t)$$

$$V_{RMS} = \frac{1}{\sqrt{2}} V \text{ for } v = V \cos(\omega t)$$

$$V_R = IR$$

$$V_L = IX_L, \text{ where } X_L = \omega L$$

$$V_C = IX_C, \text{ where } X_C = \frac{1}{\omega C}$$

$$V = IZ, \text{ where } Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$P_{Avg} = \frac{1}{2} VI \cos \varphi, \quad \tan \varphi = \frac{X_L - X_C}{R}$$

$$V_s = V_p \frac{N_s}{N_p}$$

## Calculus

### Derivatives:

$$\frac{d}{dx} x^n = nx^{n-1}$$

$$\frac{d}{dx} \ln ax = \frac{1}{x}$$

$$\frac{d}{dx} e^{ax} = ae^{ax}$$

$$\frac{d}{dx} \sin ax = a \cos ax$$

$$\frac{d}{dx} \cos ax = -a \sin ax$$

### Integrals:

$$\int x^n dx = \frac{x^{n+1}}{n+1} \quad (n \neq -1)$$

$$\int \frac{dx}{x} = \ln x$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax}$$

$$\int \sin ax dx = -\frac{1}{a} \cos ax$$

$$\int \cos ax dx = \frac{1}{a} \sin ax$$

$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \arcsin \frac{x}{a}$$

$$\int \frac{dx}{\sqrt{x^2 + a^2}} = \ln(x + \sqrt{x^2 + a^2})$$

$$\int \frac{dx}{x^2 + a^2} = \frac{1}{a} \arctan \frac{x}{a}$$

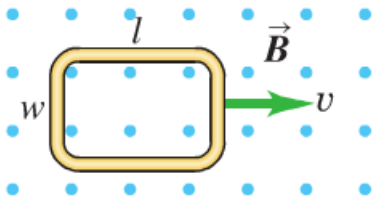
$$\int \frac{dx}{(x^2 + a^2)^{3/2}} = \frac{1}{a^2} \frac{x}{\sqrt{x^2 + a^2}}$$

$$\int \frac{x dx}{(x^2 + a^2)^{3/2}} = -\frac{1}{\sqrt{x^2 + a^2}}$$

# Physics 161-001 Spring 2013 Exam 4

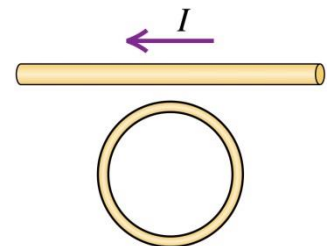
Name: \_\_\_\_\_ Box# \_\_\_\_\_

1) A flat rectangular coil of dimensions  $l = 5.0$  cm and  $w = 2.0$  cm is pulled with uniform speed  $v = 2.0$  m/s through a uniform magnetic field  $B = 2.0$  T with the plane of its area perpendicular to the magnetic field as shown. The coil has a resistance of  $10.0 \Omega$ . What is the current induced in this coil?



- A) 0.0 A
- B) 1.0 A
- C) 2.0 A
- D) 3.0 A
- E) 4.0 A
- F) 5.0 A
- G) 6.0 A
- H) 7.0 A
- I) 8.0 A
- J) 9.0 A

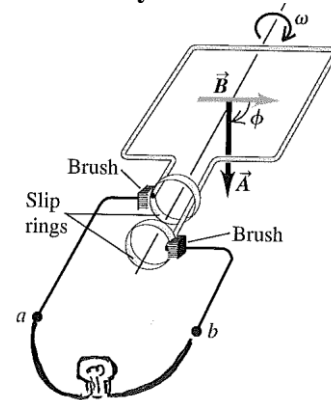
2) A circular loop of wire is initially held below a long straight wire carrying a constant current  $I$ . The loop is then released, so that it can fall. All this takes place near the earth's surface. A moment after the loop is released, the downward acceleration that the loop experiences is:



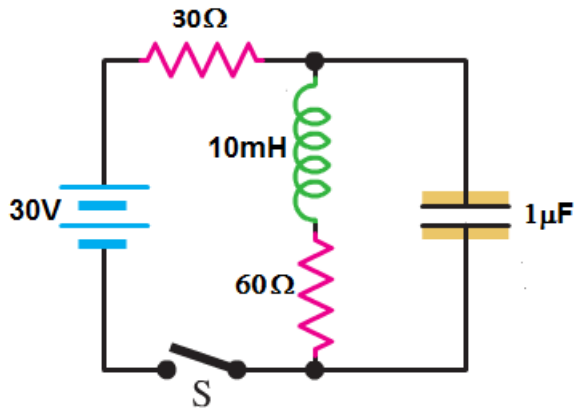
- A) zero.
- B) equal to  $g$ , the acceleration due to gravity near the earth's surface, and constant.
- C) equal to  $g$ , the acceleration due to gravity near the earth's surface, and increasing.
- D) equal to  $g$ , the acceleration due to gravity near the earth's surface, and decreasing.
- E) greater than  $g$ , the acceleration due to gravity near the earth's surface, and constant.
- F) greater than  $g$ , the acceleration due to gravity near the earth's surface, and increasing.
- G) greater than  $g$ , the acceleration due to gravity near the earth's surface, and decreasing.
- H) less than  $g$ , the acceleration due to gravity near the earth's surface, and constant.
- I) less than  $g$ , the acceleration due to gravity near the earth's surface, and increasing.
- J) less than  $g$ , the acceleration due to gravity near the earth's surface, and decreasing.

3) A rectangular coil is rotated at angular speed  $\omega$  in a uniform horizontal  $B$  field, as shown. What is the position of the coil when the emf around the loop is momentarily zero?

- A) in the orientation shown
- B)  $90^\circ$  clockwise (loop vertical)**
- C)  $180^\circ$  flipped from what is shown
- D) the EMF is never zero through the loop
- E) at an intermediate position



4) In the DC circuit shown, immediately after the switch is closed, what is the current through the capacitor?



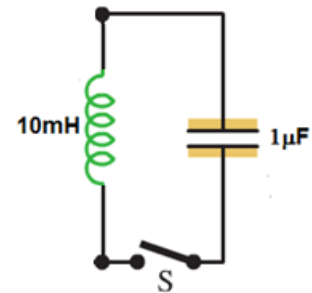
- A) 0 A
- B)  $10^{-6}$  A
- C)  $30 \times 10^{-6}$  A
- D) 0.3 A
- E) 0.5 A
- F) 1 A**
- G) 3 A
- H) 30 A
- I)  $3 \times 10^5$  A
- J) cannot determine

5) In the same circuit, what is the potential across the inductor immediately after the switch is closed?

- A) 0 V**
- B)  $3 \times 10^{-3}$  V
- C) 0.1 V
- D) 0.3 V
- E) 0.5 V
- F) 1 V
- G) 5 V
- H) 10 V
- I) 30 V
- J) cannot determine

6) In the circuit below, if the capacitor initially has a charge  $10 \times 10^{-6} \text{C}$ , what is the value of  $di/dt$  (the time rate of change of the current through the inductor) immediately after the switch is closed?

- A) 0 A/s
- B) 1.0 A/s
- C) 5.0 A/s
- D) 10 A/s
- E) 20 A/s
- F) 50 A/s
- G) 100 A/s
- H) 300 A/s
- I) 600 A/s
- J) 1000 A/s**



7) In the previous problem, assuming that the damping factor is small enough to ignore, what is the approximate angular frequency of the subsequent oscillation, if any?

- A) there is no oscillation
- B)  $1 \times 10^{-8} \text{ rad/s}$
- C)  $6 \times 10^{-3} \text{ rad/s}$
- D) 10 rad/s
- E)  $1 \times 10^2 \text{ rad/s}$
- F)  $3 \times 10^2 \text{ rad/s}$
- G)  $1 \times 10^4 \text{ rad/s}$**
- H)  $4 \times 10^4 \text{ rad/s}$
- I)  $1 \times 10^6 \text{ rad/s}$
- J)  $6 \times 10^6 \text{ rad/s}$

8) You are given a solenoid of length 1m and cross-sectional area of  $0.01 \text{m}^2$ . If you double the current through the solenoid, what happens to the self inductance of the solenoid?

- A) Nothing.**
- B) It goes up by a factor of  $\sqrt{2}$ .
- C) It goes up by a factor of 2.
- D) It goes up by a factor of 4.
- E) It goes down by a factor of  $\sqrt{2}$ .
- F) It goes down by a factor of 2.
- G) It goes down by a factor of 4.

9) In an LC circuit, with  $L = 10 \text{ H}$  and  $C = 1 \text{ mF}$ , the capacitor has an initial total energy stored in its electric field of  $1 \text{ mJ}$ , and the inductor initially has no current through it.  $314 \text{ ms}$  later, what is the total energy stored in the inductor?

- A) Not enough information to solve.
- B)  $0 \text{ J}$
- C)  $0.25 \text{ mJ}$
- D)  $0.33 \text{ mJ}$
- E)  $0.5 \text{ mJ}$
- F)  $1 \text{ mJ}$**
- G)  $-0.25 \text{ mJ}$
- H)  $-0.33 \text{ mJ}$
- I)  $-0.5 \text{ mJ}$
- J)  $-1 \text{ mJ}$

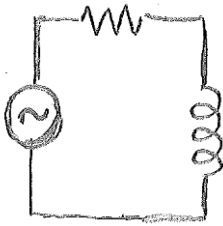
10) A capacitor is charging in a simple RC circuit with a dc battery. Which one of the following statements about this capacitor is accurate?

- A) There is a magnetic field between the capacitor plates because charge travels between the plates by jumping from one plate to the other.
- B) There is a magnetic field between the capacitor plates, even though no charge travels between them, because the magnetic flux between the plates is changing.
- C) There is no magnetic field between the capacitor plates because no charge travels between the plates.
- D) The magnetic field between the capacitor plates is increasing with time because the charge on the plates is increasing.
- E) There is a magnetic field between the capacitor plates, even though no charge travels between them, because the electric flux between the plates is changing.**

11) For a long ideal solenoid having a circular cross-section, the magnetic field strength within the solenoid is given by the equation  $B(t) = (2.0 \text{ T/s})t$ , where  $t$  is time in seconds. If, at  $t = 2\text{s}$ , the induced electric field outside the solenoid is  $1.0 \text{ V/m}$  at a distance of  $2.0 \text{ m}$  from the axis of the solenoid, find the radius of the solenoid.

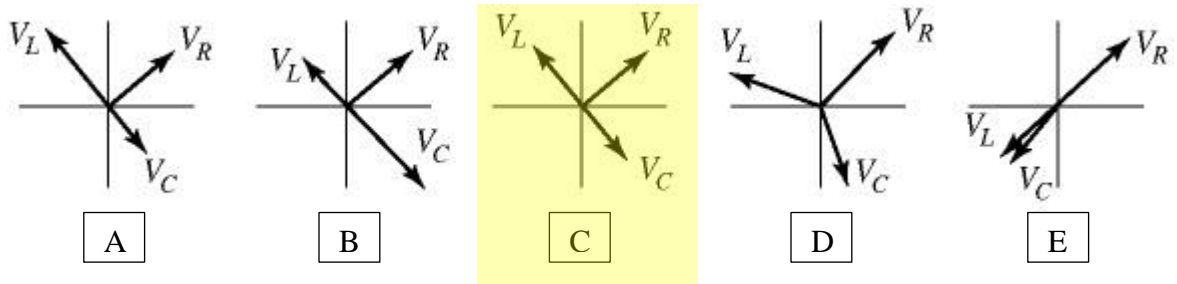
- A)  $0.2 \text{ m}$
- B)  $0.6 \text{ m}$
- C)  $0.9 \text{ m}$
- D)  $1.0 \text{ m}$
- E)  $1.2 \text{ m}$
- F)  $1.4 \text{ m}$**
- G)  $1.6 \text{ m}$
- H)  $1.8 \text{ m}$
- I)  $2.0 \text{ m}$
- J) Not enough information to solve.

12) In the AC circuit shown, the amplitude of the voltage across the inductor is 4 V; the amplitude of the voltage across the resistor is 3 V. Use a phasor diagram to determine the amplitude of the voltage provided by the source.

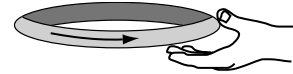


- A) 1 V
- B) 2 V
- C) 3 V
- D) 4 V
- E) 5 V**
- F) 6 V
- G) 7 V
- H) 8 V
- I) 9 V
- J) 10 V

13) Which one of the phasor diagrams shown below best represents a series *LRC* circuit driven at resonance?



14) Suppose it is known that at time  $t_0$  the current in a conducting loop held in place is in the indicated direction.



Which of the following statements I–III about an external magnetic field through the loop at time  $t_0$  could be true?

- I. The external magnetic field is directed upward.
- II. The external magnetic field is directed downward.
- III. The external magnetic field is zero.

- A. Only I could be true.
- B. Only II could be true.
- C. Only III could be true.
- D. Either I or II could be true, but not III.
- E. Any of I, II, or III could be true.

15) An ideal transformer consists of a 500-turn primary coil and a 1500-turn secondary coil. If the current in the secondary is 3.0 A, what is the current in the primary?

- A) 1 A
- B) 2 A
- C) 3 A
- D) 4 A
- E) 5 A
- F) 6 A
- G) 7 A
- H) 8 A
- I) 9 A
- J) 10 A